

# Application of Third-Generation Charge-Optimized Many-Body Potentials (COMB3) in LAMMPS

Tao Liang, Tzu-Ray Shan, Dundar Yilmaz, Simon R. Phillpot, and Susan B. Sinnott

*University of Florida  
Sandia National Lab*

**August 7, 2013**

**Supported by: NSF-DMR, DOE-EFRC, NSF-CHE, DOE-CASL**

**LAMMPS Users' Workshop and Symposium  
August 7 - 8, 2013, Albuquerque, NM**

Liang75@ufl.edu

# Reactive many-body empirical potentials in materials science



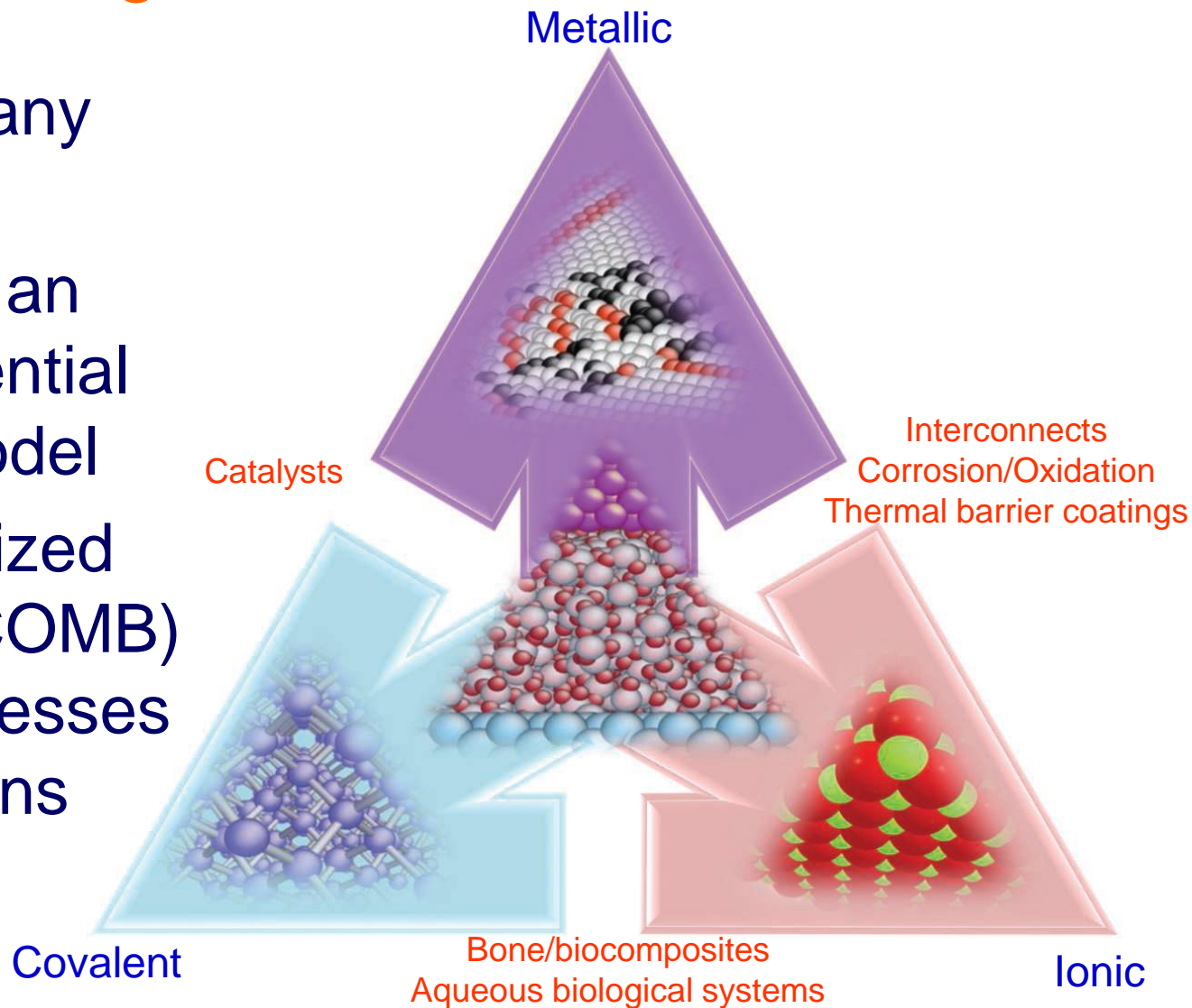
**May 2012 issue**

**Historically developed for materials with specific types of chemical bonds**

- Tersoff potentials for Si
  - Brenner or REBO potential for C,H + O,F,S,.....
  - AIREBO
- EAM potentials for metals
  - MEAM for metals and oxides
  - EAM+ES for metals and oxides
- Buckingham potentials for ionically bound materials

# Modeling heterogeneous interfaces

- Inherent to many applications
- Challenge for an empirical potential function to model
- Charge optimized many body (COMB) potential addresses these limitations



S. R. Phillpot, S. B. Sinnott, *Science* 325, 1634 (2009).

# Functional form of COMB3 potential

$$E_T = \sum_i \left\{ \begin{aligned} &E_i^{Self}(q_i) + \frac{1}{2} \sum_{j \neq i} [V_{ij}^{short}(r_{ij}, q_i, q_j) + V_{ij}^{Coul}(r_{ij}, q_i, q_j)] \\ &+ B_i(q_i) + C_i(r_{ij}, \theta_{ijk}) + E^{polar}(q_i, r_{ij}) + E^{vdW}(r_{ij}) \end{aligned} \right\}$$

- Self energy: ionization energies and electron affinities; includes penalty function to capture change in self-energy due to the field from the ionic lattice
- Short-range interactions: bond-order REBO potential
- Coulomb interactions: Streit & Mintmire QeQ scheme
- Angular correction terms
- Polarization: Atomic polarizability for organic systems
- van der Waals energy: Lennard Jones

S.R. Phillpot and S.B. Sinnott, *Science* (2009)

T. Liang et al., *Materials Science and Engineering R* (2013)

# Dynamic Variable Charge

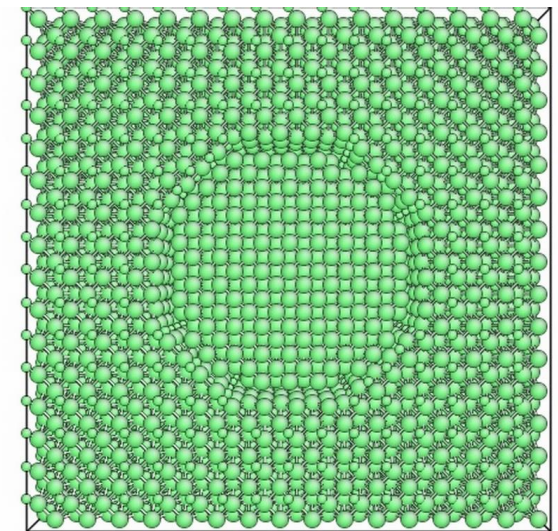
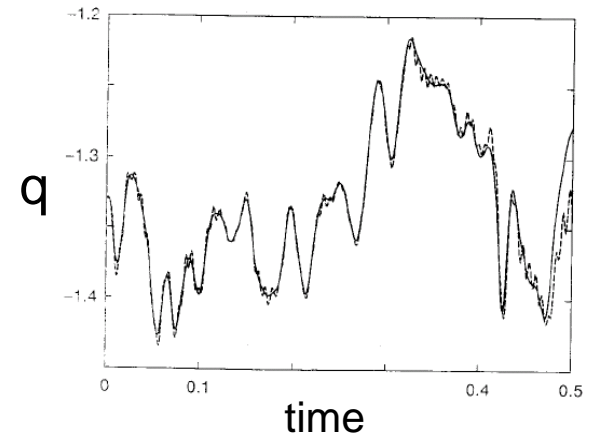
- The electronegativity ( $-\partial E/\partial q$ ) is equal at all sites

$$L = \sum_{i=1}^N \frac{1}{2} m \dot{r}_i^2 + \sum_{i=1}^N \frac{1}{2} m_q \dot{q}_i^2 - U(r, q) - \lambda \sum_{i=1}^N q_i$$

Extended Lagrangian  
Dynamics:

$$m_i \ddot{\vec{r}} = -\vec{\nabla}_i V$$

$$\mu_i \ddot{q}_i = -\frac{\partial V}{\partial q_i}$$



Cu<sub>2</sub>O with a Cu core

- Avoids matrix inversion or optimization
- Low computational cost
- requires smaller time step
- Damped dynamics

$$-m_q \ddot{q}_i = \mu_{T_i} - \bar{\mu}_T + \eta_D \dot{q}_i$$

Rick & Stuart *Rev Comp Chem* 18, 89 (2002)

A. K. Rappe, W. A. Goddard, *J Phys Chem* 95, 3358 (1991)

J. Yu, S. Sinnott, S. Phillpot *Phys. Rev. B* 75 085311 (2007)

# Cost of Potentials in LAMMPS

| Potential        | System                       | # Atoms                  | Memory        | LJ Ratio             |
|------------------|------------------------------|--------------------------|---------------|----------------------|
| Lennard-Jones    | LJ liquid                    | 32000                    | 12 Mb         | 1.0x                 |
| <b>EAM</b>       | <b>bulk Cu</b>               | <b>32000</b>             | <b>13 Mb</b>  | <b>2.4x</b>          |
| <b>Tersoff</b>   | <b>bulk Si</b>               | <b>32000</b>             | <b>9.2 Mb</b> | <b>4.1x</b>          |
| Stillinger-Weber | bulk Si                      | 32000                    | 11 Mb         | 4.1x                 |
| EIM              | crystalline NaCl             | 32000                    | 14 Mb         | 6.5x                 |
| CHARMM + PPPM    | solvated protein             | 32000                    | 124 Mb        | 13.6x                |
| MEAM             | bulk Ni                      | 32000                    | 54 Mb         | 15.6x                |
| AIREBO           | polyethylene                 | 32640                    | 101 Mb        | 54.7x                |
| ReaxFF/C         | PETN crystal                 | 32480                    | 976 Mb        | 185x                 |
| COMB2 (fixed q)  | Ti                           | 32400                    | 31 Mb         | 55x                  |
| QEq              | crystalline SiO <sub>2</sub> | 32400                    | 85 Mb         | 284x                 |
| eFF              | H plasma                     | 32000                    | 365 Mb        | 306x                 |
| ReaxFF           | PETN crystal                 | 16240                    | 425 Mb        | 337x                 |
| VASP/small*      | water                        | 192 (512e <sup>-</sup> ) | 320 procs     | 17.7×10 <sup>6</sup> |

Intel Xeon 2.66 GHz, single processor

\*Not from LAMMPS

Courtesy of Steve Plimpton, Sandia  
<http://lammps.sandia.gov/bench.html>



# Current status of COMB3

## ❖ Semiconductors

- Si

## ❖ Metals

- Cu, Zn, Al, Zr, Ti, U

## ❖ Compounds

- $\text{Cu}_2\text{O}$ ,  $\text{ZnO}$ ,  $\text{UO}_2$ ,  $\text{NO}_x$ ,  $\text{NH}_3$ ,  $\text{Al}_2\text{O}_3$ ,  
 $\text{TiO}_2$
- TiN, AlN

## ❖ Carbon based systems

- CHO systems
- $\text{H}_2\text{O}$  and  $\text{O}_2$
- C/H/Cu/O/Zn
- CN
- CHON

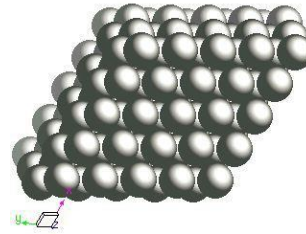
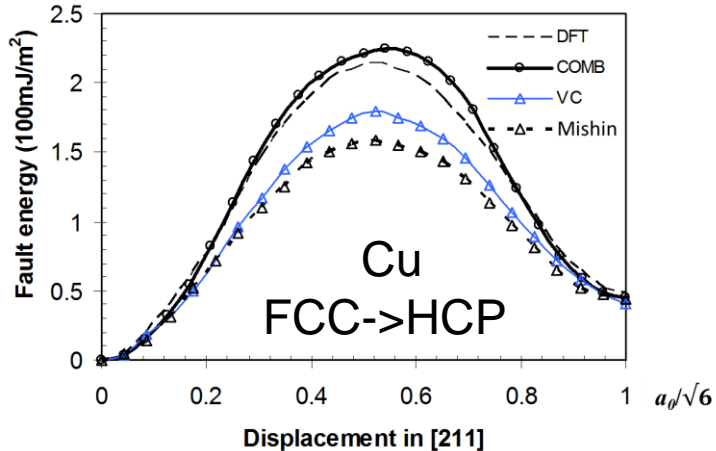
# Applications

- **Tensile test of polycrystalline Zr**
- Graphene/Cu<sub>2</sub>O interfaces
- Cu metallization on PS surfaces



# Stacking fault map of Zr

COMB -> Tersoff-type



Zr:

- hcp
- $a=3.23$
- $c=5.15$
- $c/a=1.59 < 1.633$

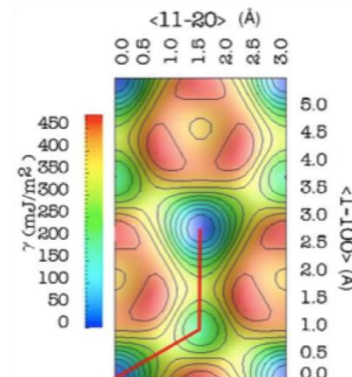
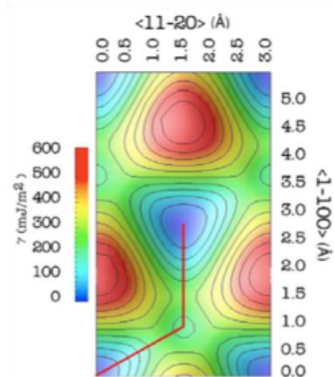
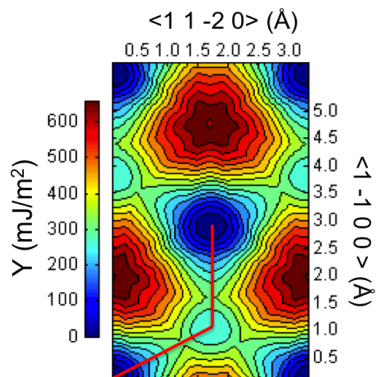
Yu et al., *Phil. Mag. Lett.*, 89 (2009)

Noordhoek et al., *J. Nucl. Mat.*, 441 (2013)

COMB: 267  
saddle 367

DFT: 213  
saddle 260

EAM: 199  
saddle 314



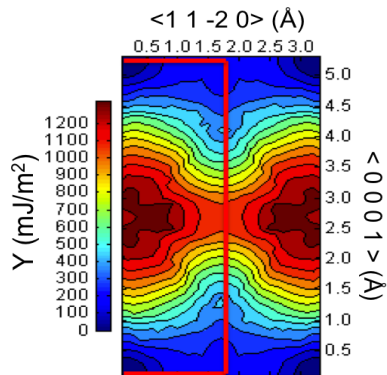
**HCP-> FCC:**

Basal {0001} stacking fault map

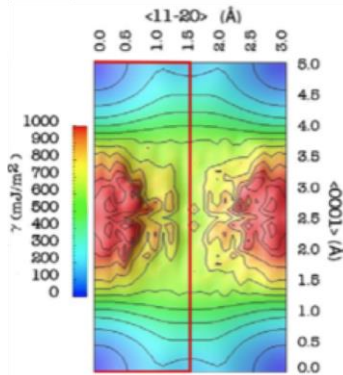
➤ {0001}  $\langle 11\bar{2}0 \rangle$

# Tensile test on polycrystalline Zr

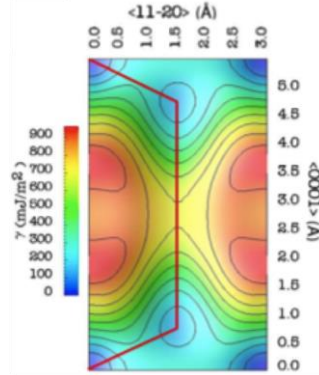
COMB: 215  
Saddle 247



DFT: 166  
saddle 194



EAM: 145  
saddle 190



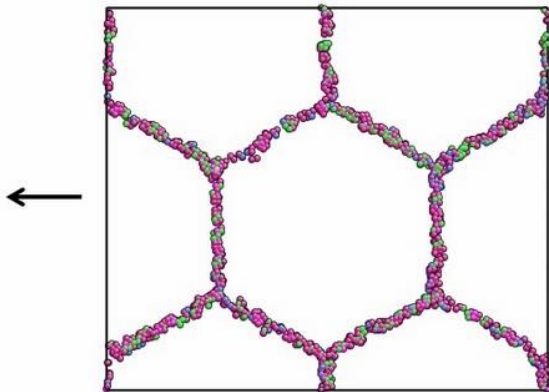
$c/a \ll 1.633$

Prism  $\{10\bar{1}0\}$  stacking fault map

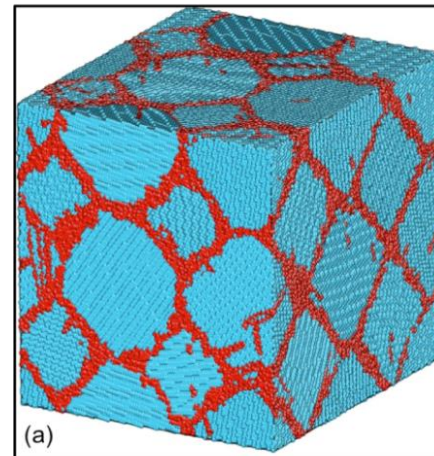
➤  $\{10\bar{1}0\} \langle 11\bar{2}0 \rangle$

$\{11\bar{2}2\} \langle 11\bar{2}3 \rangle$

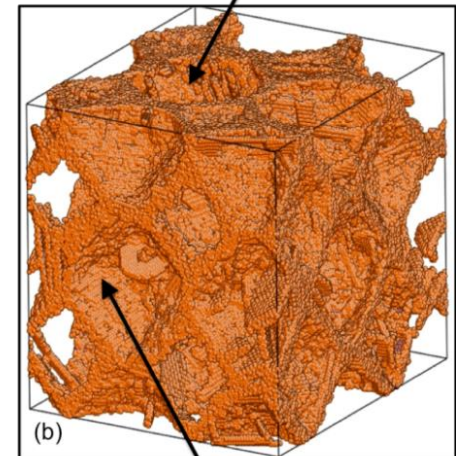
Colored by CN



Zr system



~3 million atoms



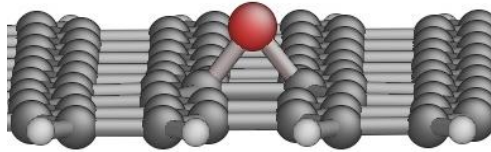
Prismatic slip

$\{10\bar{1}0\} \langle 11\bar{2}0 \rangle$

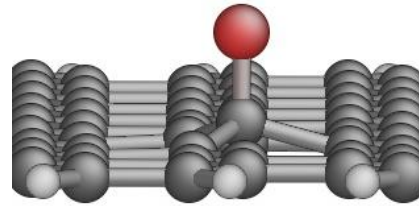
# Applications

- Tensile test of polycrystalline Zr
- **Graphene/Cu<sub>2</sub>O interfaces**
- Cu metallization on PS surfaces

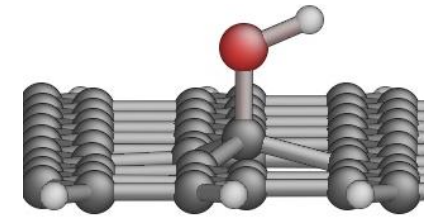
# Graphene oxides



GO-bridge



GO-atop



GO-Hydroxyl

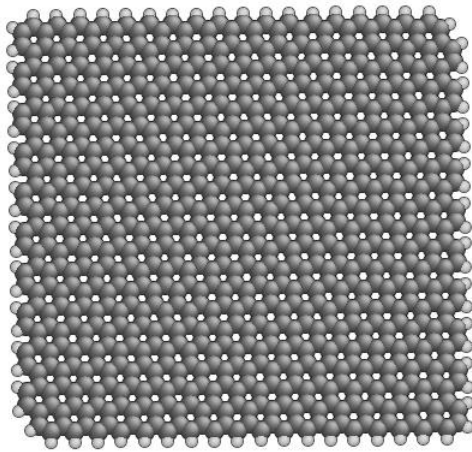
| O site      | Properties                     | DFT <sup>a</sup> | COMB  |
|-------------|--------------------------------|------------------|-------|
| GO-bridge   | C-O length (Å)                 | 1.44             | 1.40  |
|             | E <sub>ads</sub> (eV @ 0.1 ML) | -3.18            | -3.18 |
| GO-atop     | C-O length (Å)                 | 1.40             | 1.30  |
|             | E <sub>ads</sub> (eV @ 0.1 ML) | -2.43            | -2.40 |
| GO-hydroxyl | C-O length (Å)                 | 1.48             | 1.44  |
|             | E <sub>ads</sub> (eV @ 0.1 ML) | -1.48            | -1.48 |

<sup>a</sup>: A. F. Fonseca et al, *Phy. Rev. B* 84, 075460 (2011)



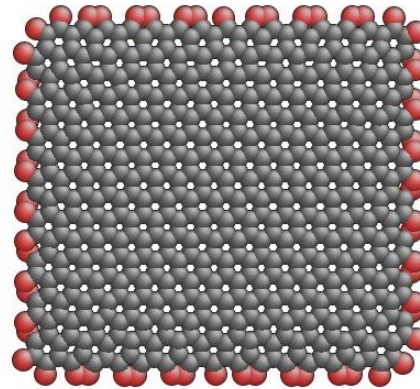
# Graphene adhesion on $\text{Cu}_2\text{O}$

4114 C atoms



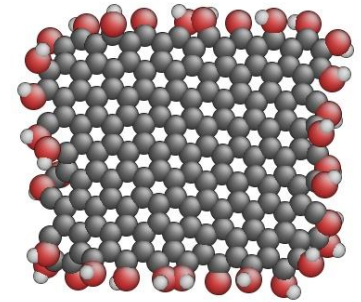
H-Terminated

796 C atoms

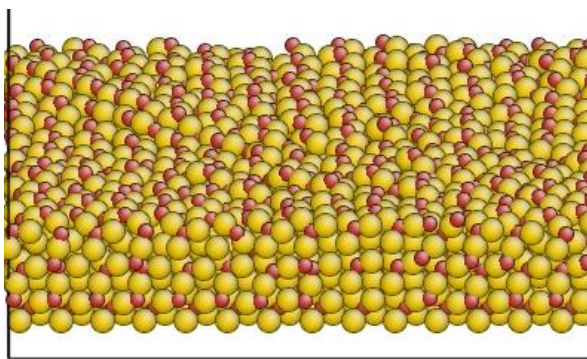


O Terminated

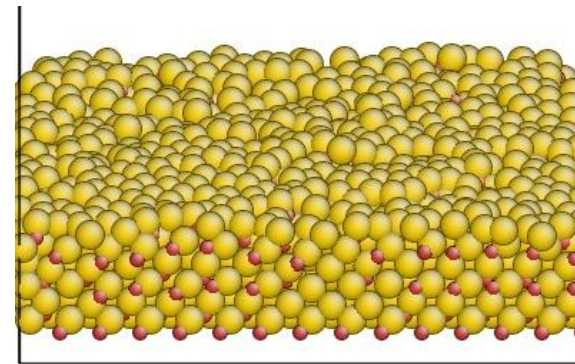
542 C atoms



OH Terminated

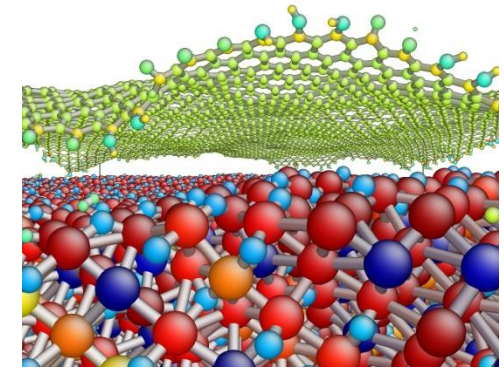
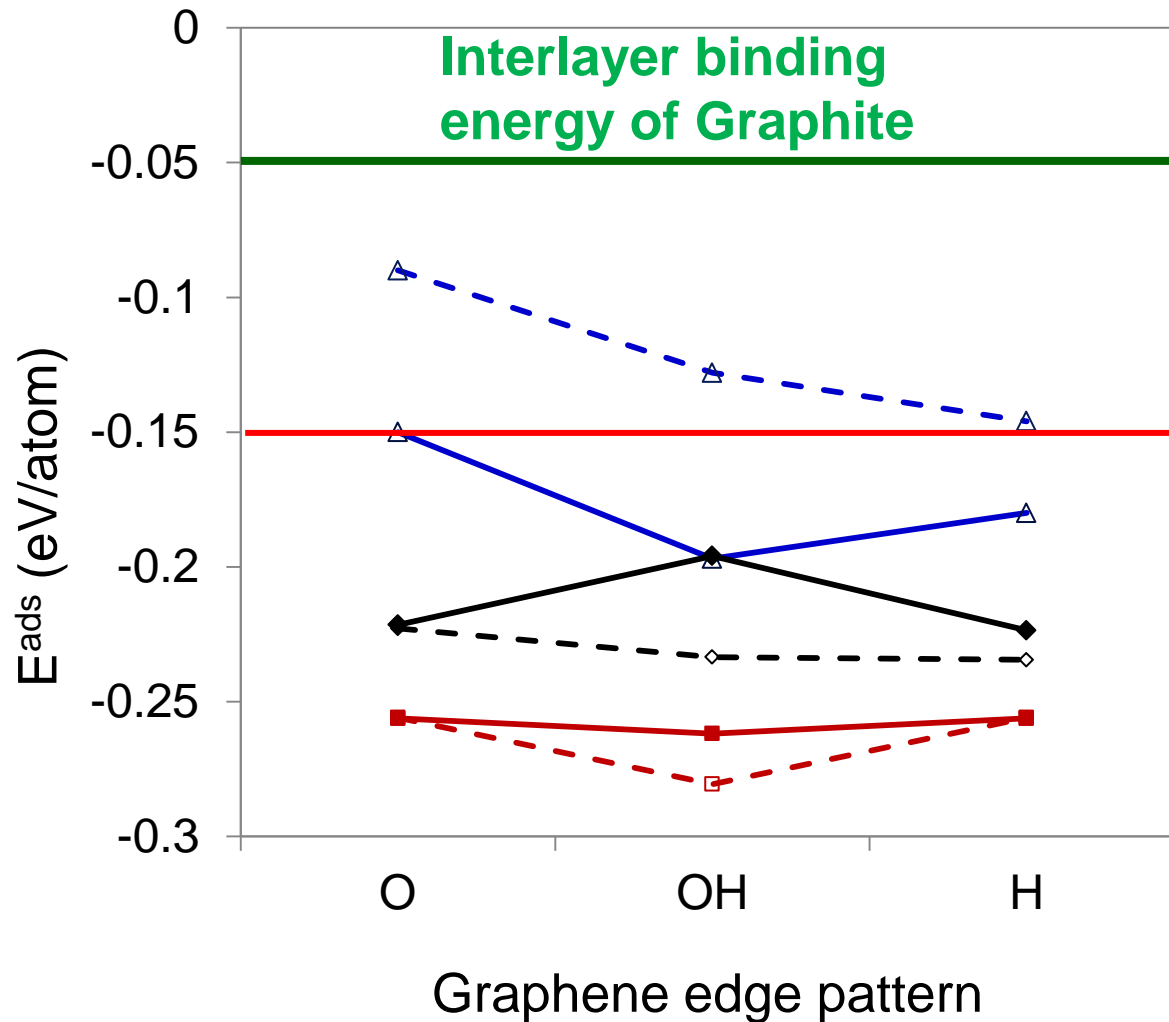


CuO-Termination



Cu-Termination

# Graphene adhesion on $\text{Cu}_2\text{O}$



Exp.  $E_{\text{ads}}$  on  $\text{SiO}_2$

Solid line CuO terminated and dash line Cu terminated  $\text{Cu}_2\text{O}$  substrate

Koenig et al. Nature Nano, 6 (2011)

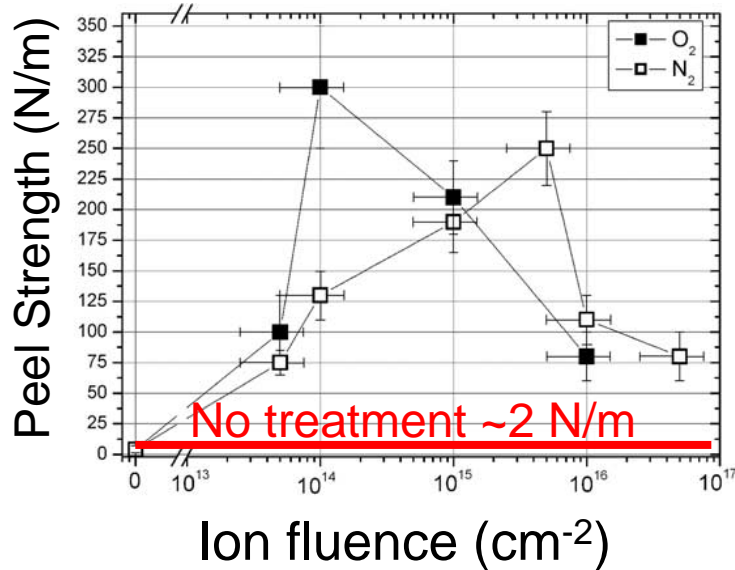
# Applications

- Tensile test of polycrystalline Zr
- Graphene/Cu<sub>2</sub>O interfaces
- **Cu metallization on PS surfaces**



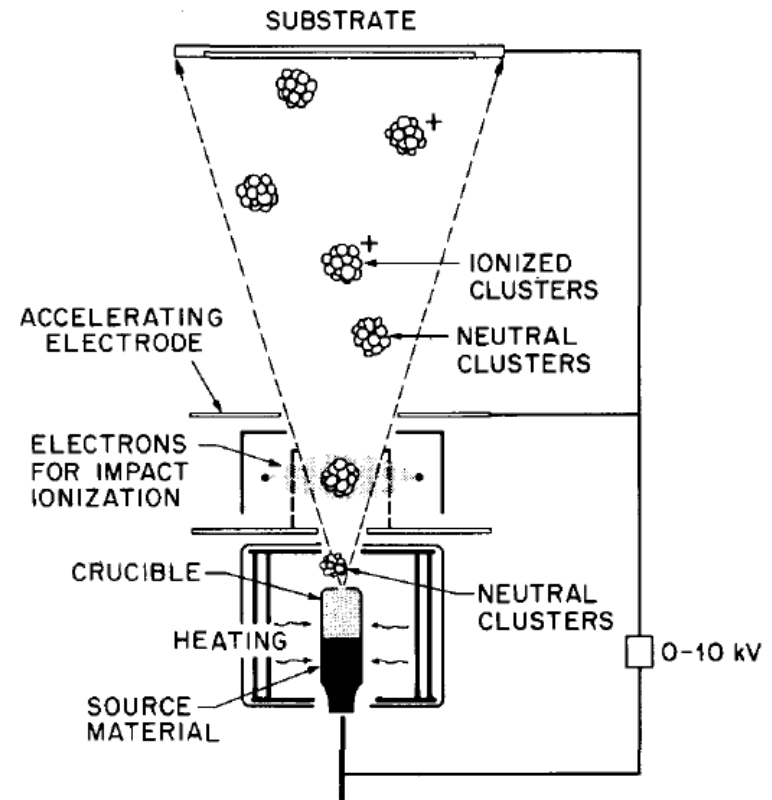
# Electroless metallization of polymers

- Poor wettability and adhesion
- Pre-treatments needed
  - Surface modification
  - Metal seeds
- Metal deposition



McEachern et al. J. Vac. Sci. Tech. A 9 (1991)  
Zaporojtchenko et al. Nucl. Instrum Meth. B,  
236 (2005)

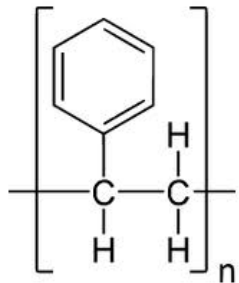
ion cluster beam deposition



Incident beam energy: several eV/atom  
Complex surface chemistry: adhesion,  
diffusion, nucleation, sputtering ....

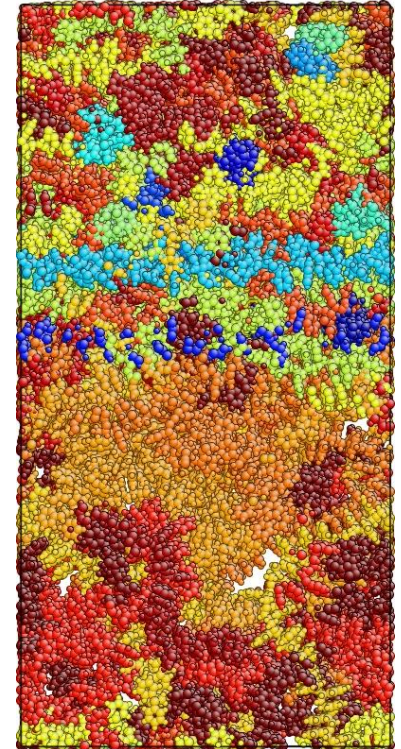
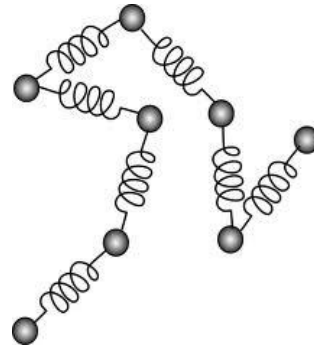
# Build amorphous polystyrene

Monomer



$C_8H_8$

Bead-spring



PS: Colored  
by chain ID

## Summary

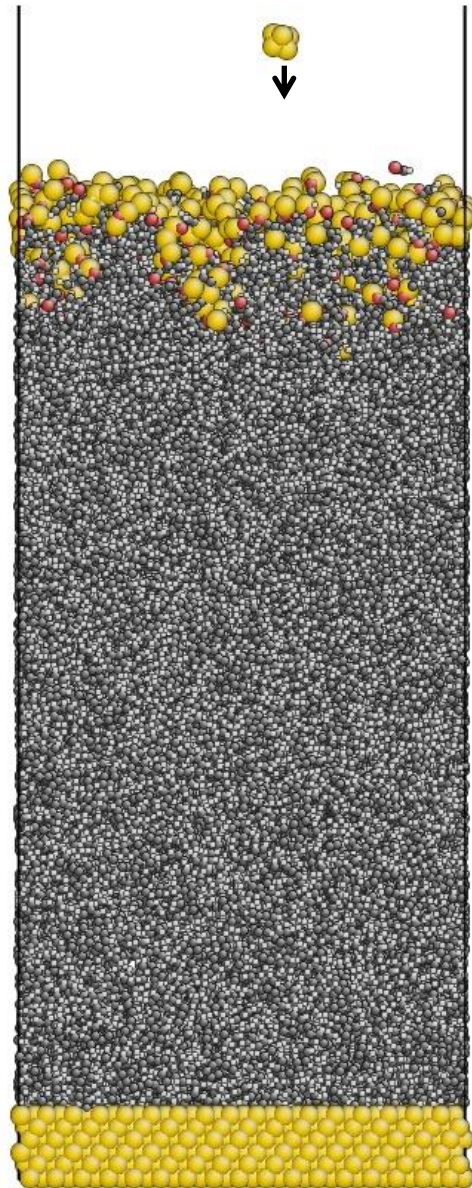
Density:  $1.05 \text{ g/cm}^3$

Molecular weight:  $\sim 23,000$

# of atoms:  $\sim 83,000$

# of C atoms:  $\sim 41,300$

As-build PS is relaxed and then built PS-O, PS-Cu,  
PS-OCu systems



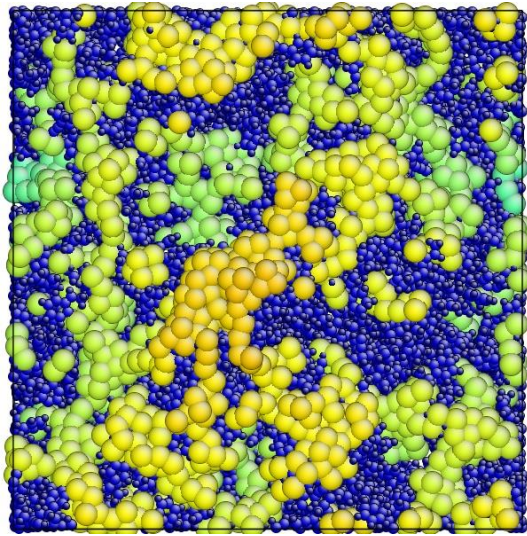
## Metallization on PS surfaces – Effects of surface modification and seeds

Summary:

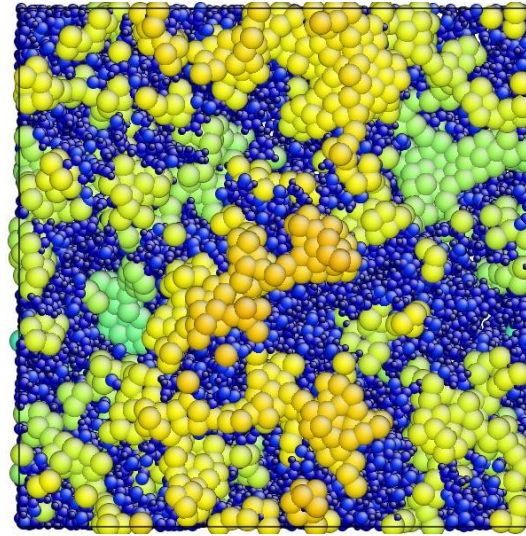
- PS built by bead-spring model
- PS, PS-O, PS-Cu and PS-OCu
- Incident molecules are 200 x Cu<sub>6</sub>
- Incident energies are 5 eV/atom
- Molecules are randomly distributed
- Relaxation time between deposition events is 0.5 ps
- Surface temperature is 300 K
- Total atoms ~90,000



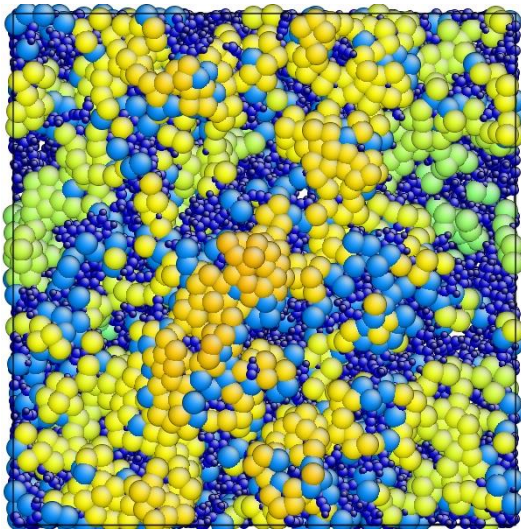
# 2 ML Cu on PS surfaces



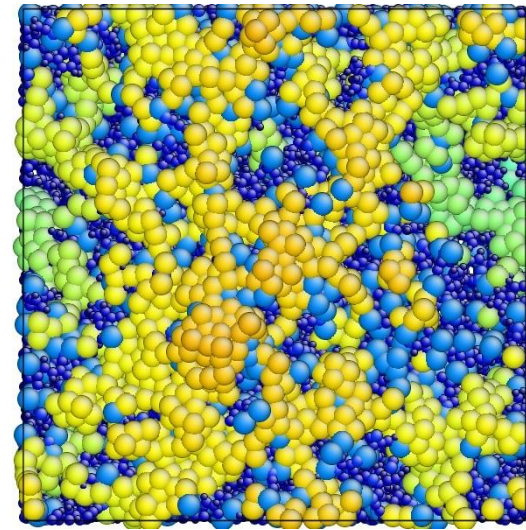
PS



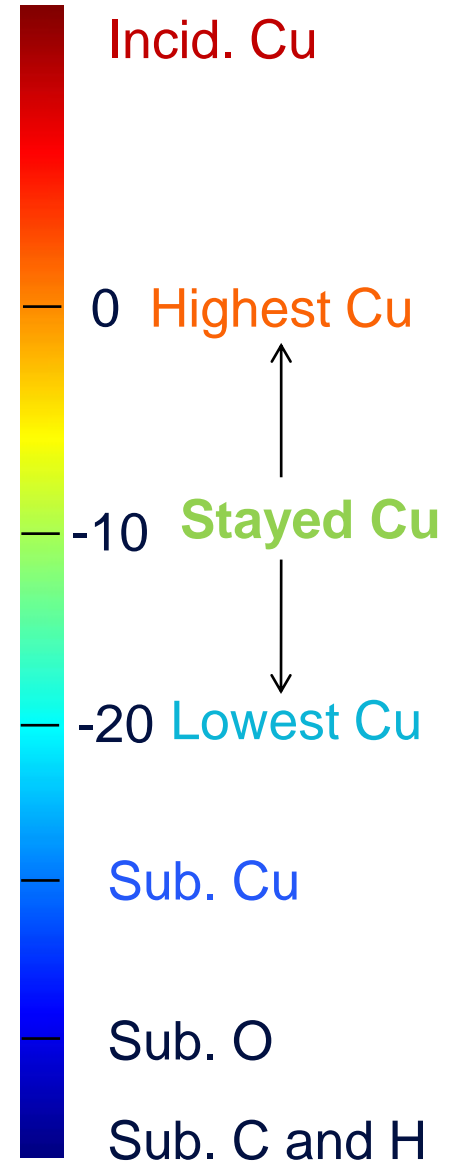
PS-O



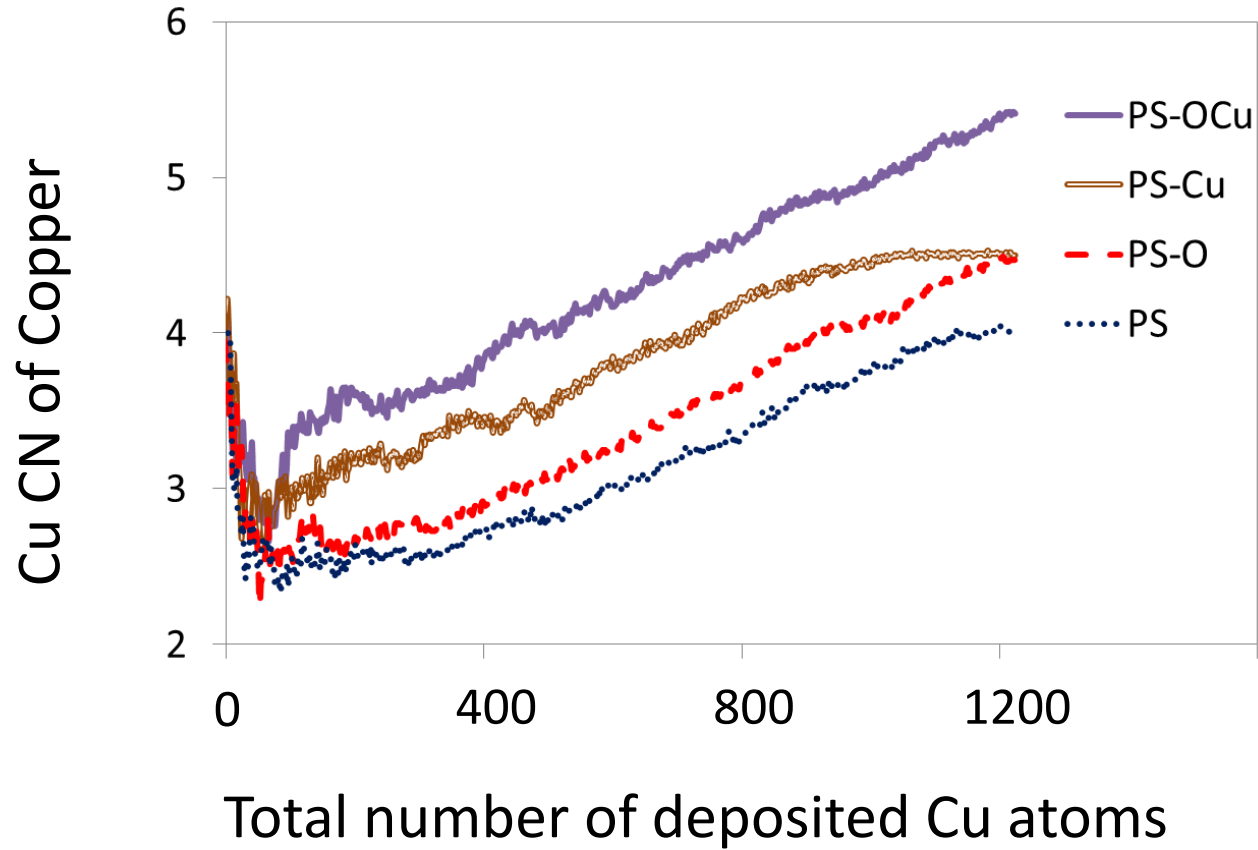
PS-Cu



PS-OCu



# Cu Coordination Number of Cu





# Conclusions

- Have developed an empirical, variable charge many body (COMB3) potential for modeling heterogeneous interfaces
- Successfully applied to atomic-scale simulations of systems consisting of discrete bonding types



Work with Steve Plimpton to disseminate COMB3 in LAMMPS

# Acknowledgement



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science



National Science  
Foundation



Center for Atomic-Level  
Catalyst Design



Consortium for Advanced  
Simulation of Light Water  
Reactors

