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Applications of Charge Optimized Many Body (COMB) Potentials in Multicomponent Systems

Tao Liang^{1,2}, Simon R. Phillpot¹ and Susan B. Sinnott^{1,2}

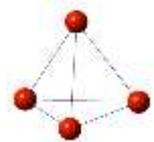
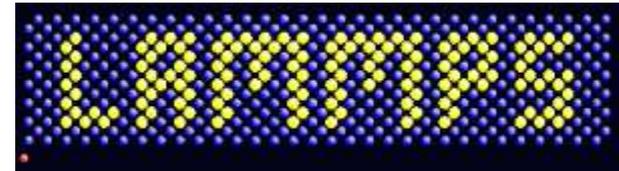
¹Department of Materials Science and Engineering, University of Florida

²Department of Materials Science and Engineering, Penn State University

Aug 6, 2015

August 2015 LAMMPS Users' Workshop and Symposium,
August 5-6, 2015 at Albuquerque, NM

tul17@psu.edu



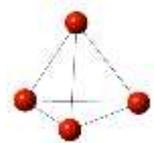
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Current COMB3 on LAMMPS is out dated
Contact me (TUL17@psu.edu) for updates



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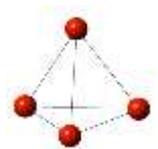
Reactive many-body empirical potentials to model materials



May 2012 issue

Historically developed for materials with specific types of chemical bonds

- SW and Tersoff potentials for Si
 - Brenner or REBO potential for C,H + O,F,S,.....
 - AIREBO
- EAM potentials for metals
 - MEAM for metals and oxides
 - EAM+ES for metals and oxides
- Buckingham potentials for ionically bound materials



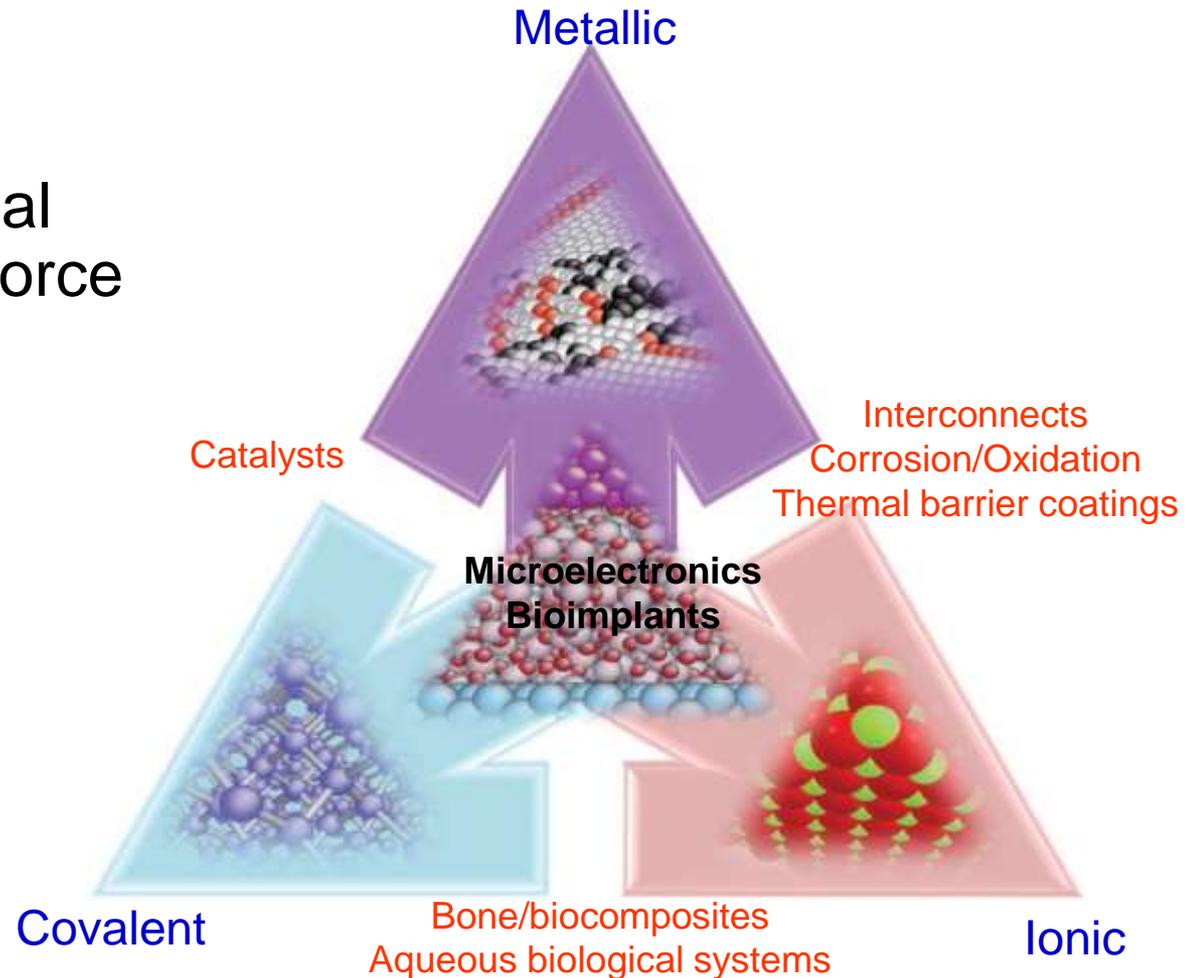
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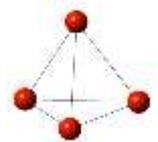
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Modeling Multicomponent Systems

- Inherent to many applications
- Challenge for traditional empirical potentials (force fields)
- This need spurred the development of *next generation potentials*: **charge optimized many body (COMB)**, ReaxFF, EAM+ES and a few others



S.R. Phillpot and S.B. Sinnott, *Science* (2009)



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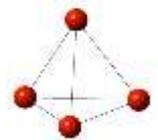
Functional form of COMB3 potential

$$E_T = \sum_i \left\{ \begin{aligned} & E_i^{Self}(q_i) + \frac{1}{2} \sum_{j \neq i} [V_{ij}^{short}(r_{ij}, q_i, q_j) + V_{ij}^{Coul}(r_{ij}, q_i, q_j)] \\ & + B_i(q_i) + C_i(r_{ij}, \theta_{ijk}) + E^{polar}(q_i, r_{ij}) + E^{vdW}(r_{ij}) \end{aligned} \right\}$$

- **Self energy**: ionization energies and electron affinities; includes penalty function to capture change in self-energy due to the field from the ionic lattice
- **Short-range interactions**: reactive bond-order potential
- **Coulomb interactions**: Coulomb integral over the charge densities
- **Charge and angular correction terms**
- **Polarization**: Atomic polarizability for organic systems
- **van der Waals energy**

S.R. Phillpot and S.B. Sinnott, *Science* (2009)

T. Liang et al., *Materials Science and Engineering R* (2013)



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Current status of COMB3

❖ Semiconductors

➤ Si

❖ Metals

➤ Cu, Zn, Al, Zr, Ti, U, Pt, Ni, Au

❖ Compounds

➤ Cu_2O , ZnO , UO_2 , NO_x , NH_3 , Al_2O_3 ,
 TiO_2 , NiO

➤ Ni_3Al , ZnCu

➤ TiN , AlN , TiC , TiH_2 , TiC

❖ Carbon based systems

➤ CHO systems

➤ H_2O and O_2

➤ C/H/Cu/O/Zn

➤ C/H/O/Ti

➤ CN

➤ CHON/Ti

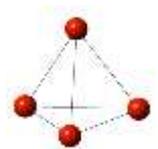
T. Liang et al., *Materials Science and Engineering R* (2013)

T. Liang et al., *J. Physical Chemistry A* (2011)

Yu-Ting Cheng et al., *Surface Science* (2013)

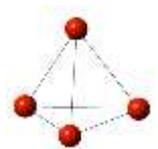
Yangzhong Li et al., *J. Physics: Condense Matter* (2012)

Mark J. Noordhoek et al., *J. Nuclear Materials* (2013)



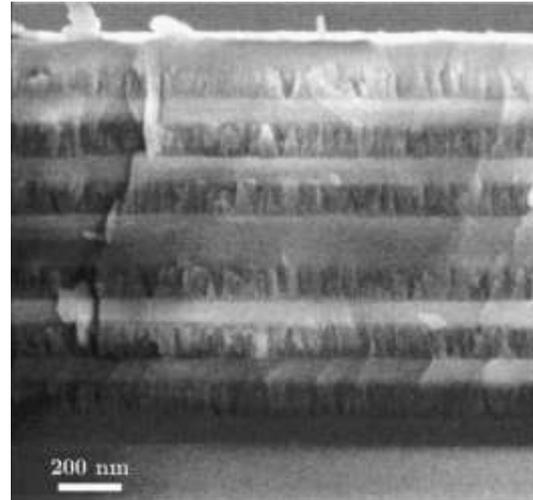
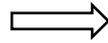
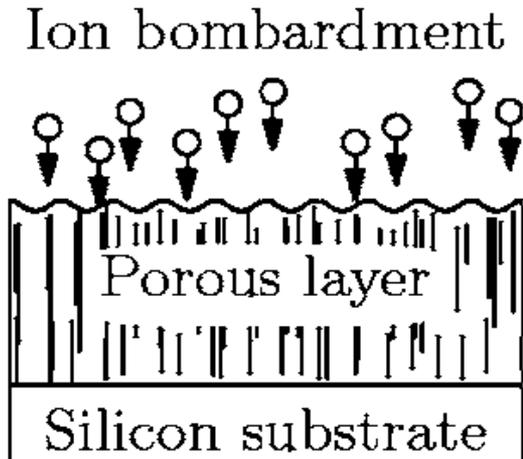
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- O₂ densification of porous titanium tetra-isopropoxide (TTIP) on TiO₂ surfaces
- Applications in electrochemical systems



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Motivation

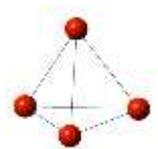


densification

Cross section of the treated $\text{SiN}_x\text{:H}$ filter film

- Plasma Enhanced Chemical vapor deposition (PECVD): surface treatment, thin film growth, ion densification ...
- $\text{Ti}(\text{OC}_3\text{H}_7)_4/\text{TiO}_2$ commonly used in optical devices
- Details of thin film growth mechanisms not well understood

Vernhes and et al, JAP, 99 (2006)

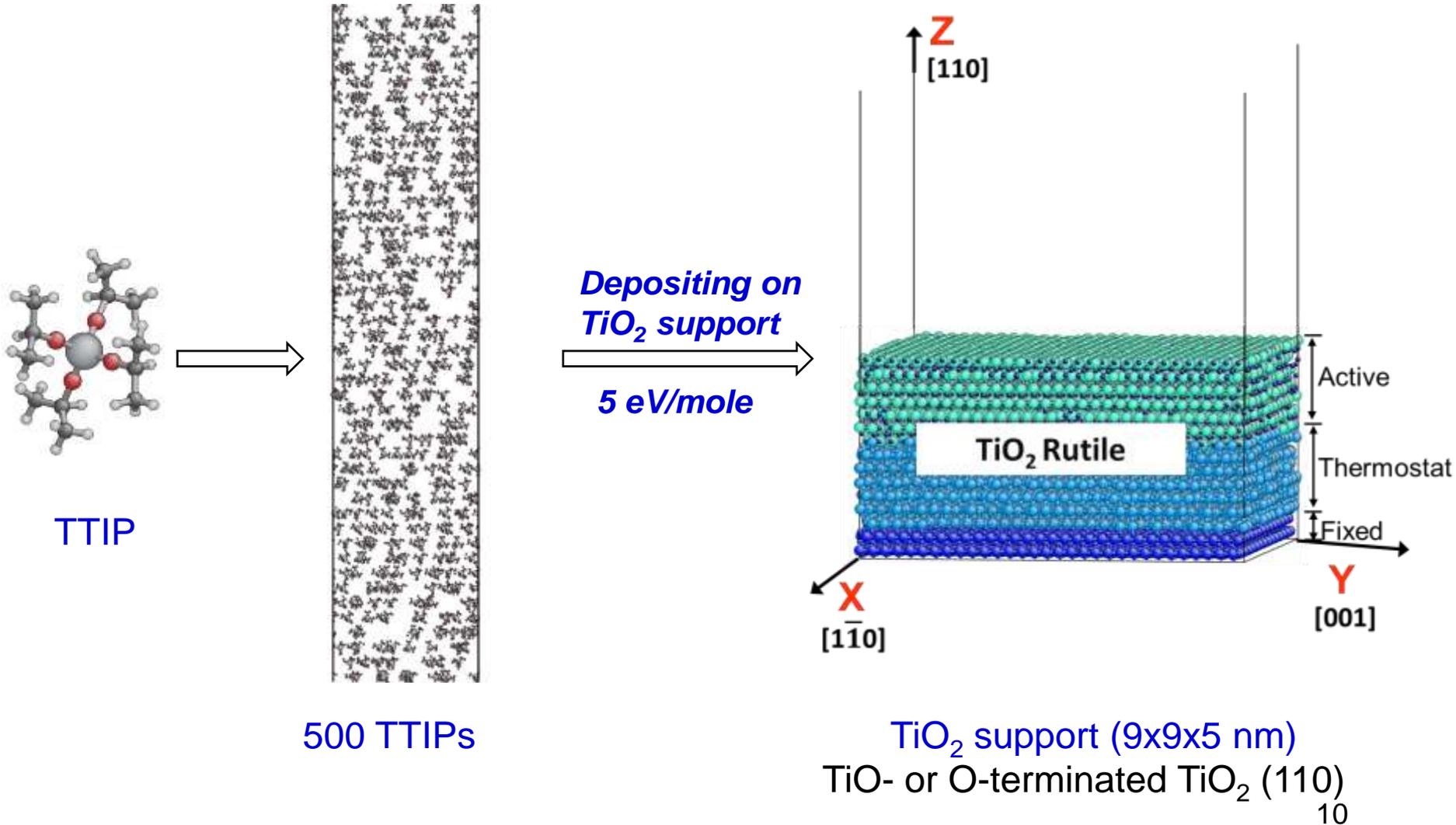


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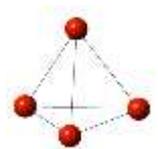
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Building Porous TTIP Layer on TiO₂ Support

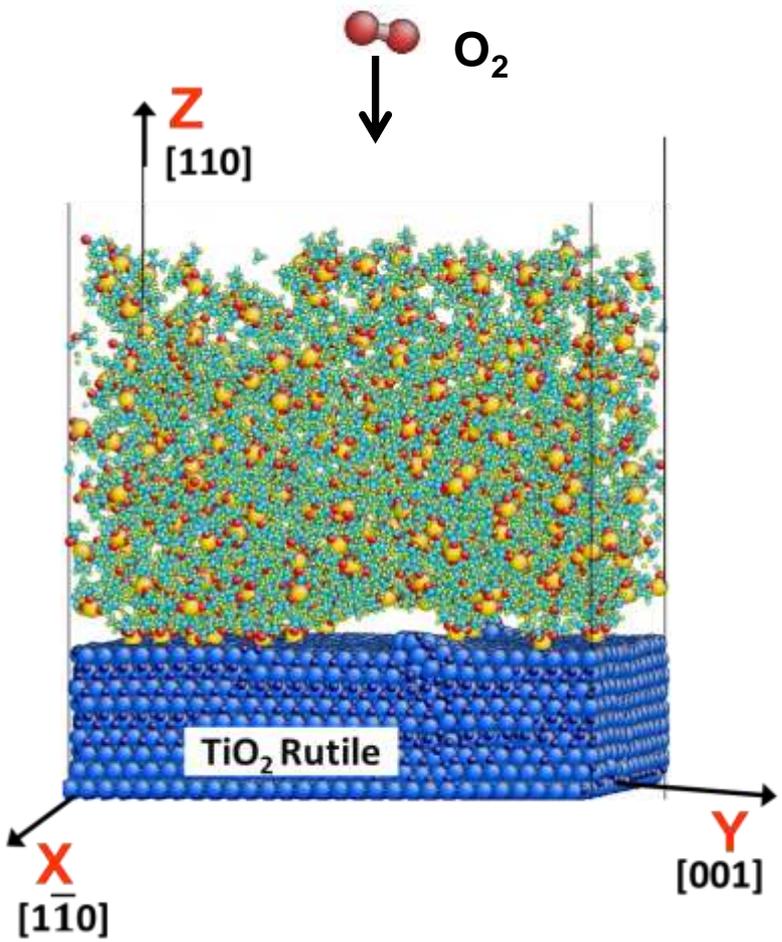


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System Configuration for Densification with O₂

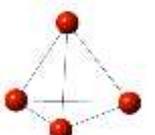


Densification settings:

- Incident energy 100 eV/O₂
- Every round has 400 O₂ molecules
- Performed 5 rounds of bombardment
- Ion/TTIP ratio: 4

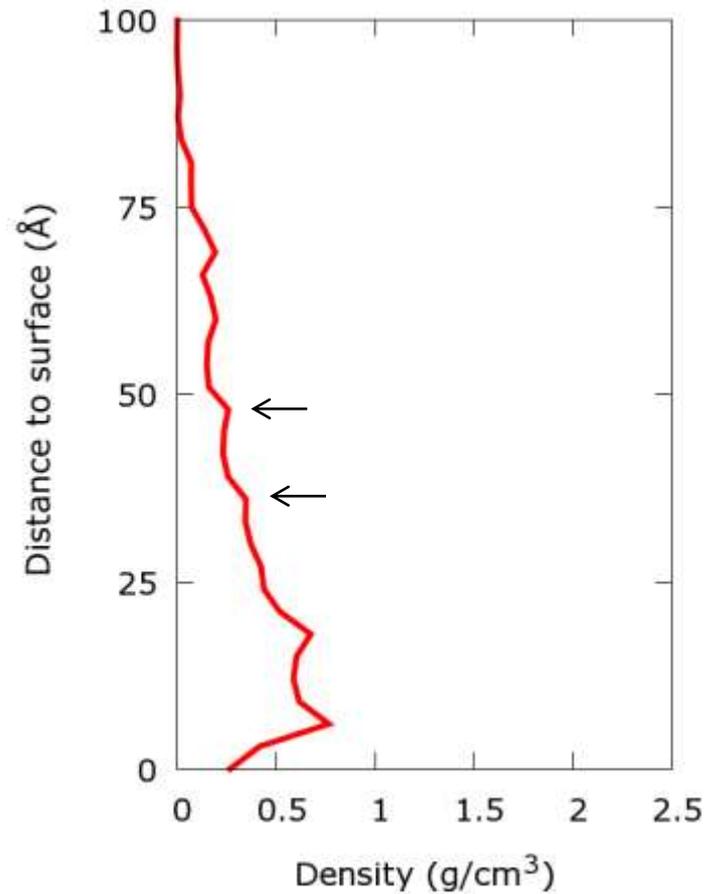
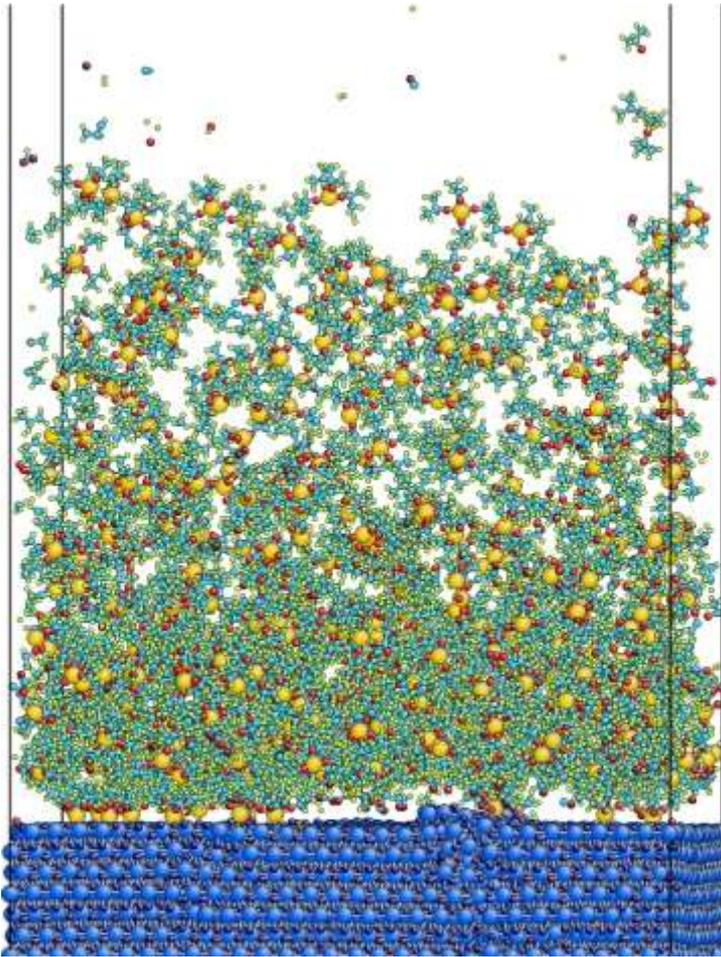
- Thermostat at 300 K
- Relaxation time between incident beams 0.5 ps
- Time step 0.2 fs

Porous TTIP layer with TiO₂ support



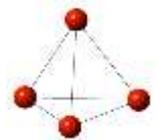
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TTIP Desorption



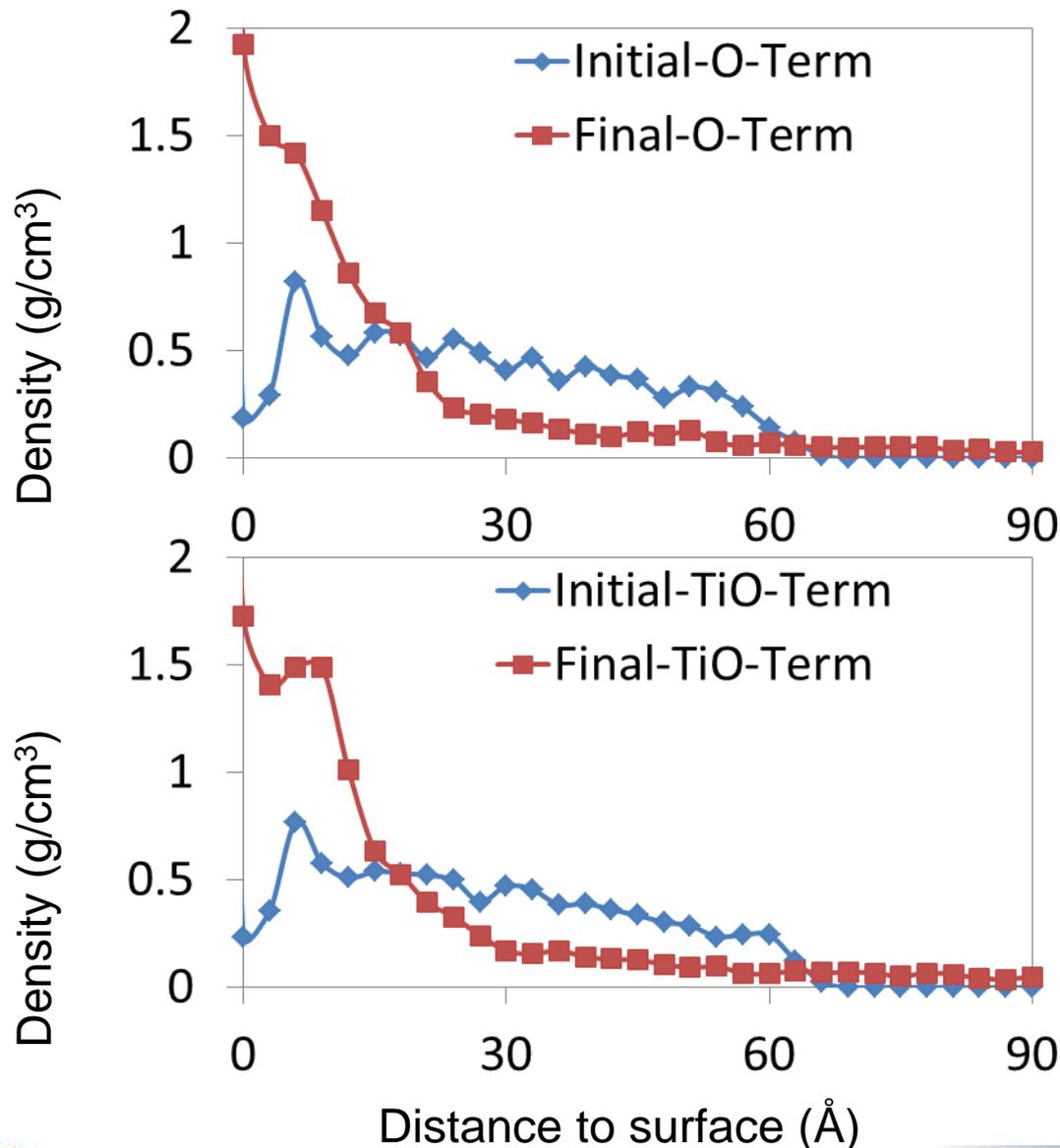
At early stage

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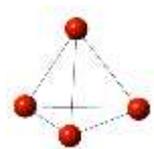


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Densification



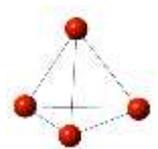
- Density increases more than two times near the surface region
- Densification only happens around 1.5 nm above the surface
- No TTIP stay as TTIP
- Wide range of molecular segments formed
- More than 200 water molecule form



➤ O₂ densification of porous titanium tetra-isopropoxide (TTIP) on TiO₂ surfaces

➤ Applications in electrochemical systems

- Recent change in O₂
- Reactive water potential with the variable charge
- Proton transfer
- Applying voltage in the variable charge potentials

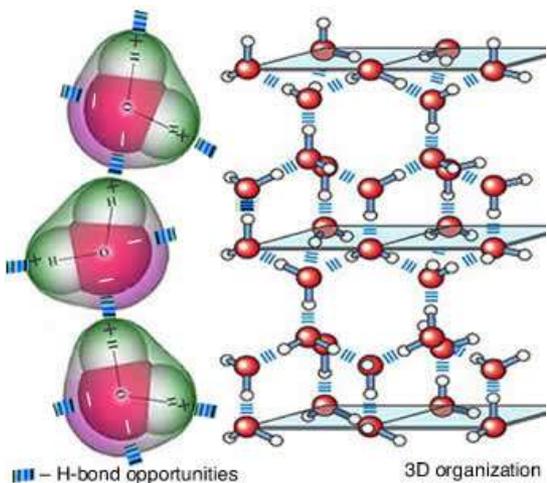


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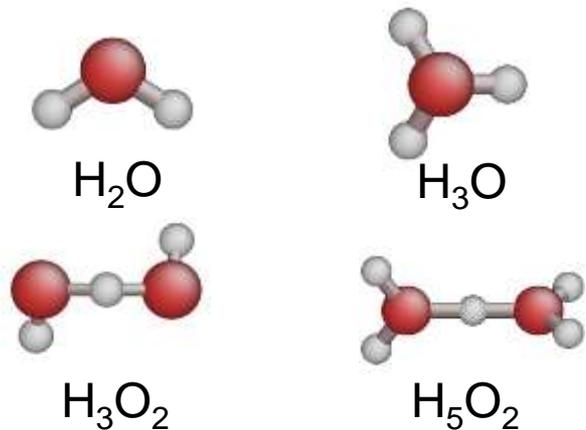
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Water Properties (within training database)



Properties	TIP4P	SPC/E	Exp.	COMB
H_2O				
ΔH_f (eV/mole.)			-2.50	-2.41
Charge on O, q_O (e)	-1.04	-0.82		-0.71
Dipole moment (eÅ)	0.62	0.49	0.39	0.42
Ice I_h				
a (Å)			4.52 ^a	4.55
c (Å)			7.36 ^a	7.39
O-O distance (Å)			2.76 ^b	2.78
ΔH_f (eV/mole.)			-3.02 ^c	-3.16
Charge on O, q_O (e)	-1.04	-0.82		-0.87
Dipole moment (eÅ)	0.62	0.49	0.52 ^d , 0.64 ^e	0.53



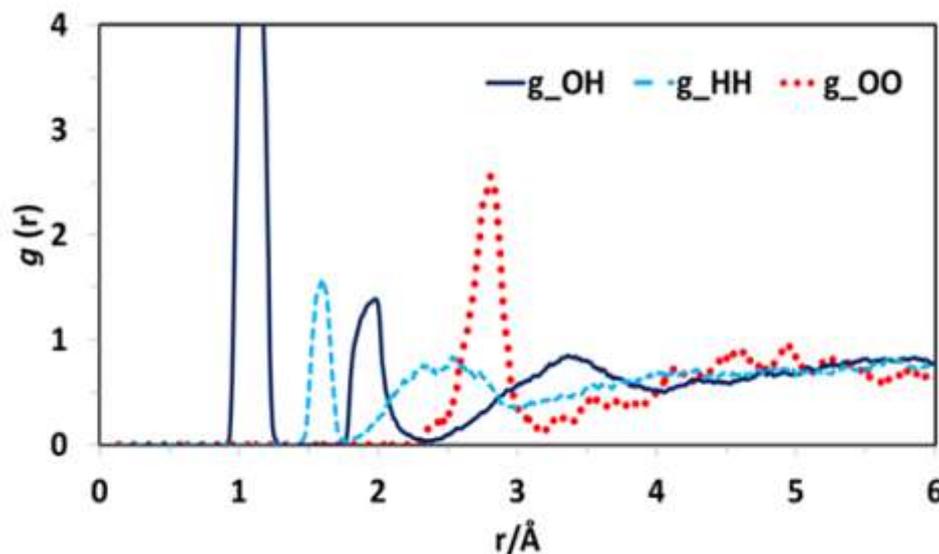
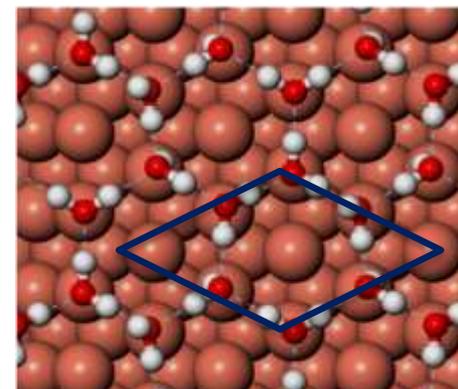
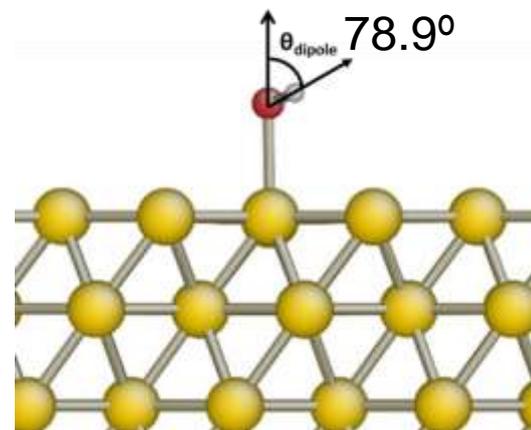
Structures	Exp. or DFT	COMB
H_2O	-2.41	-2.41
HO	0.38	0.31
H_2O_2	-1.34	-1.72
H_3O	1.25	1.25
H_3O_2 (HO- H_2O)	-1.80	-1.80
H_5O_2 (H bridge 2 H_2O)	-1.45	3.40

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Predicted water properties

Selected properties of water

	TIP4P	SPC/E	Exp	COMB
ΔH_f (eV/unit)			-2.96	-2.81
ΔH^{sol} (eV/unit)			-0.46	-0.40
Density (g/cm ³)	0.99	1.02	1.00	1.00
Dipole (eÅ)	0.45	0.49	0.6	0.45
Diffusion Coeff. (10 ⁻⁵ cm ² /s)	3.9	2.52	2.30	0.96



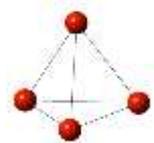
	DFT+vdW	COMB3
H ₂ O _{atop}	-0.40	-0.49
H ₂ O _{fcc/hcp}	-0.28	-0.54
H ₂ O _{dimer}	-0.55	-0.59
H ₂ O _{hexamer}	-0.73	-0.91

Pair distribution of water

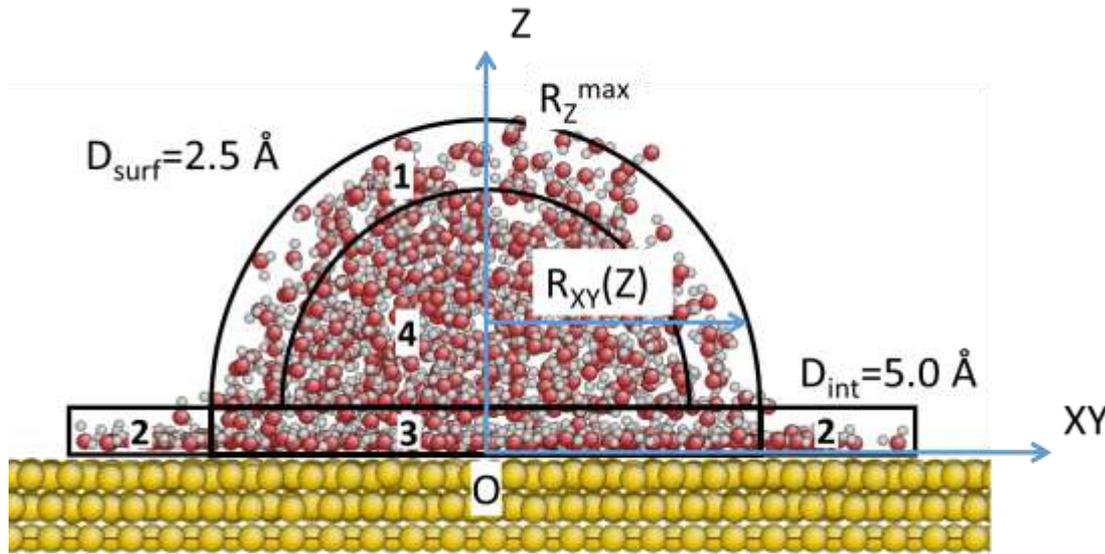
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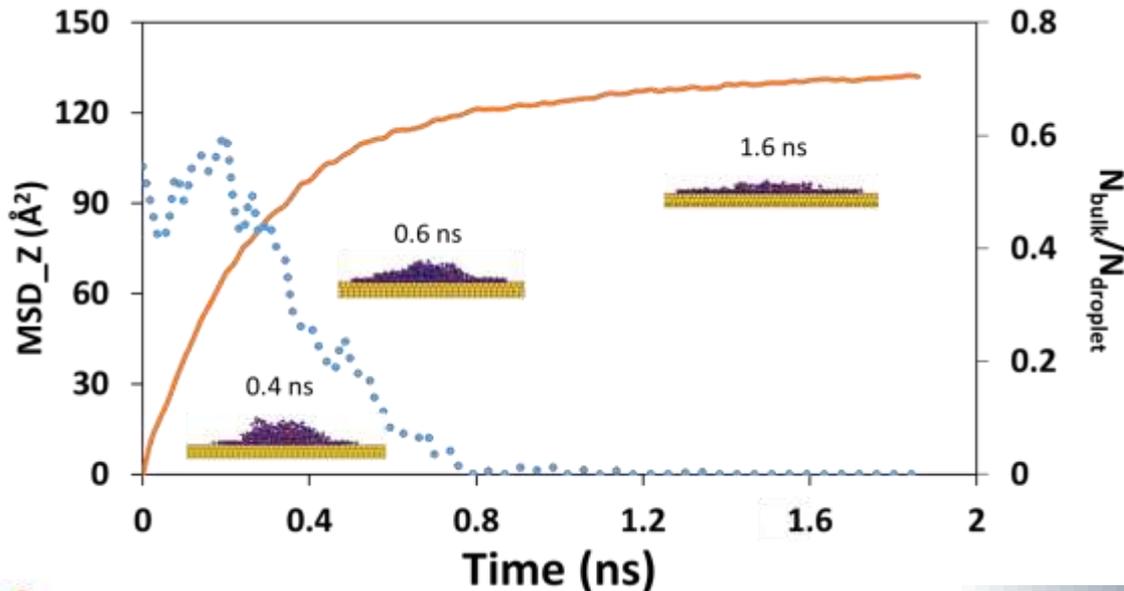
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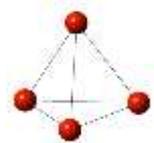
Wetting Mechanism



1. Surface water
2. Precursor water
3. Interfacial water
4. Bulk water

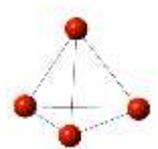
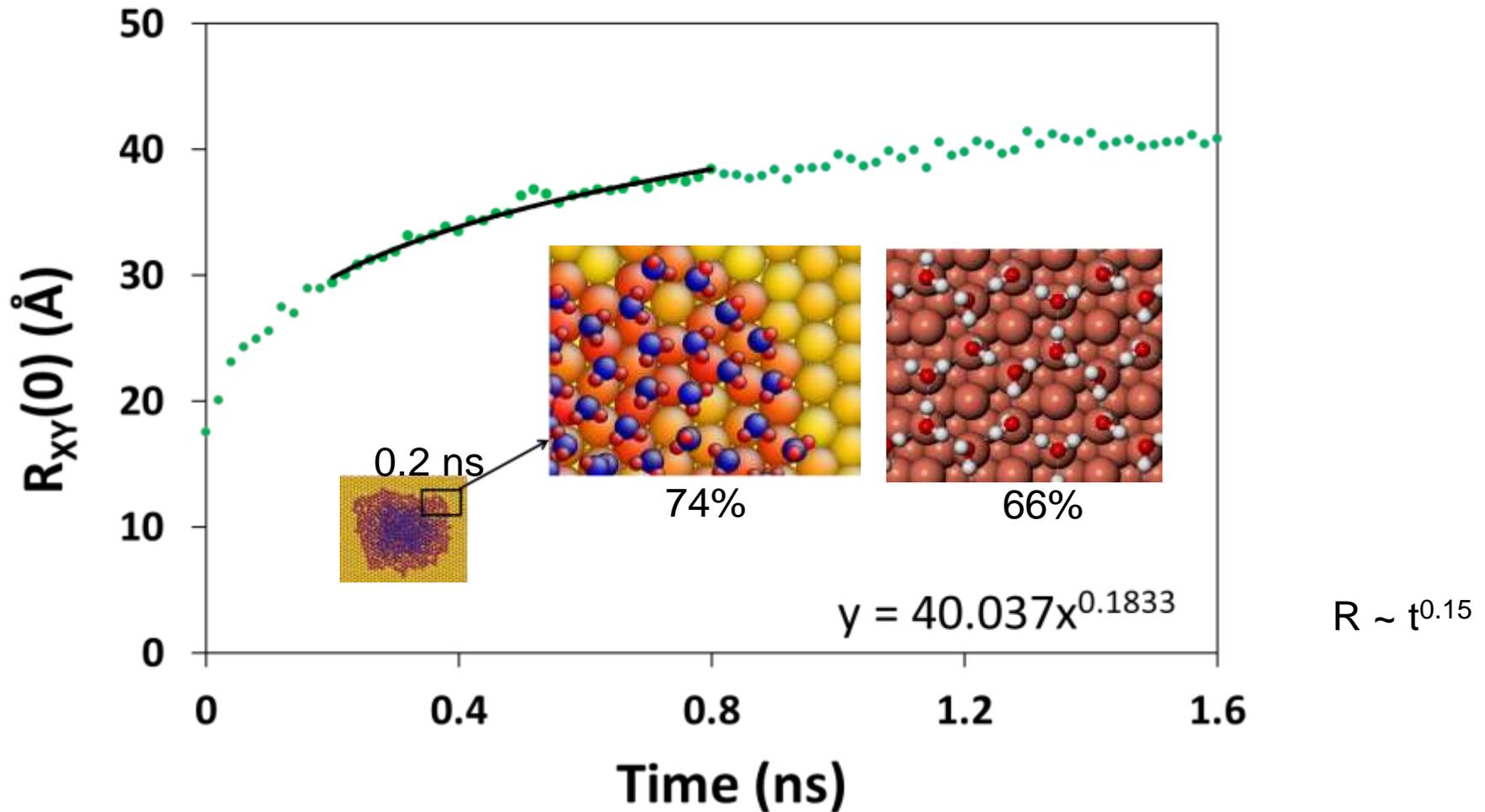


No bulk water after 0.8 ns



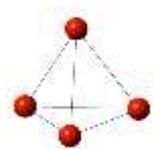
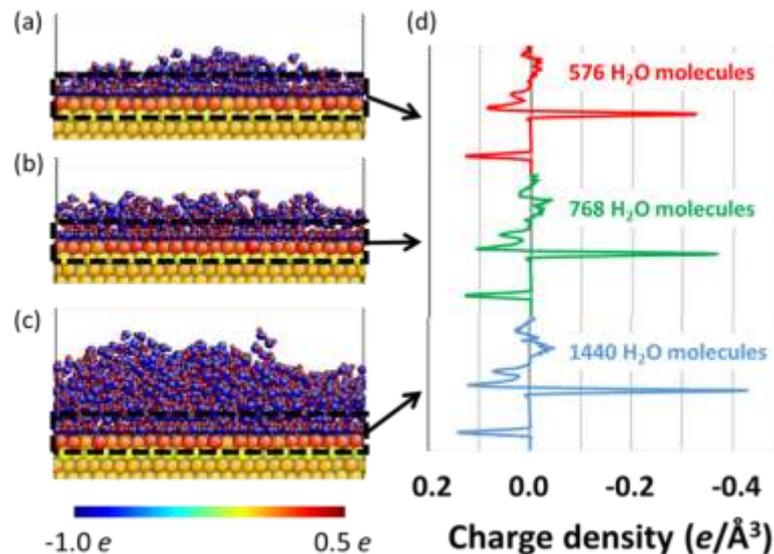
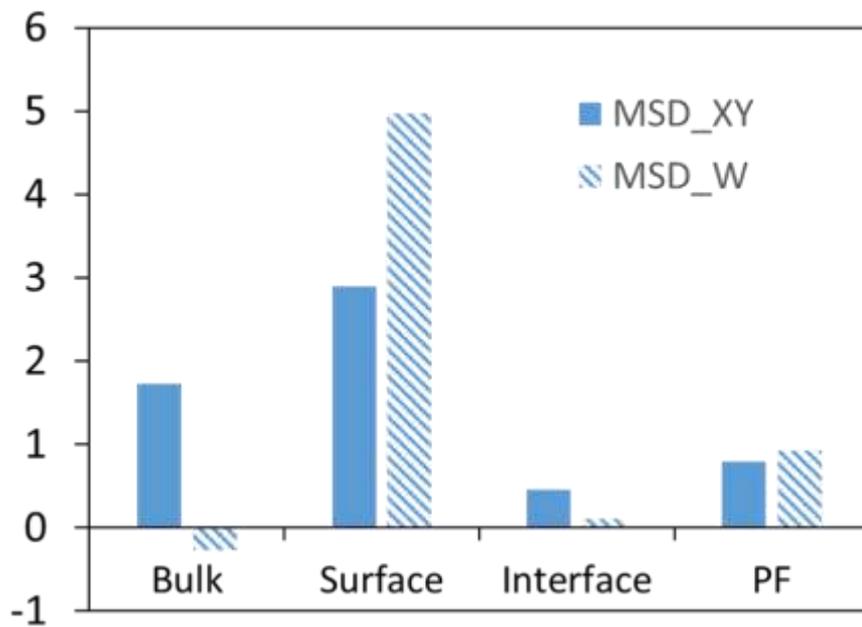
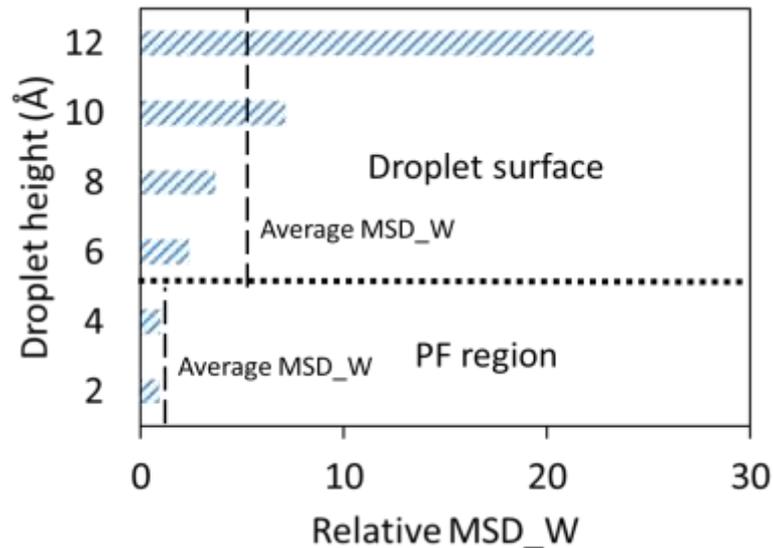
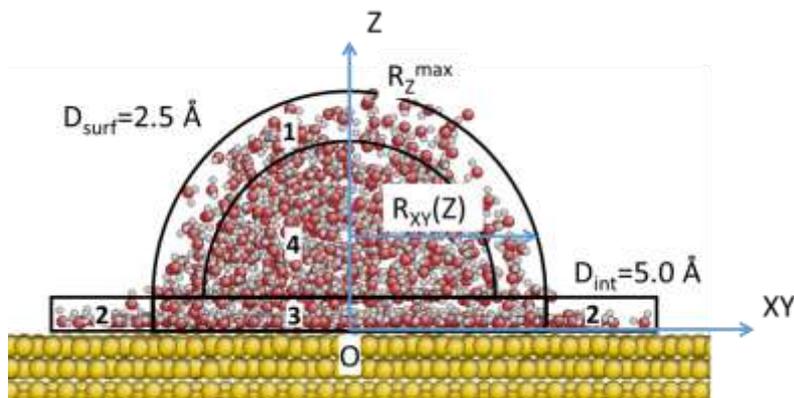
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Wetting Mechanism



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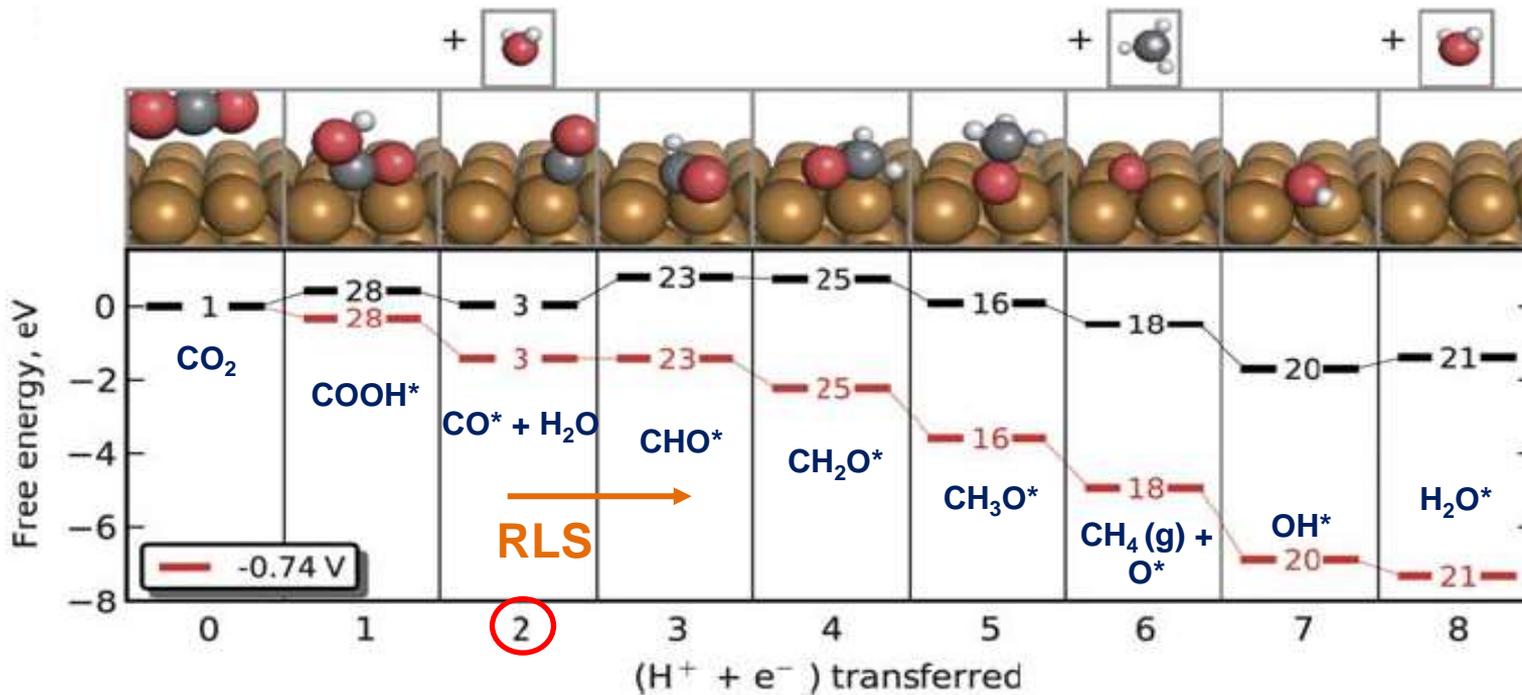
Wetting Mechanism



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Reaction Energies ΔG of Steps in Electrochemical Reactions

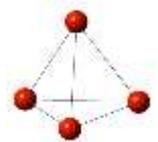
20



$$\Delta G_{\text{CO}^*}(U) = G_{\text{CO}^*} - G_* - G_{\text{CO}_2(\text{g})} + G_{\text{H}_2\text{O}(\text{aq})} - G_{\text{H}_2(\text{g})} + 2 \text{e}U$$

Kinetics dictate the activity and selectivity with the CO₂ ER pathway

Peterson, Andrew A., et al. *Energy Environ. Sci.* 3.9 (2010): 1311-1315

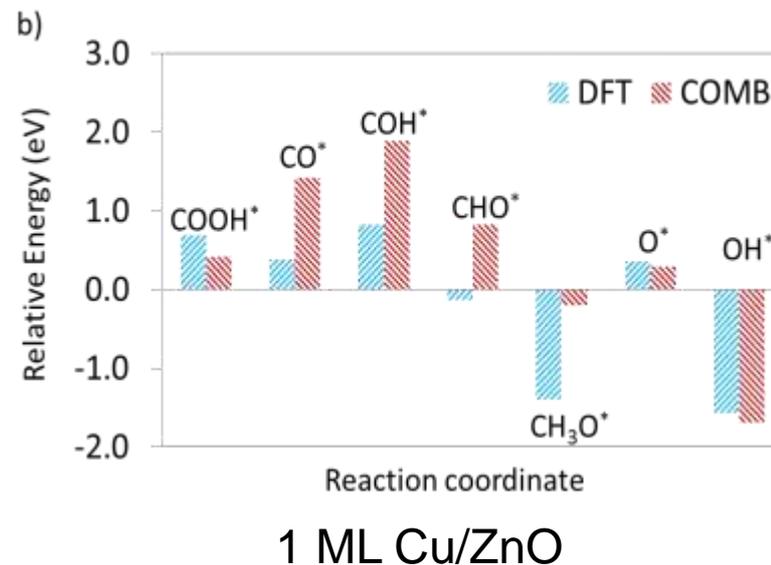
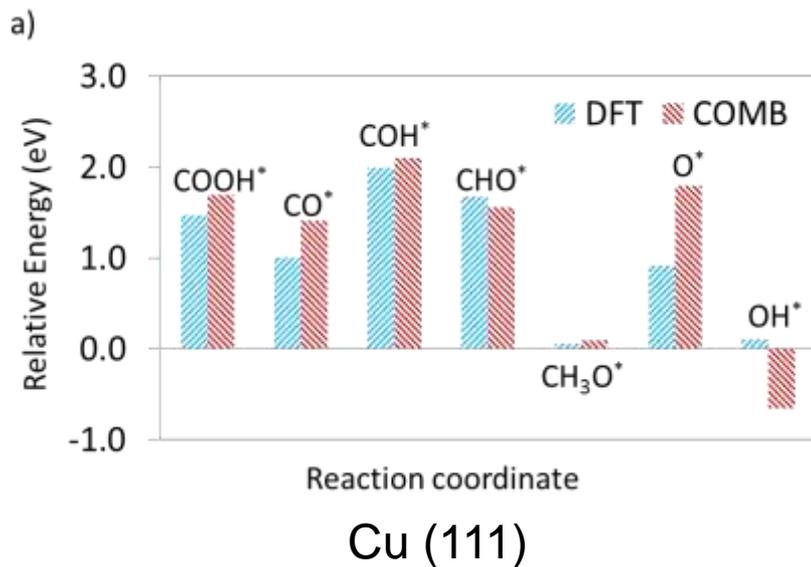


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Florida Laboratory for Advanced Materials Engineering Simulation

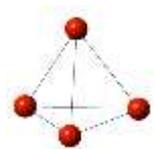
CO₂ Reduction on Cu and 1ML Cu/ZnO



The calculated reaction energies with added entropic terms at 0V vs. RHE

Reaction	Surface	DFT (eV)	COMB (eV)
$\text{CO}^* + \text{H}^+ + \text{e}^- \rightarrow \text{COH}^*$	Cu (111)	1.31	1.02
	1ML Cu/ZnO	0.83	0.85
$\text{CO}^* + \text{H}^+ + \text{e}^- \rightarrow \text{CHO}^*$	Cu (111)	0.96	0.44
	1ML Cu/ZnO	-0.14	-0.22

T. Liang and etal, CAT. Comm., 52 (2014)



Applying Potential in COMB3

At ES equilibrium:

- Electronegativity ($\partial U / \partial q$) is equal at all sites

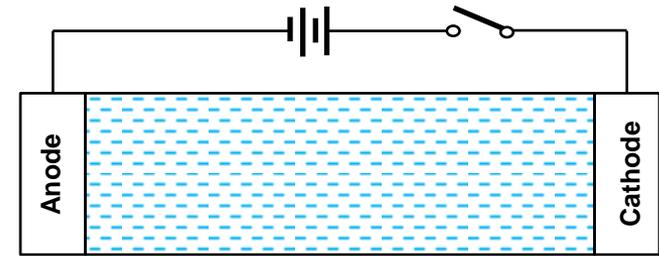
$$\chi_i = \frac{\partial U}{\partial q_i}$$

$$\bar{\chi} = \frac{1}{N} \sum_i \chi_i$$

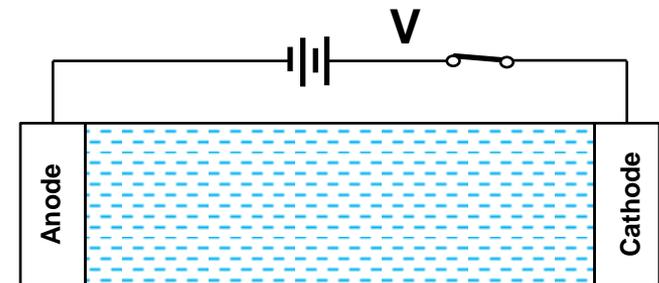
At ES non-equilibrium:

- Electronegativity is biased by V

$$\frac{\partial U_{cathode}}{\partial q_i} - \frac{\partial U_{anode}}{\partial q_i} = V$$



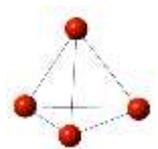
$$\text{EOM} \quad m_q \ddot{q}_i = \bar{\chi} - \chi_i + \nu \dot{q}_i$$



$$\text{E: } m_q \ddot{q}_i = \bar{\chi} - \chi_i + \nu \dot{q}_i$$

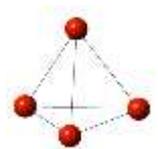
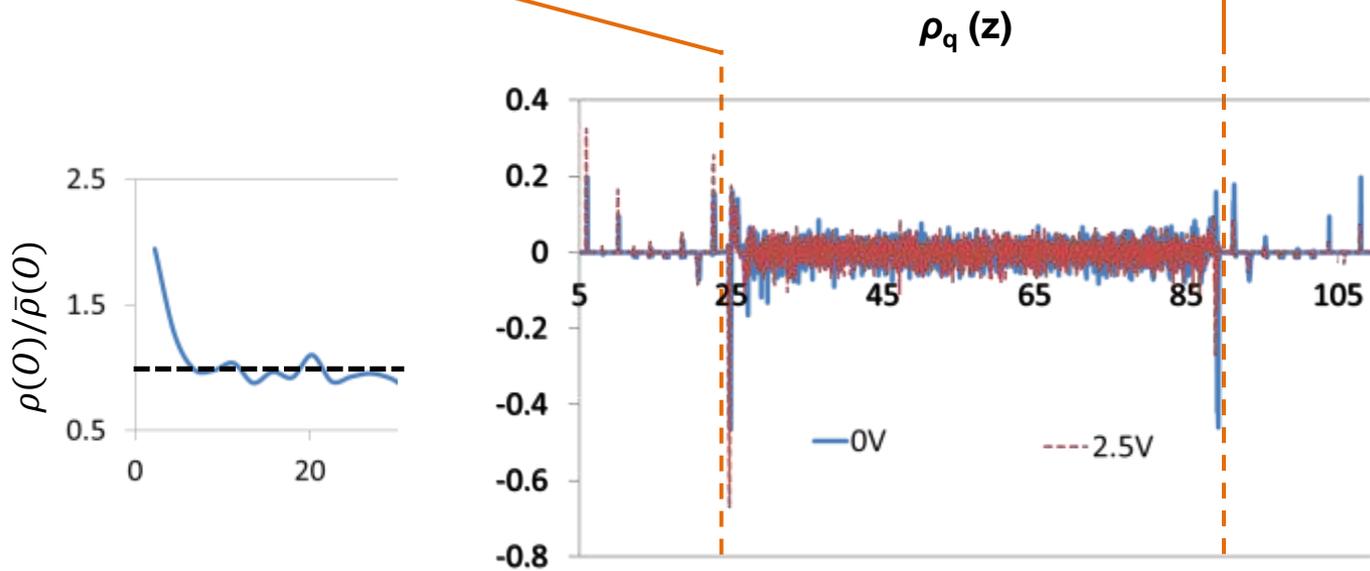
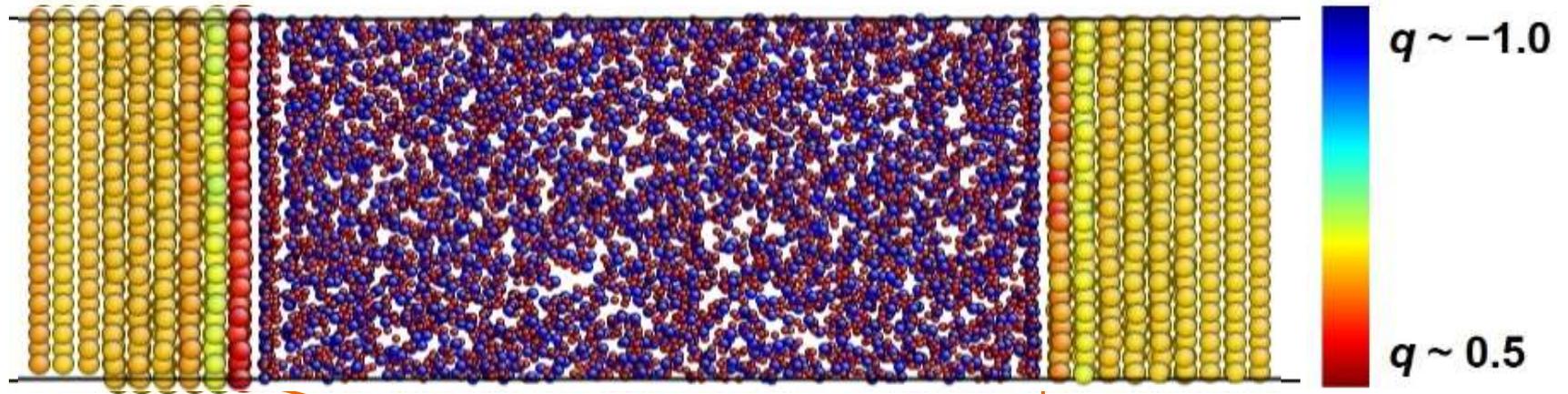
$$\text{C: } m_q \ddot{q}_i = \bar{\chi} + \frac{N_c}{N_A + N_C} V - \chi_i + \nu \dot{q}_i$$

$$\text{A: } m_q \ddot{q}_i = \bar{\chi} - \frac{N_A}{N_A + N_C} V - \chi_i + \nu \dot{q}_i$$



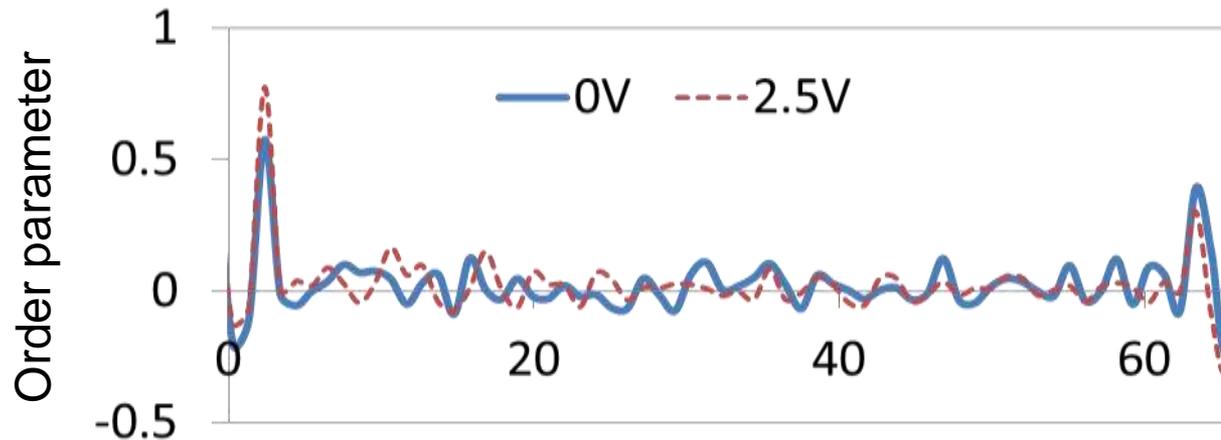
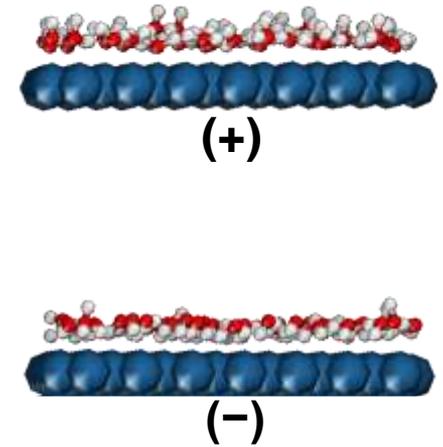
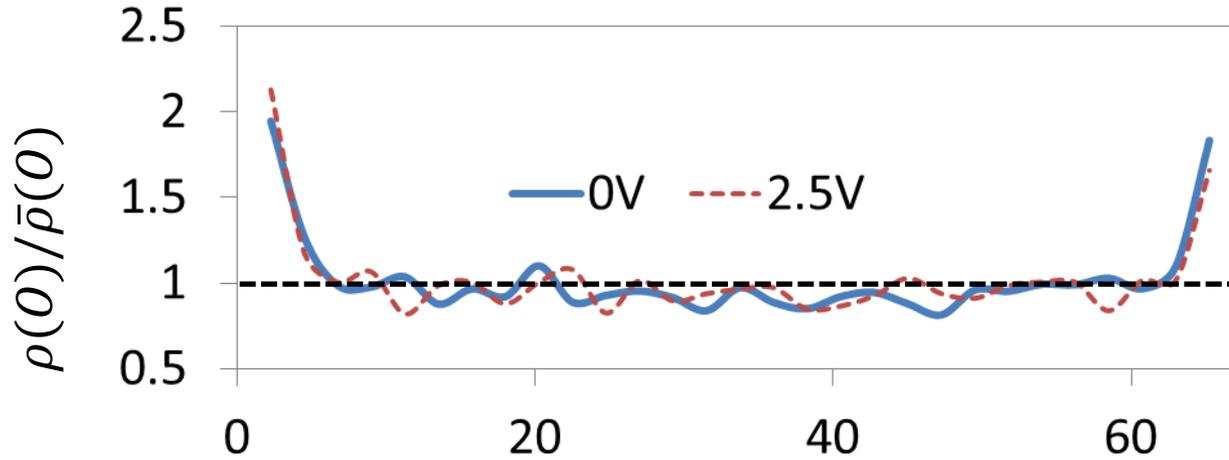
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E-COMB Results



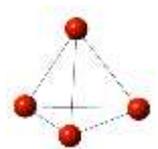
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E-COMB Results



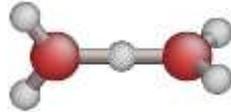
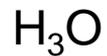
$$P(z) = \left\langle \frac{1}{N(z)} \sum_{i=1}^N \frac{(3\hat{\mu}_{z,i}^2 - 1)}{2} \right\rangle$$

Order parameter

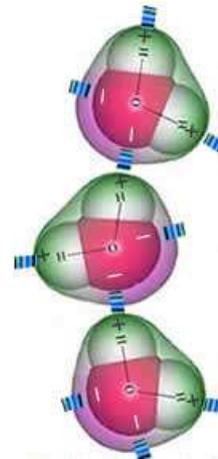


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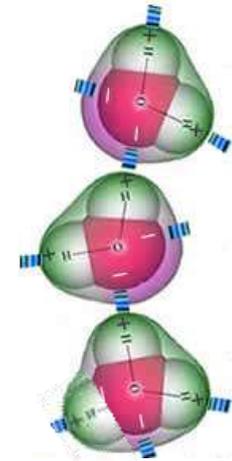
Proton transfer



OH distance = 1.2 Å



OH distance = 0.96 Å
Hydrogen bond = 1.78 Å

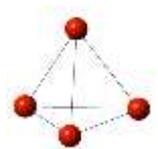


Proton transfer

Barrier ~ 0.2 eV
COMB ~ 1.5 eV

Ongoing applications

- CDC materials
- Electrochemical simulations with applied potentials
- TiC_2 , Ti_2C_3 2D MXene materials
- Proton transfer in electrochemical systems and MXene materials



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