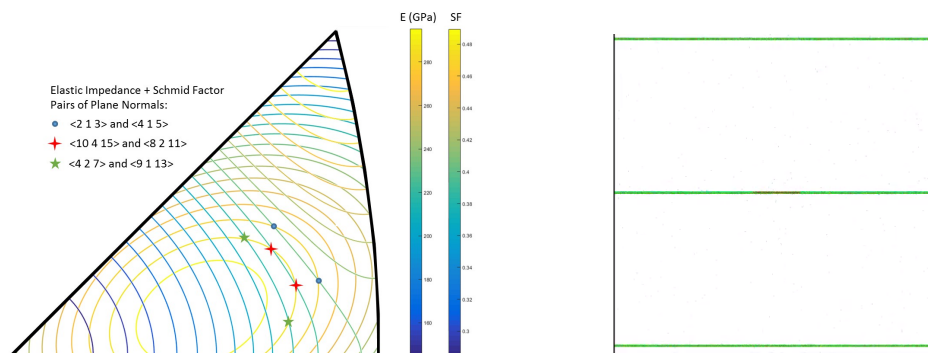


Exceptional service in the national interest



A primer on selecting grain boundary sets for comparison of interfacial fracture properties in MD simulations



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LAMMPS random fact of the day:

Fast parallel algorithms for short-range molecular dynamics

[S Plimpton](#) - [Journal of computational physics](#), 1995 - Elsevier

Three parallel algorithms for classical molecular dynamics are presented. The first assigns each processor a fixed subset of atoms; the second assigns each a fixed subset of inter-atomic forces to compute; the third assigns each a fixed spatial region. The algorithms are

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crack

About 1,590 results (0.03 sec)

interfacial crack

About 563 results (0.07 sec)

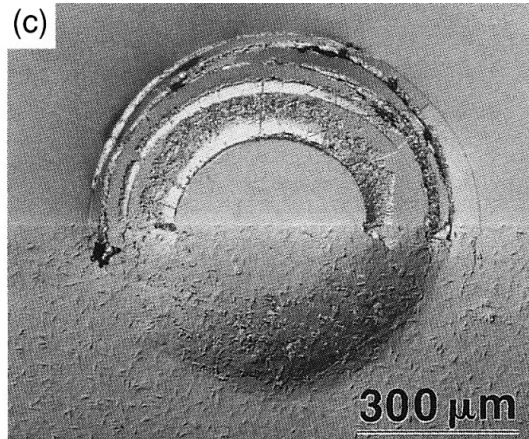
Fast parallel algorithms for short-range molecular dynamics

Search within citing articles

[Source: Google scholar as a 8/3/2017]

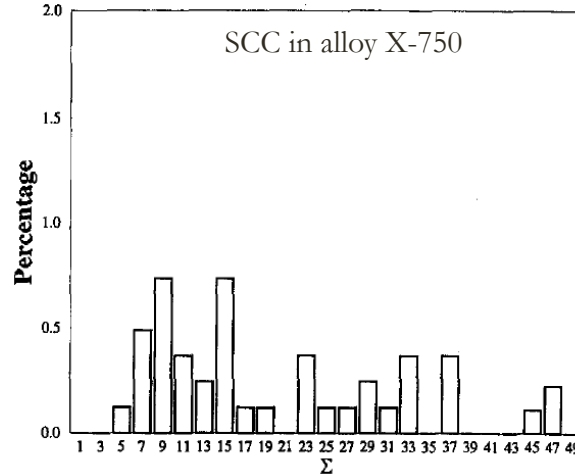
Fundamentals of fracture processes influenced by interfacial structure

Crack resistant glass/ceramic



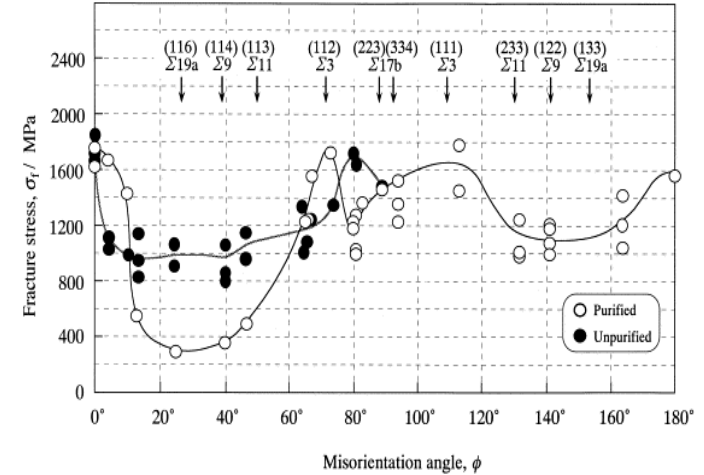
[Wuttiphon, 1996, JAmCeramSoc]

GB effects on intergranular SCC



[Pan, 1996, ActaMater]

Fracture stress in Mo bicrystals



[Watanabe, 1999, ActaMater]

■ Interfacial attributes of importance:

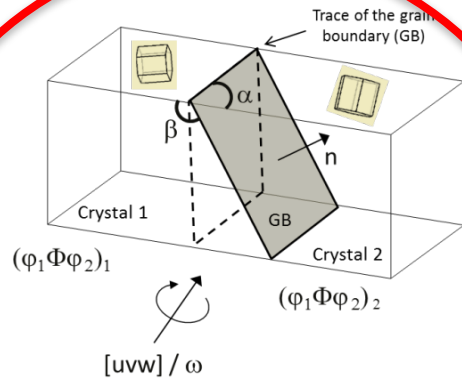
- Elastic mismatch
- Degree of symmetry
- Interfacial coherency (structure)

(physical and the chemical nature between both phases)

$$\sigma(r, \theta) = \frac{\Re(Kr^{i\epsilon})}{\sqrt{2\pi r}} \hat{\sigma}^I(\theta) + \frac{\Im(Kr^{i\epsilon})}{\sqrt{2\pi r}} \hat{\sigma}^{II}(\theta) + \frac{K_{III}}{\sqrt{2\pi r}} \hat{\sigma}^{III}(\theta)$$

$$\epsilon = \frac{1}{2\pi} \ln \left(\frac{1 - \beta}{1 + \beta} \right), \quad \beta = \frac{\mu_1(k_2 - 1) - \mu_2(k_1 - 1)}{\mu_1(k_2 + 1) + \mu_2(k_1 + 1)}$$

How do we isolate (decouple) the role of the interface structure on interfacial fracture?



Misorientation space

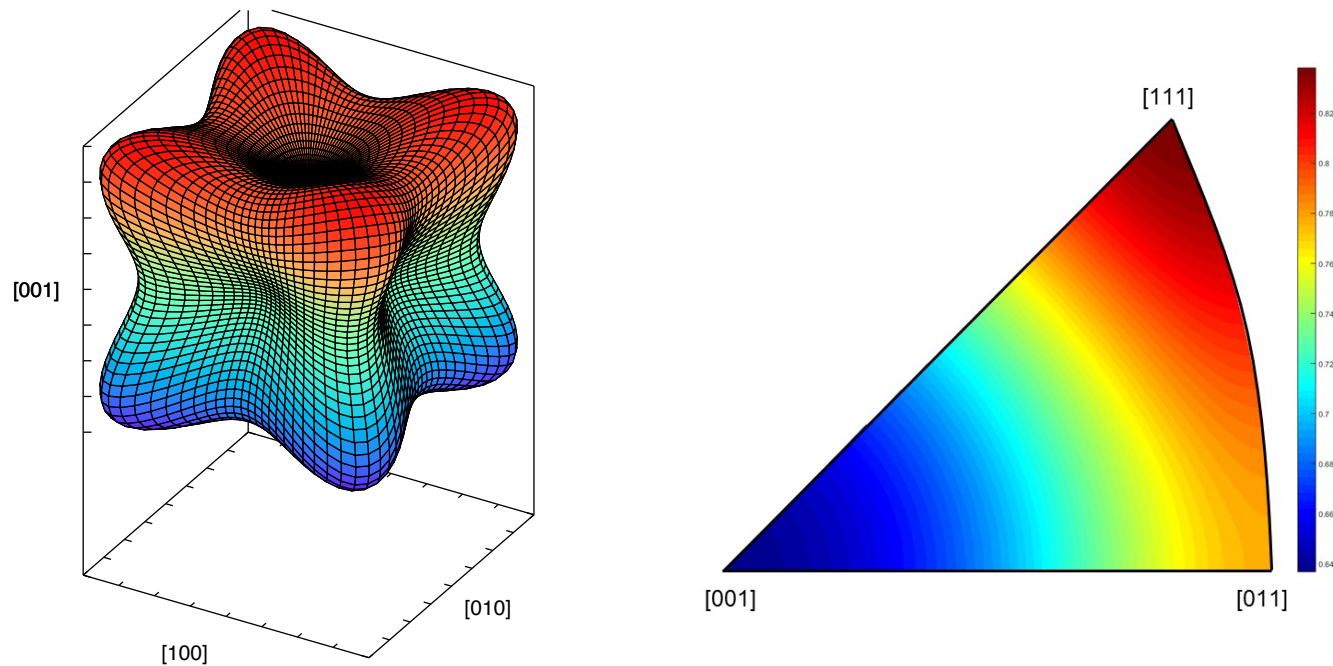
$$\sigma(r, \theta) = \frac{\Re(Kr^{i\epsilon})}{\sqrt{2\pi r}} \hat{\sigma}^I(\theta) + \frac{\Im(Kr^{i\epsilon})}{\sqrt{2\pi r}} \hat{\sigma}^{II}(\theta) + \frac{K_{III}}{\sqrt{2\pi r}} \hat{\sigma}^{III}(\theta)$$

$$\epsilon = \frac{1}{2\pi} \ln \left(\frac{1 - \beta}{1 + \beta} \right), \quad \beta = \frac{\mu_1(k_2 - 1) - \mu_2(k_1 - 1)}{\mu_1(k_2 + 1) + \mu_2(k_1 + 1)}$$

Fracture properties space

- Create grain boundaries with matching important fracture-related properties of adjoining lattices:
 - Anisotropic elastic moduli
 - Schmid factor
 - Slip mode

Criterion: Elastic Anisotropy

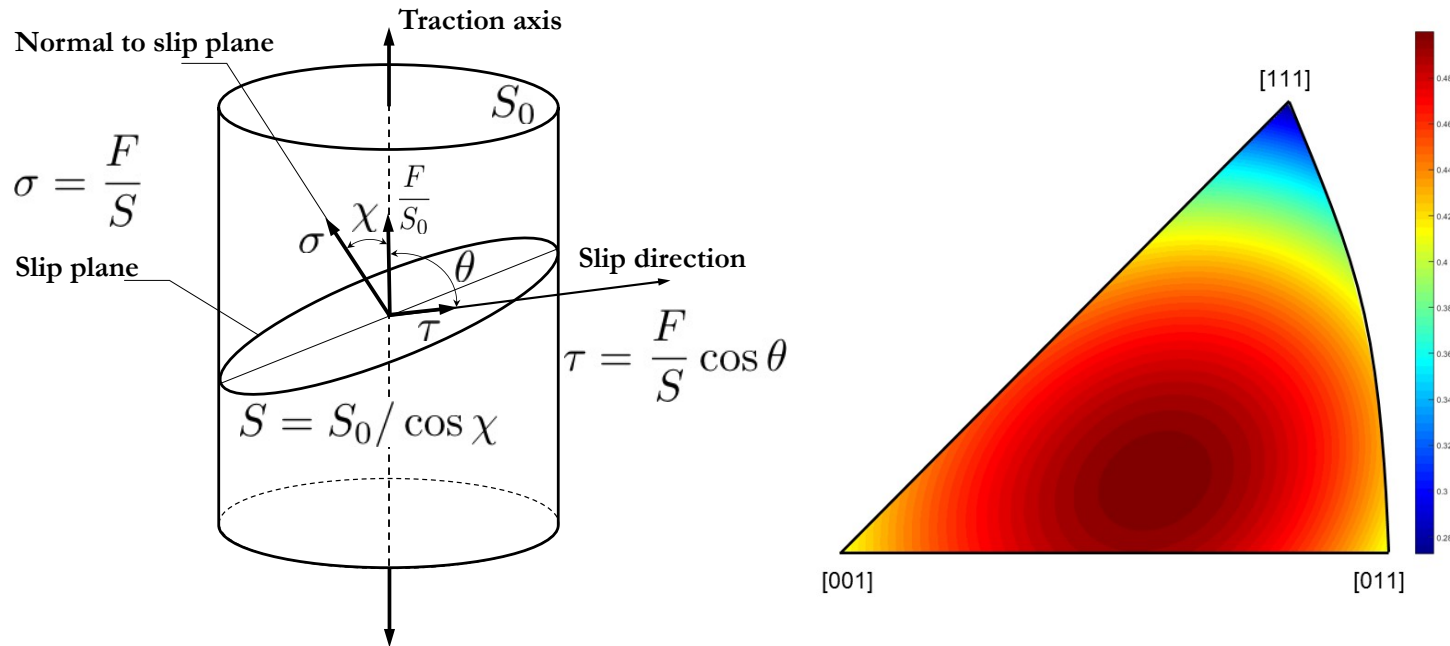


- **Orientation dependent Young's modulus:**

$$\frac{1}{E_{\vec{X}}} = \frac{C_{11} + C_{12}}{(C_{11} - C_{12})(C_{11} + 2C_{12})} + \left(\frac{1}{C_{44}} - 2 \frac{1}{C_{11} - C_{12}} \right) \frac{x_1^2 x_2^2 + x_2^2 x_3^2 + x_1^2 x_3^2}{\|\vec{X}\|^4}$$

- Difference in elastic anisotropy lead to localization effects at GB but also a contributing factor for SIF (Dundur's parameters)

Criterion: Schmid factor for primary slip



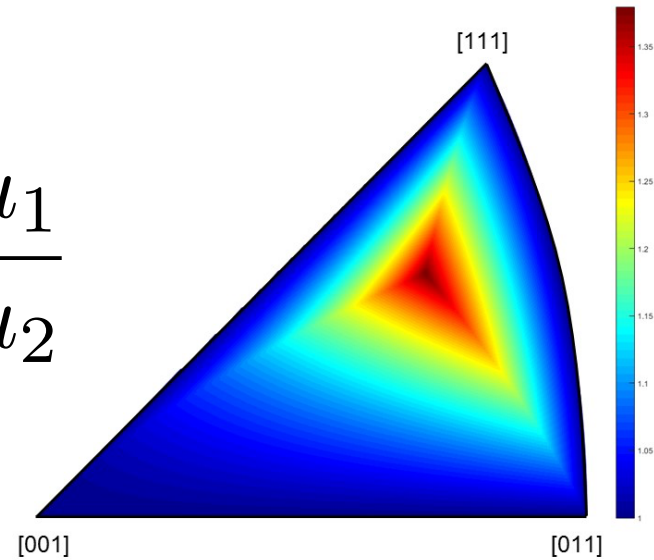
$$\tau^\alpha = \mu^\alpha \cdot \sigma, \text{ with } \mu^\alpha = \cos \chi \cos \theta$$

- Largest resolved shear stress on any slip system defines the primary slip system to be activated upon plasticity activity.

Criterion: Slide mode

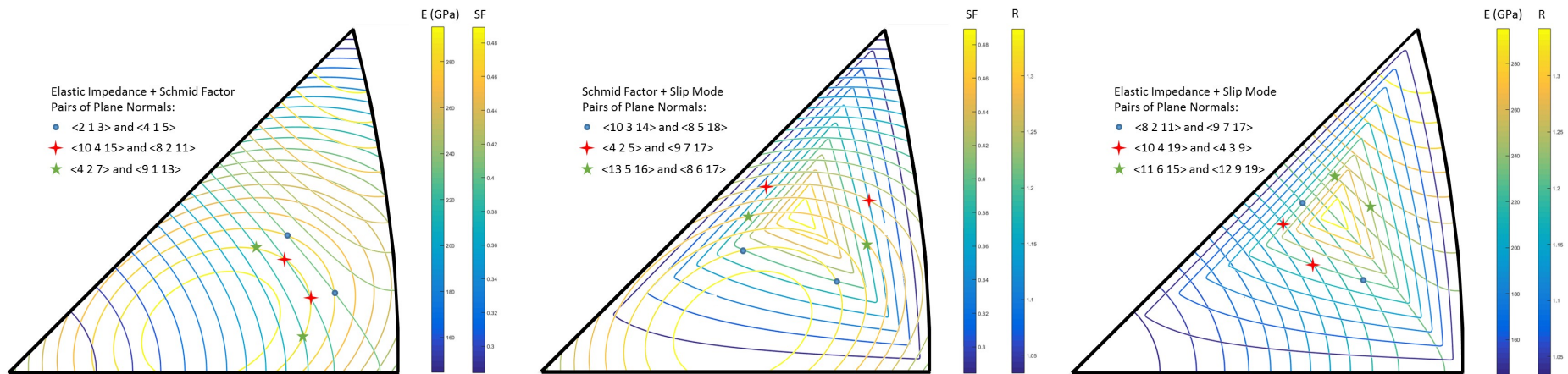
$$\mu^\alpha = \begin{bmatrix} \mu^1 \\ \mu^2 \\ \mu^3 \\ \cdot \\ \cdot \\ \mu^n \end{bmatrix}$$

$$R_\mu = \frac{\mu_1}{\mu_2}$$



- Slip mode and potential for second slip system to be activated with respect to first activated slip system:
 - Single versus multi-slip

Eliminating role of selected lattice attributes in comparative analysis of interfacial fracture:



■ Matching of lattice attributes:

- Directional Young's modulus and Schmid factor for primary slip
 - Importance of elastic/plastic transition
- Directional Young's modulus and slip mode
 - Importance of partitioning of dislocation activities
- Schmid factor for primary slip and slip mode
 - Importance of elastic anisotropy/elastic impedance

Grouping orientations

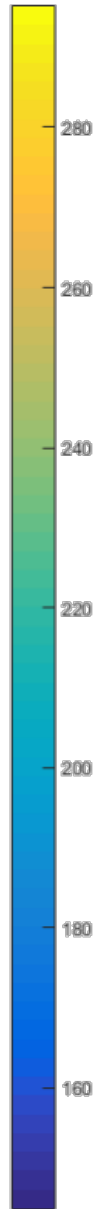
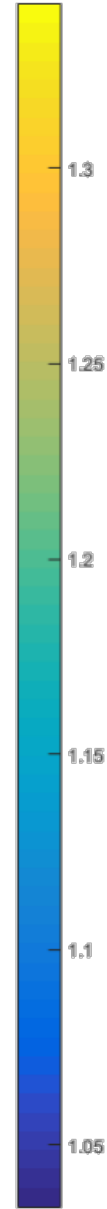
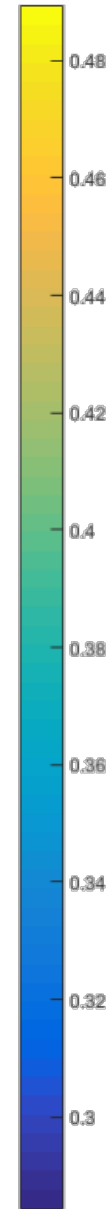
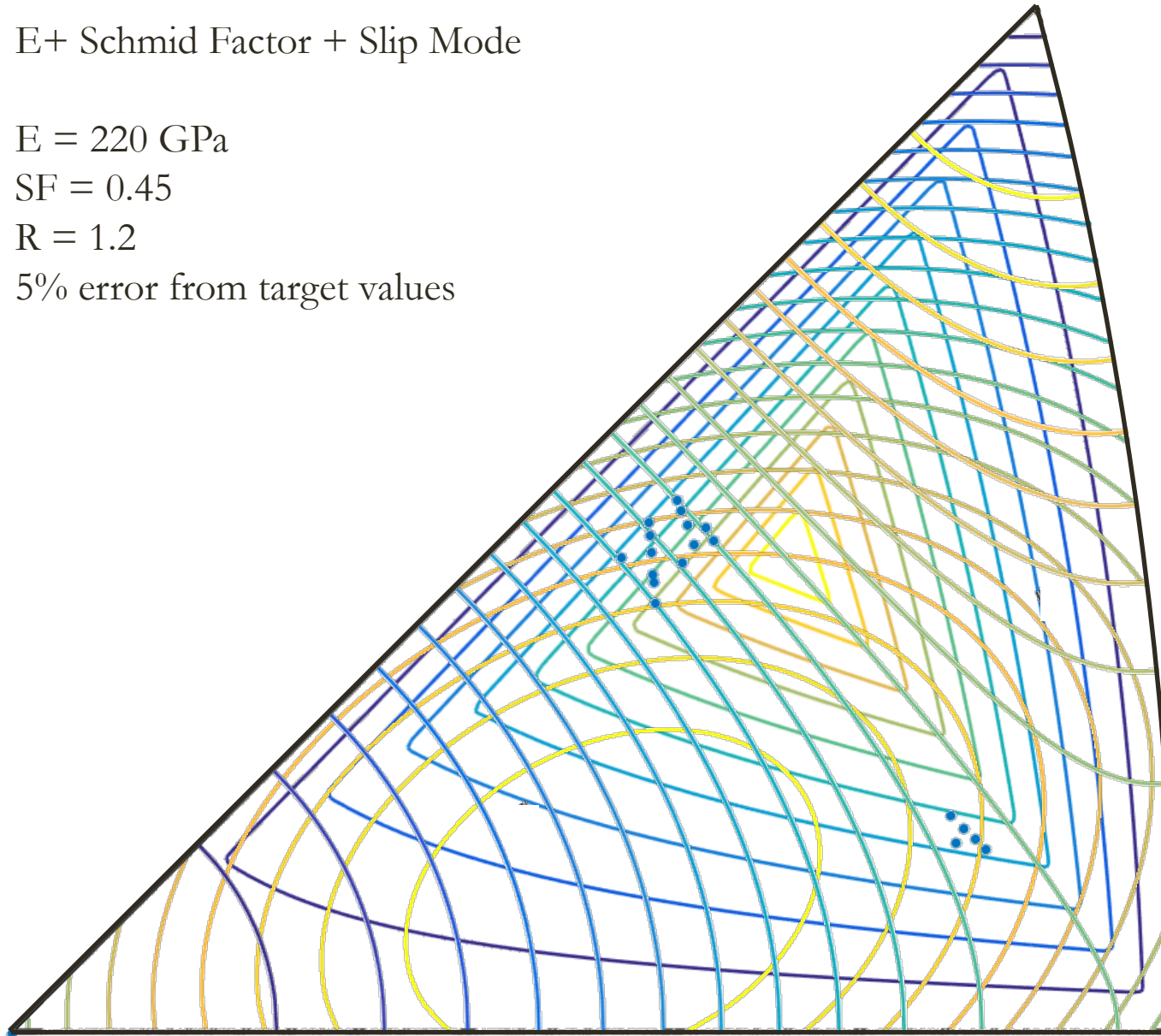
E+ Schmid Factor + Slip Mode

$E = 220 \text{ GPa}$

$SF = 0.45$

$R = 1.2$

5% error from target values



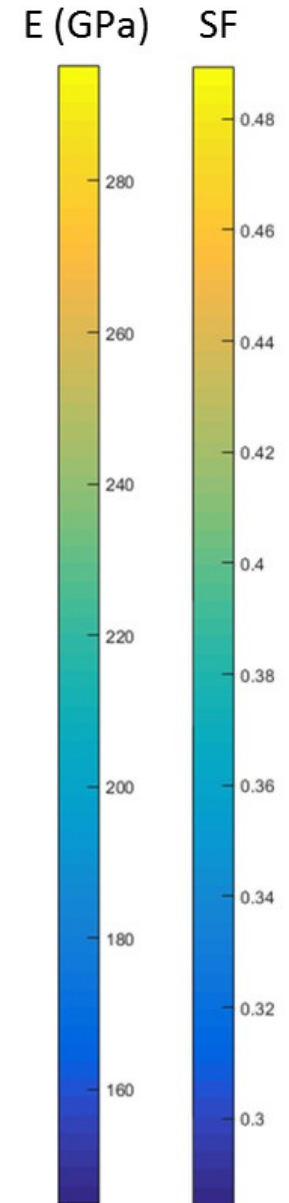
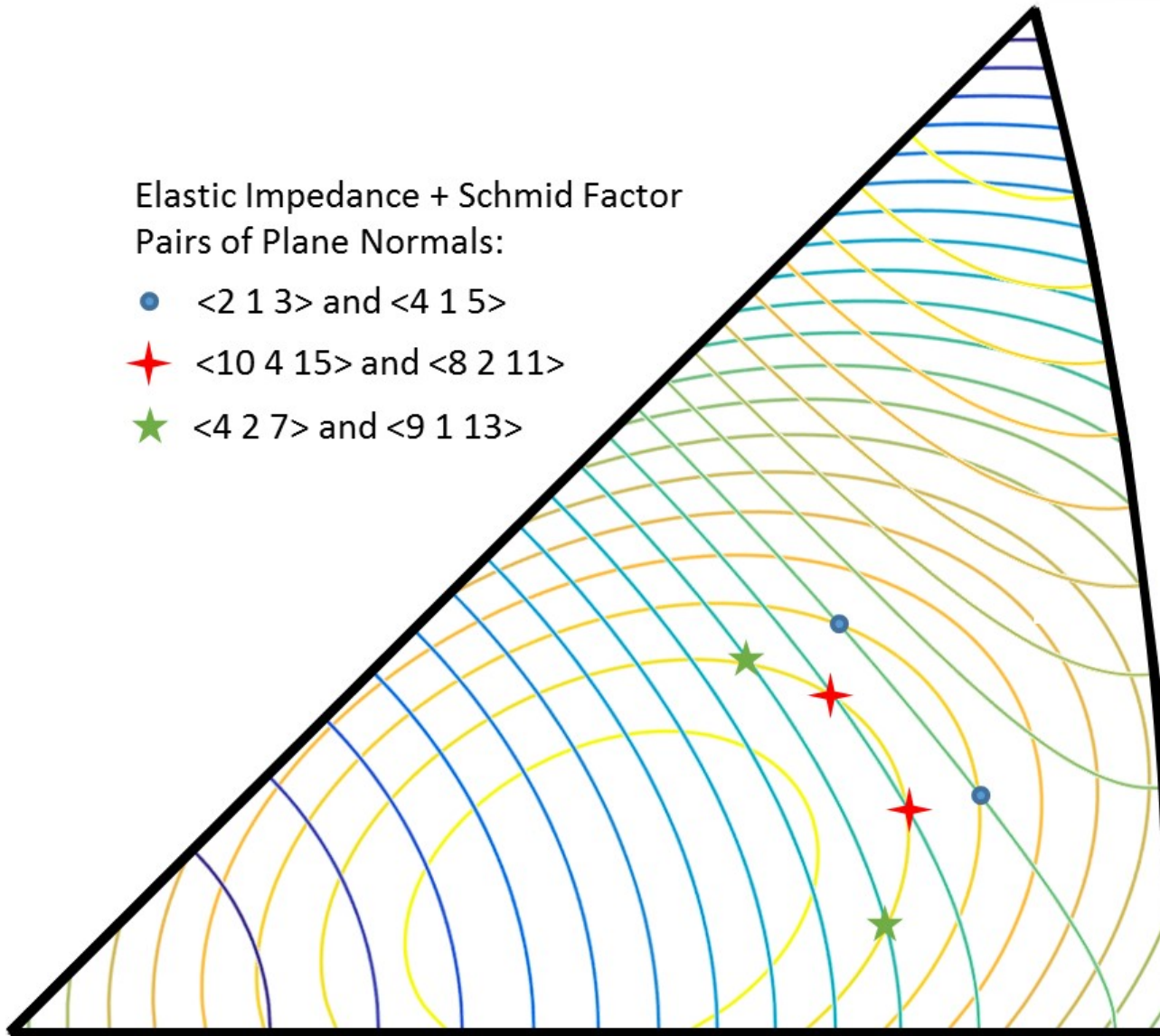
Case study

Elastic Impedance + Schmid Factor
Pairs of Plane Normals:

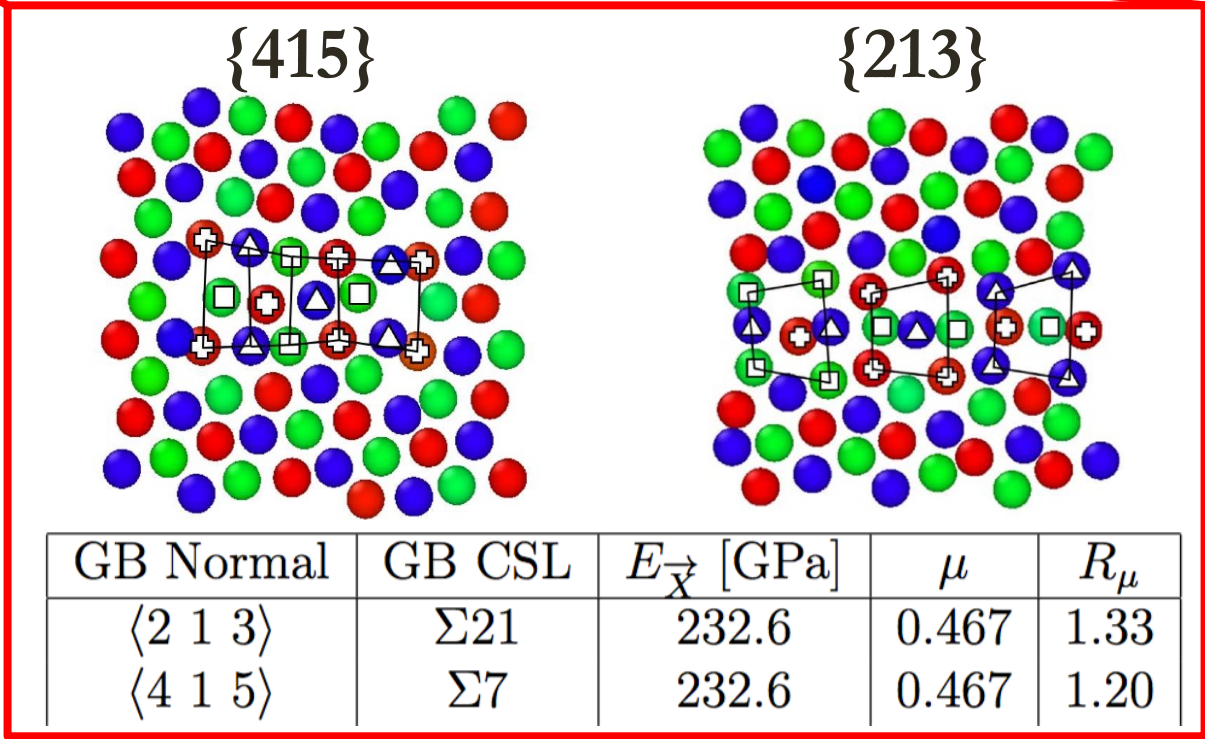
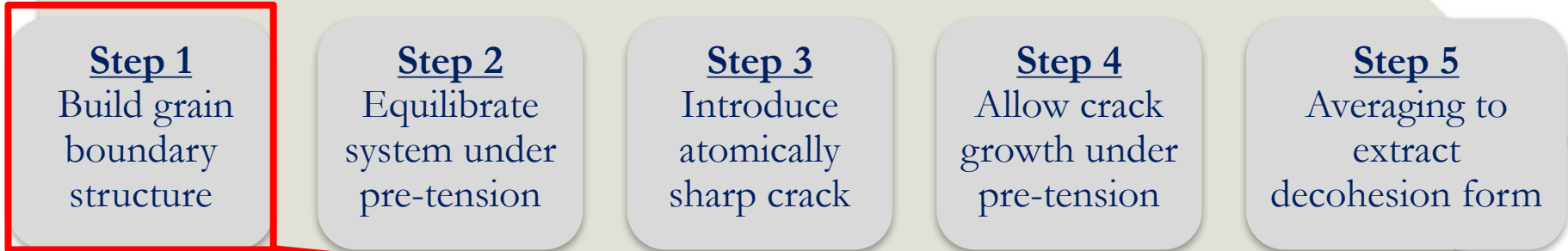
● $\langle 2\ 1\ 3 \rangle$ and $\langle 4\ 1\ 5 \rangle$

★ $\langle 10\ 4\ 15 \rangle$ and $\langle 8\ 2\ 11 \rangle$

★ $\langle 4\ 2\ 7 \rangle$ and $\langle 9\ 1\ 13 \rangle$



Simulating steady-state fracture



[Yamakov et al., 2006, JMPS]
[Barrows et al., 2016, MSEA]

Simulating steady-state fracture

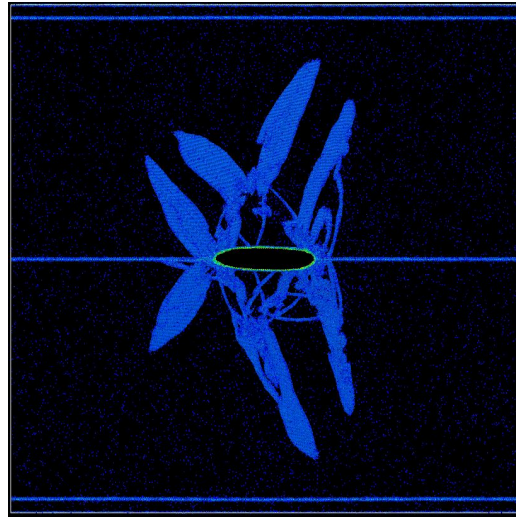
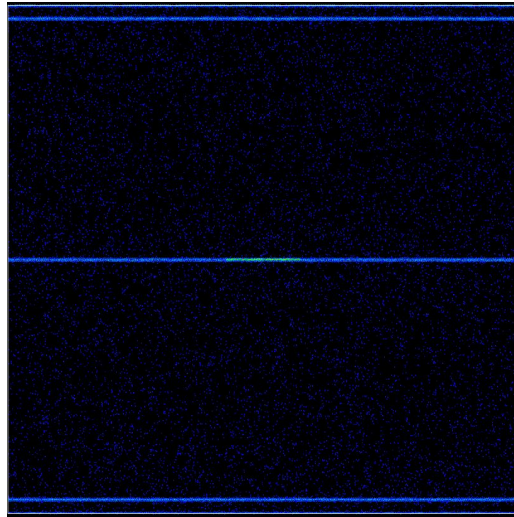
Step 1
Build grain
boundary
structure

Step 2
Equilibrate
system under
pre-tension

Step 3
Introduce
atomically
sharp crack

Step 4
Allow crack
growth under
pre-tension

Step 5
Averaging to
extract
decohesion form



- Avoids having to artificially impose a boundary velocity

Simulating steady-state fracture

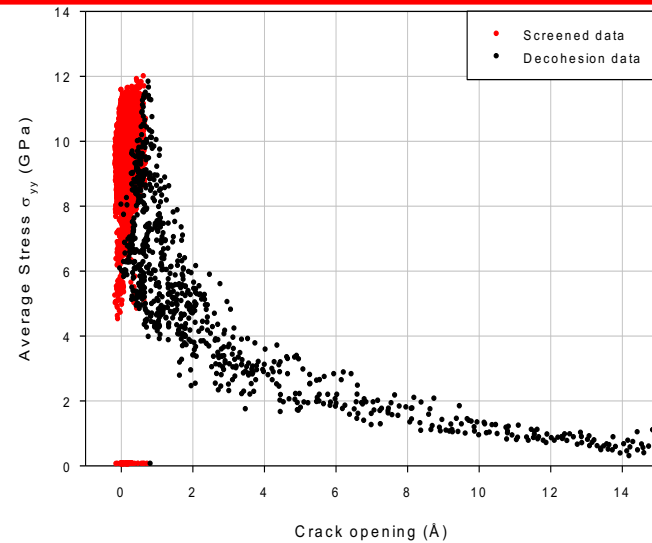
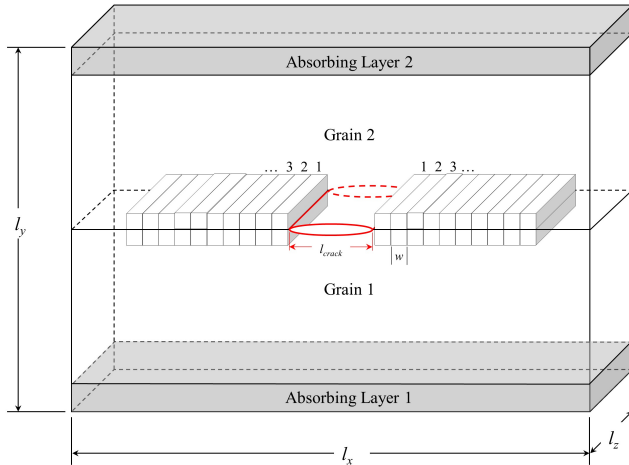
Step 1
Build grain boundary structure

Step 2
Equilibrate system under pre-tension

Step 3
Introduce atomically sharp crack

Step 4
Allow crack growth under pre-tension

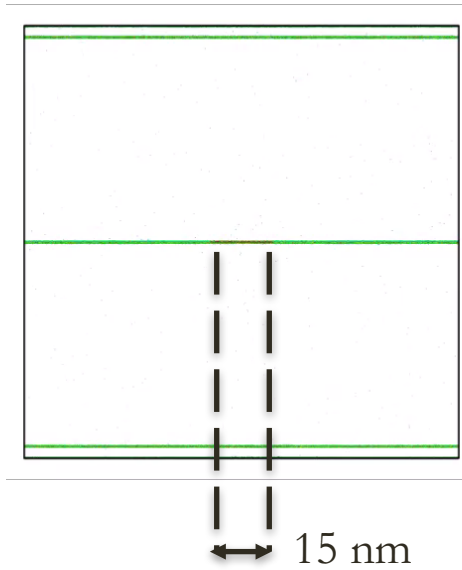
Step 5
Averaging to extract decohesion form



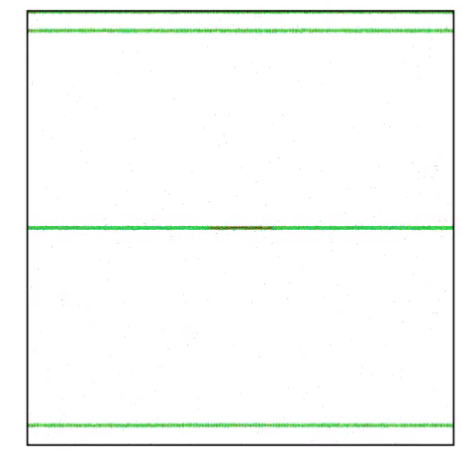
- Statistical mechanics rather than a deterministic approach

Mechanistically similar fracture behavior

Crack propagation:
 $\{213\}$ STGB + 0 H/nm²

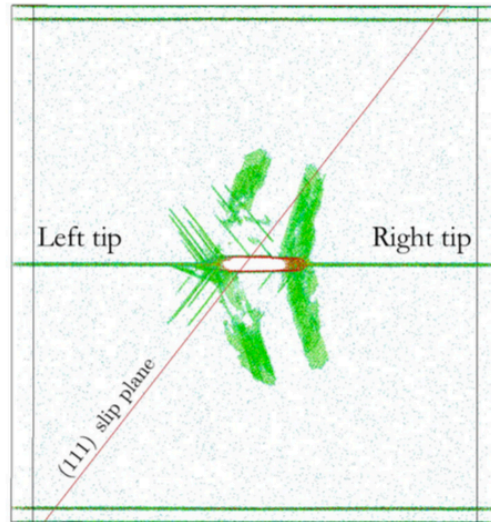


Crack propagation:
 $\{415\}$ STGB + 0 H/nm²

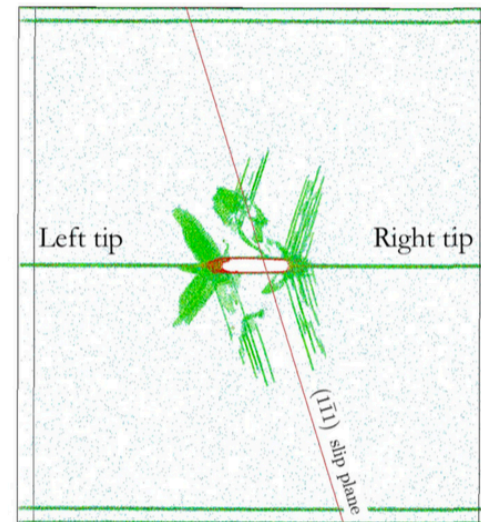


Plasticity similar for both $\{213\}$ and $\{415\}$ as generally expected from Schmid Factor

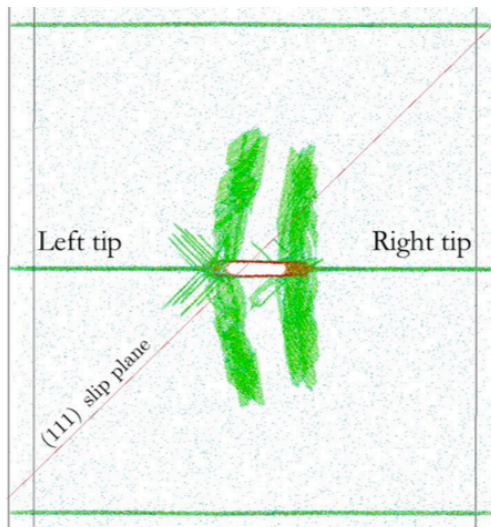
Mechanistically similar fracture behavior



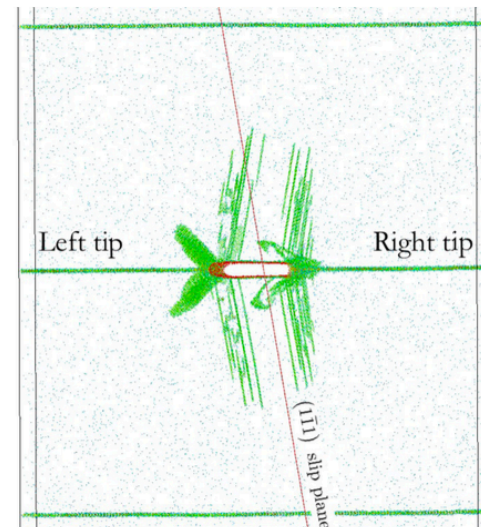
(a) $\{213\}$ grain boundary: (111) slip plane



(b) $\{213\}$ grain boundary: $(\bar{1}\bar{1}1)$ slip plane



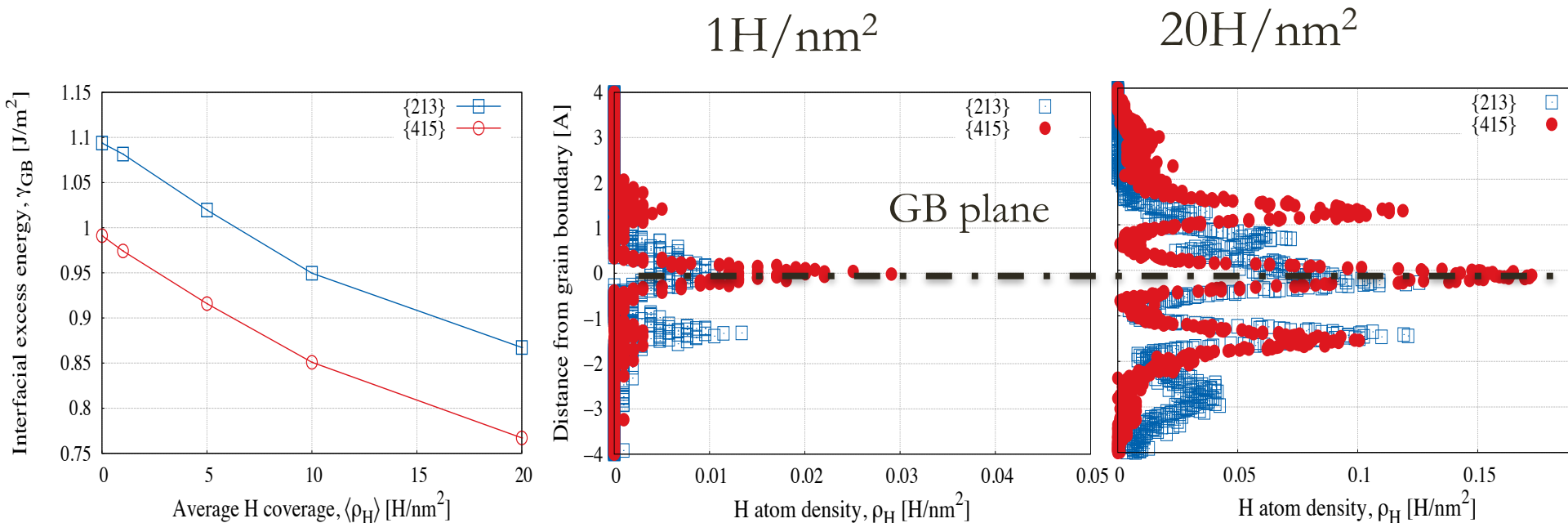
(c) $\{415\}$ grain boundary: (111) slip plane



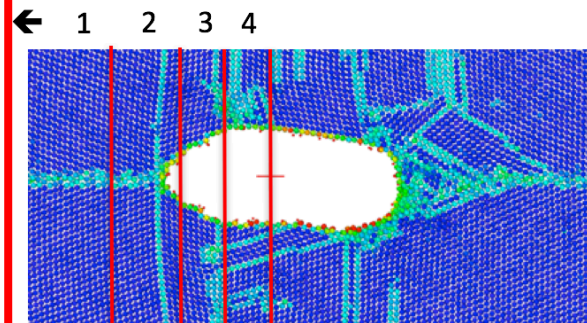
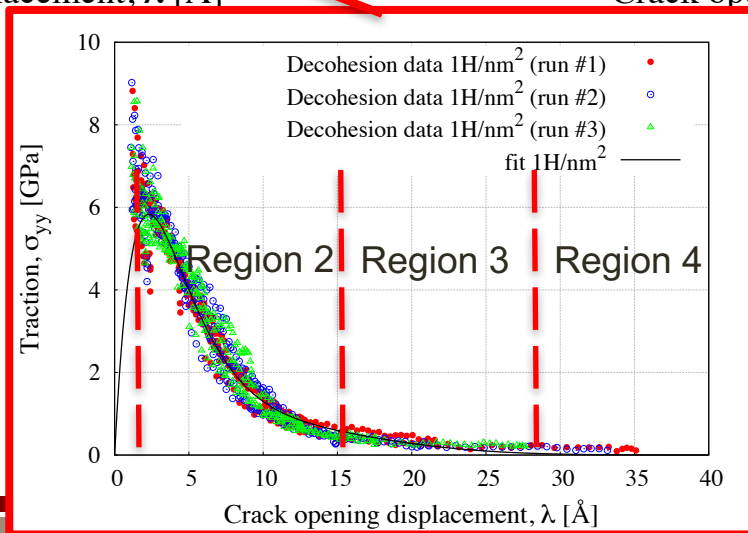
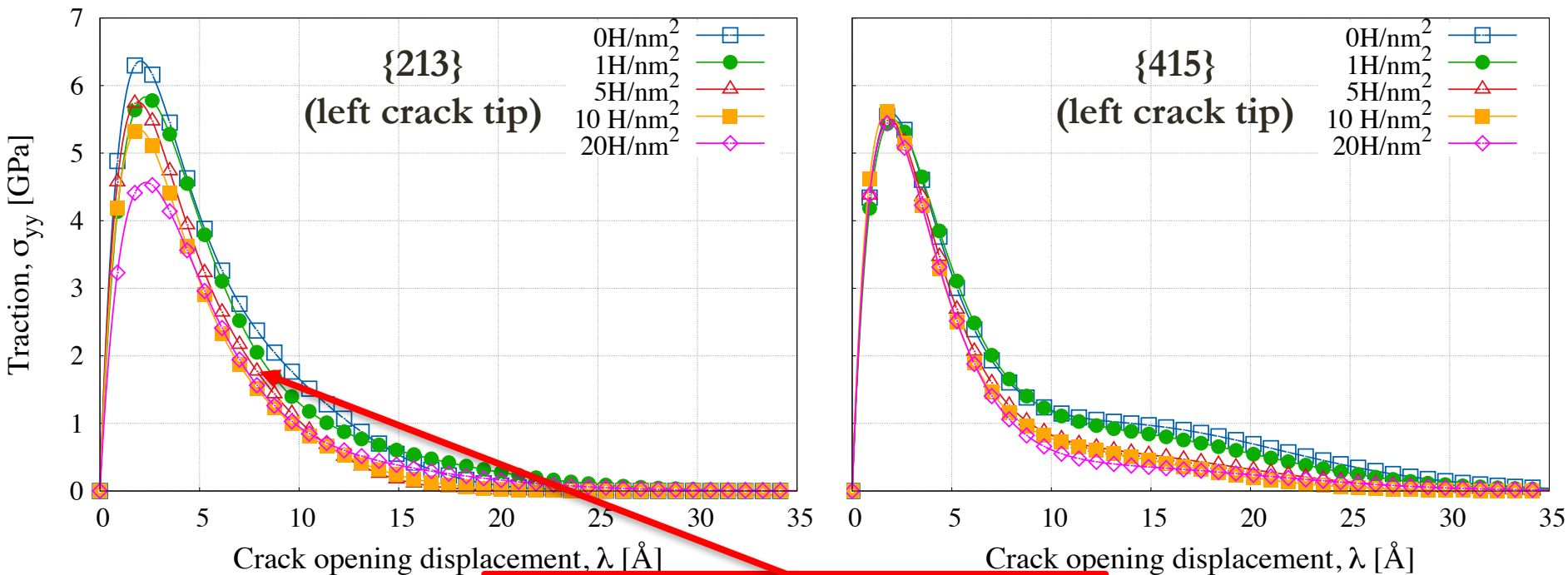
(d) $\{415\}$ grain boundary: $(\bar{1}\bar{1}1)$ slip plane

Using H segregation at GB as a surrogate for change in interfacial structure

$$\Gamma = \frac{1}{A} \left[\sum_{N_{\text{Ni}}} (E_{N_{\text{Ni}}} - E_{N_{\text{Ni}}}^{\text{bulk}}) + \sum_{N_{\text{H}}} (E_{N_{\text{H}}} - E_{N_{\text{H}}}^{\text{bulk}}) \right]$$

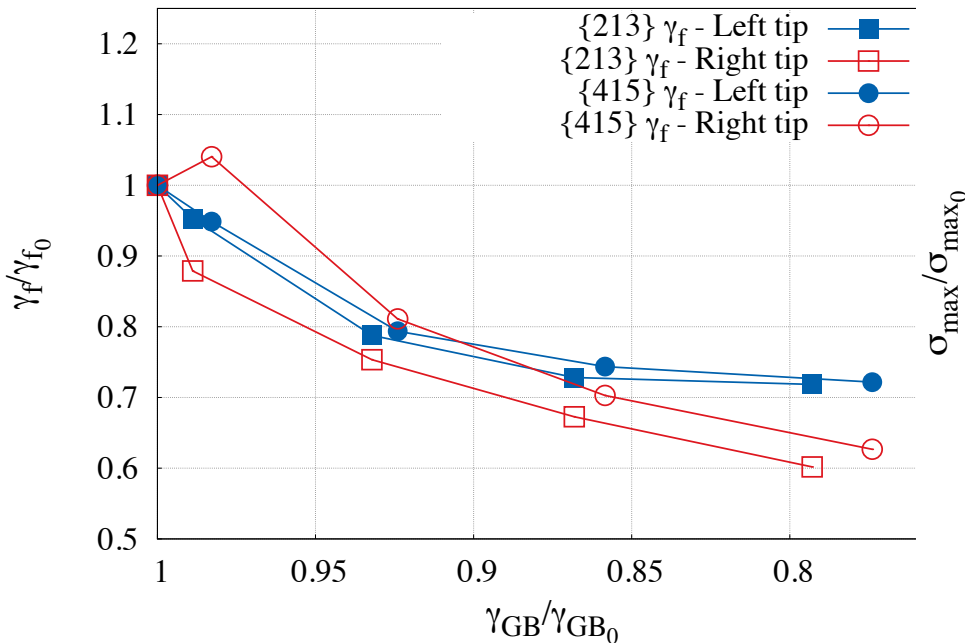


Isolating the role of the interface (1/2)

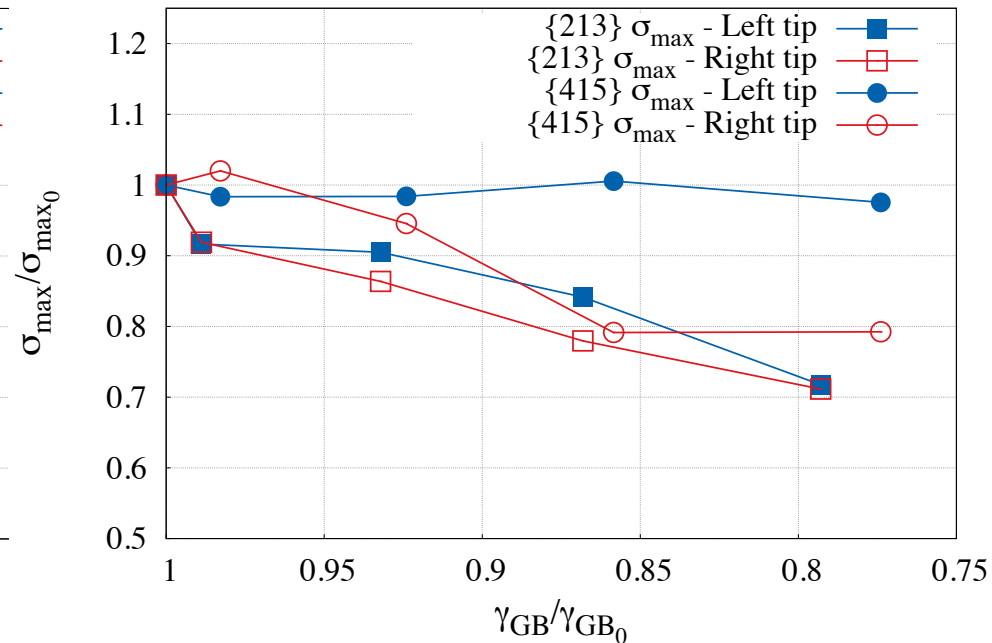


Isolating the role of the interface (2/2)

Fracture energy



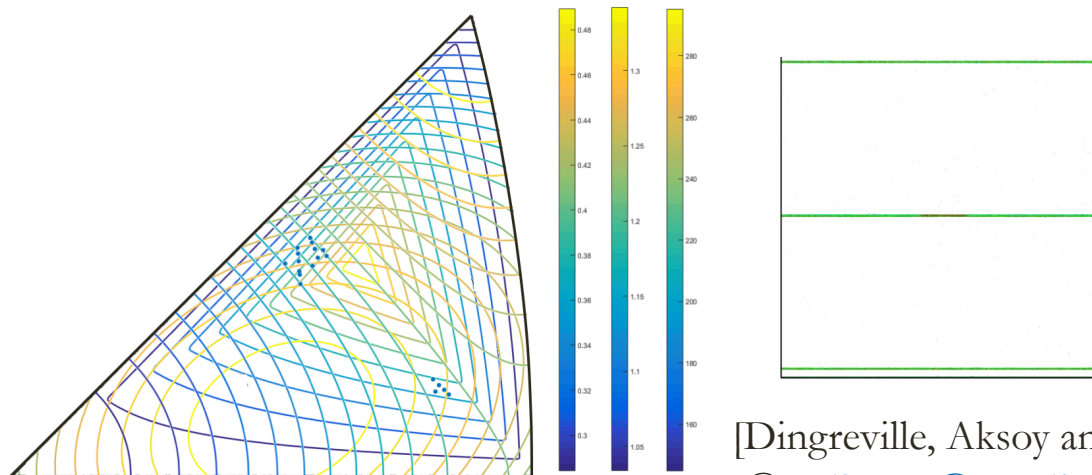
Peak stress



- In this example, structure of interface directly influence driving force for crack propagation!

Methodology to isolate role of GB structure

- Pathway for identifying general GB predisposition to resist fracture
 - Create sets of GBs using **isocurves associated with identical lattice properties** (E , μ^α , R_μ)
 - Enable identification of **structure-property relationships**
 - High-throughput simulations underway



[Dingreville, Aksoy and Spearot, in press Sci. Reports, 2017]
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