

Hydrogen-bonding Mechanical Effects
in Cross-linked Epoxy-Jeffamine Networks
from Molecular Dynamics Simulations

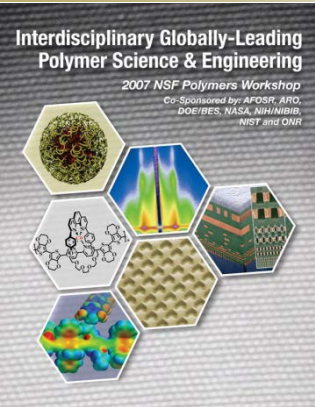
Craig Knox, Jan Andzelm, Joseph Lenhart
US Army Research Laboratory

Andrea Browning & Stephen Christensen
Boeing Research & Technology

August 9, 2011

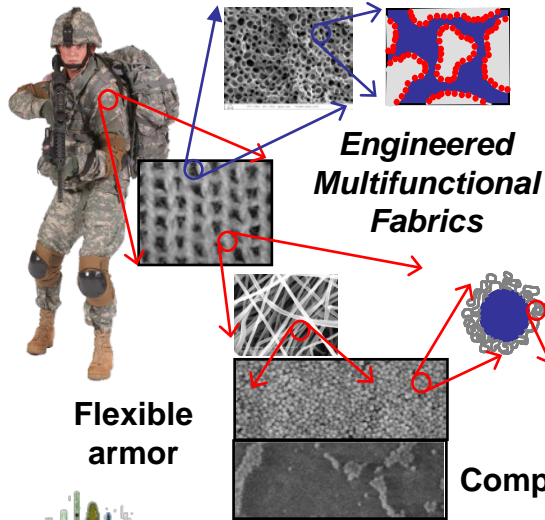
- Motivation/Background
- Methods
- Results
- Summary

Motivation/Background

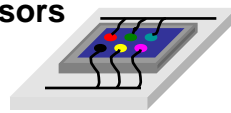


- “Polymers arguably represent the most important class of materials today; their multiple and tunable attributes underpin expanding use across most advanced technology platforms.”
 - Quoting from the report of a recent polymers workshop hosted by NSF and cosponsored by AFOSR, ARO, ONR, DOE, NASA, NIH, NIST and *Macromolecules* (2009) **42**(2) 465
- Polymer networks are **pervasive in military systems**

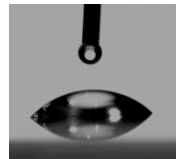
Soldier Protection



Flexible Sensors

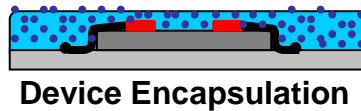


Membranes, filtration, decontamination

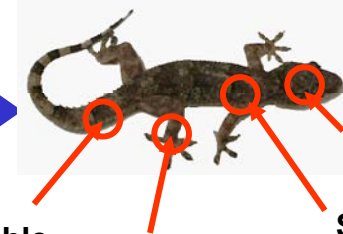


Coatings

Electronics, Power, Energy



Tough, durable, soft “body”



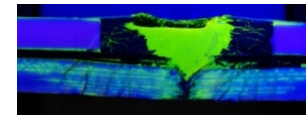
Controllable adhesion

Integrated soft sensors electronics

Soft actuators, “artificial muscles”

Robotics

Vehicles



Armor / structure

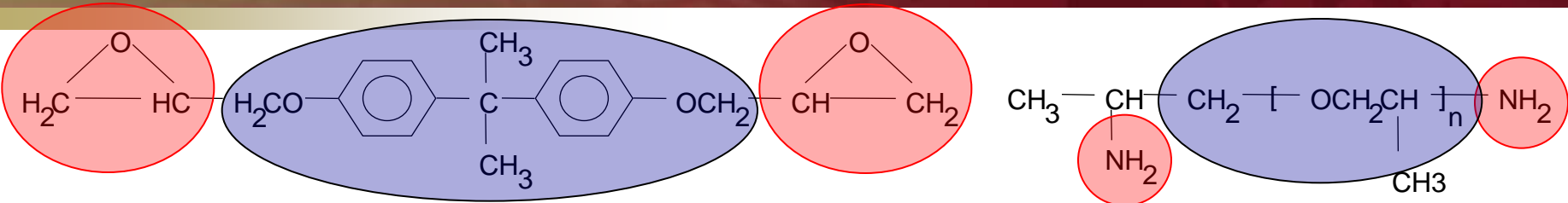


Weapons

Insensitive Munitions

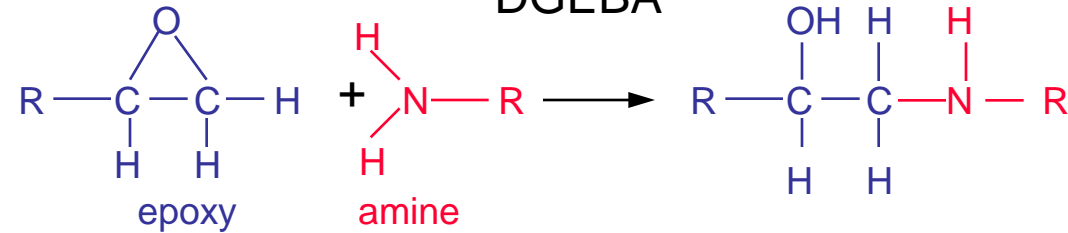
Low Observable Tracer Materials





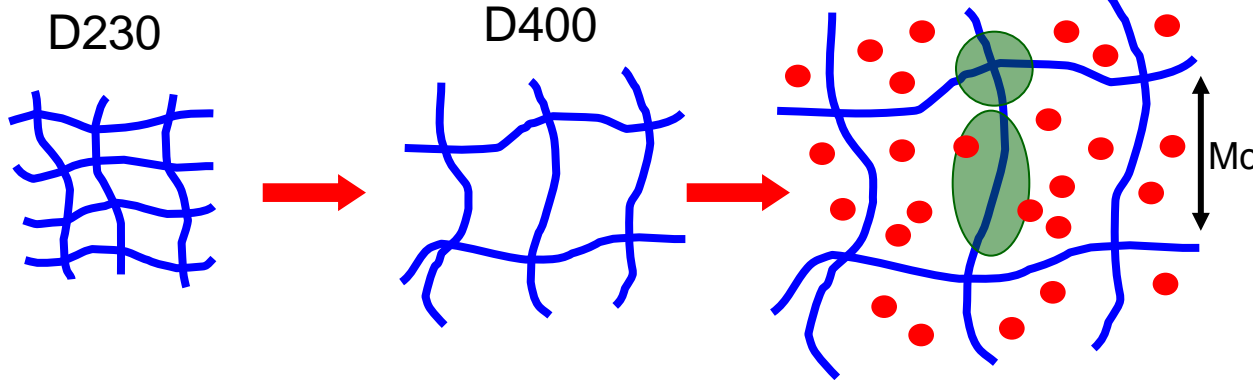
DGEBA

D2000, D400, D230



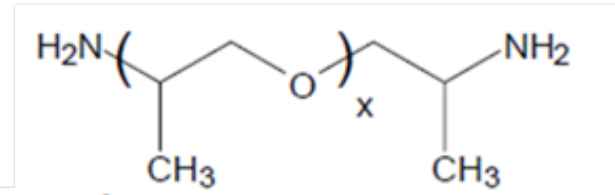
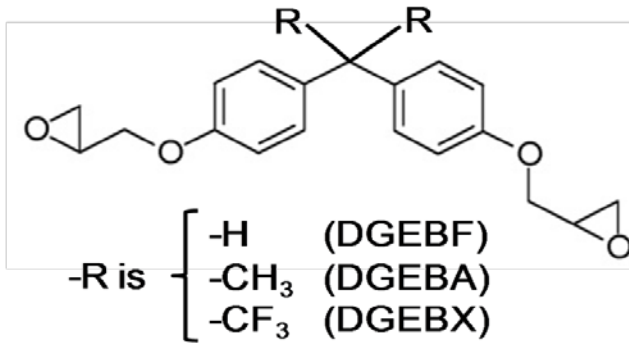
Mc = MW between crosslinks

1. Chemistry & functionality (# of rxn groups per chain)
2. Spacing between rxn groups (Mc)
3. Stiffness of junctions and backbone chains

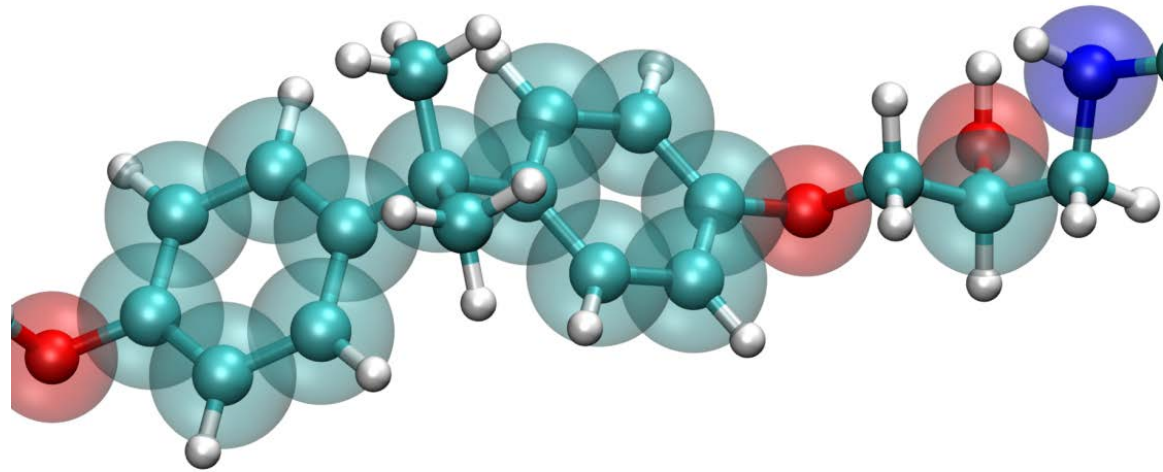


- Gels: loosely crosslinked, solvent swollen, soft materials
- Useful for bio-tissue surrogates and biomedical applications

Tg & rubbery modulus decrease; CTE & diffusion increase



JEFFAMINE [®]	x	MW*
D-230	~2.5	230
D-400	~6.1	430
D-2000	~33	2,000
D-4000 (XTJ-510)	~68	4,000



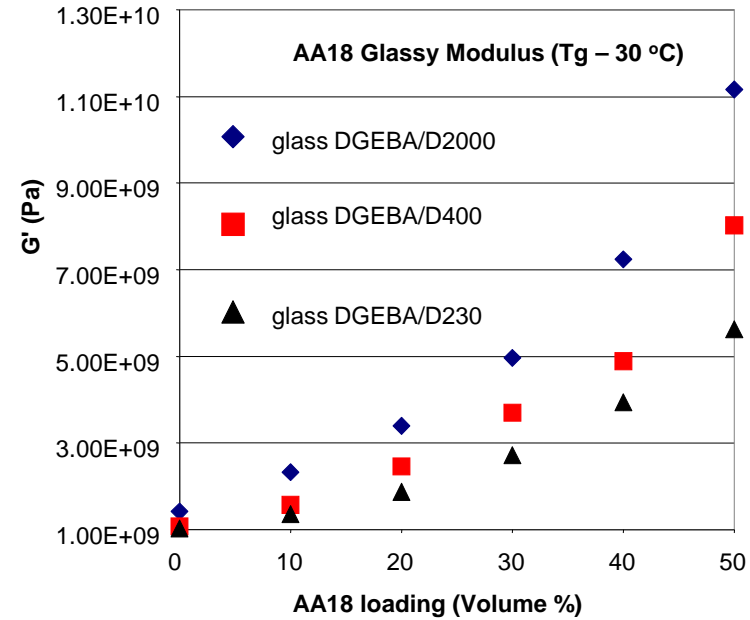
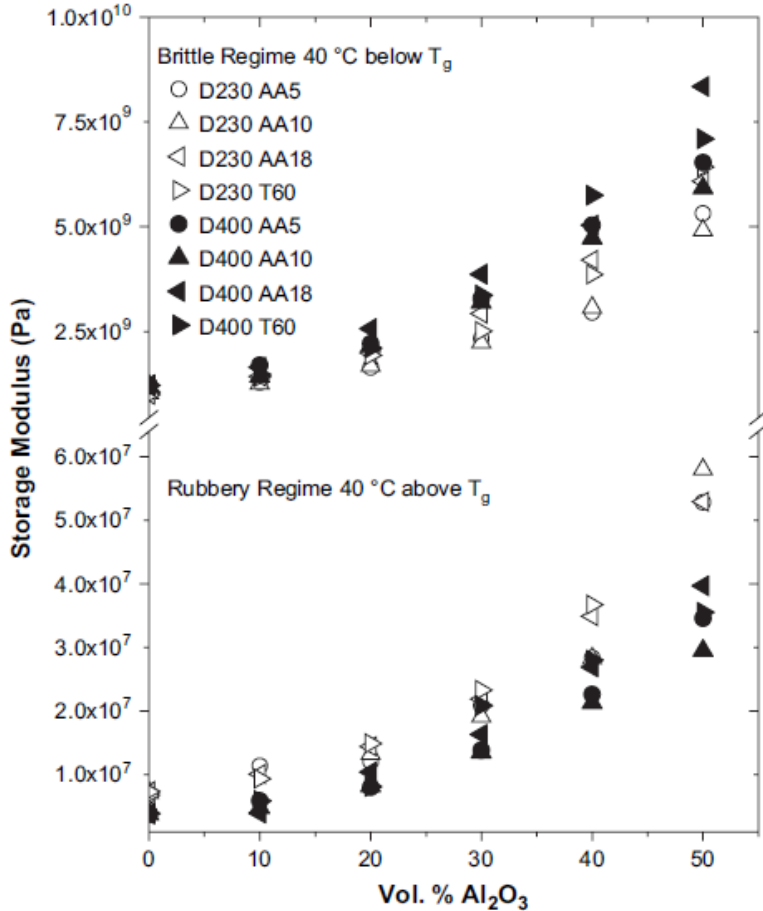
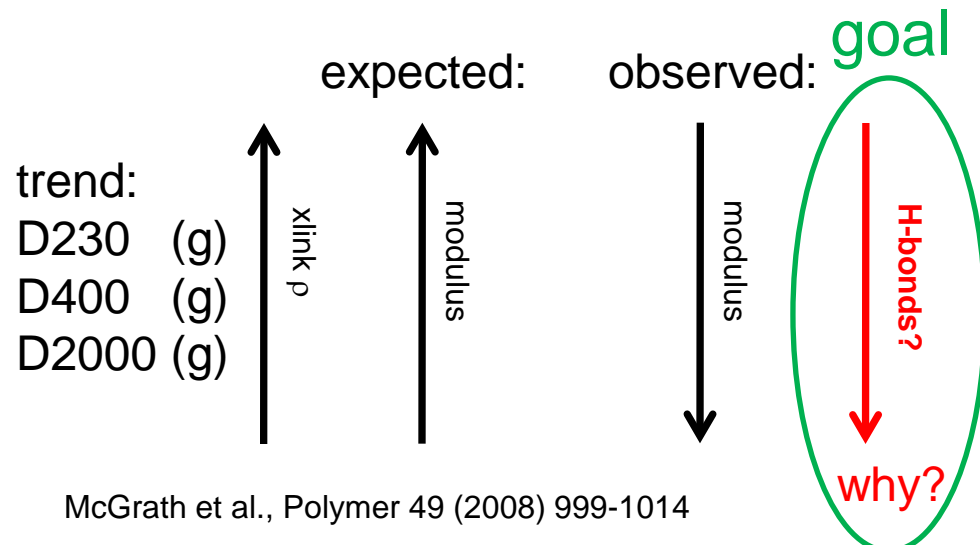


Fig. 5. (Top) the glassy modulus ($T_g - 40\text{ °C}$) for DGEBA/D230 (open symbols) and DGEBA/D400 (closed symbols) alumina composites as a function of alumina vol.%; (bottom) the rubbery modulus ($T_g + 40\text{ °C}$) for DGEBA/D230 (open symbols) and DGEBA/D400 (closed symbols) alumina composites as a function of alumina vol.% and particle type. The error is $\pm 10\%$ and was determined by multiple sample measurements.



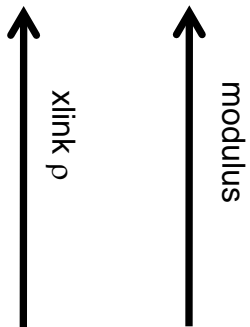
McGrath et al., Polymer 49 (2008) 999-1014

uni-tension
w/ Instron

strain rate =
 $\sim 10^{-3}$ 1/s

(for ~ 1 cm sample size,
 ~ 2.5 mm/min / 10 mm =
 $4e-3$ 1/s)

observed:



contradiction?

	T_g (in $^{\circ}\text{C}$)	Crosslink Density, ν (in moles/cc)	Glass Modulus at $T_g - 40^{\circ}\text{C}$ (in GPa)	Rubber Modulus at $T_g + 40^{\circ}\text{C}$ (in MPa)	Glass Strength at $T_g - 40^{\circ}\text{C}$ (in MPa)
Epon/D230	80	1.29×10^{-3}	3.1 ± 0.2	12.7 ± 2	51.2
Epon/D400	47	9.62×10^{-4}	2.4 ± 0.1	8.7 ± 0.8	60
Epon/D2000	-38	2.8×10^{-4}	1.3 ± 0.7	2	67.6

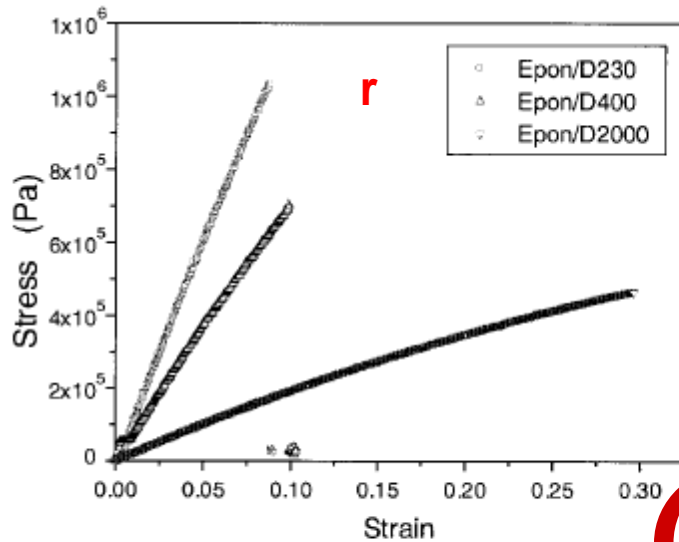


Figure 2. Stress-strain relationship at the glassy state for Epon/D230, Epon/D400, and Epon/D2000. Strain rate = 2.5 mm/min. Testing temperature are 40, 7, -78°C , respectively.

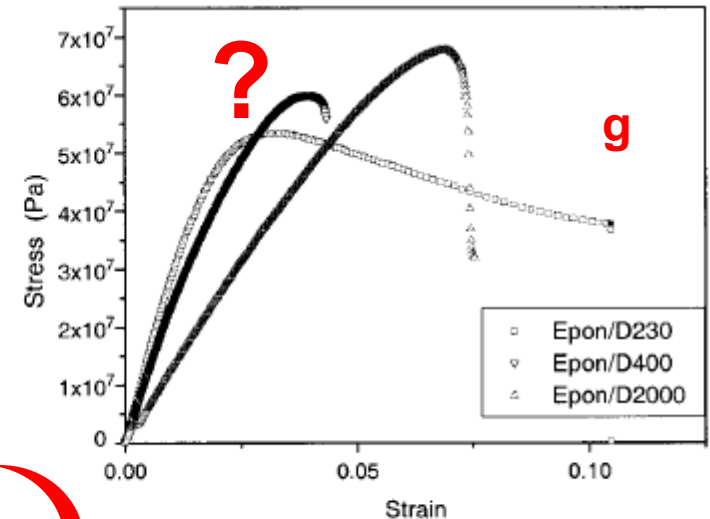
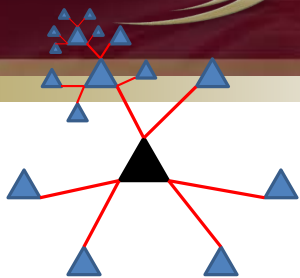


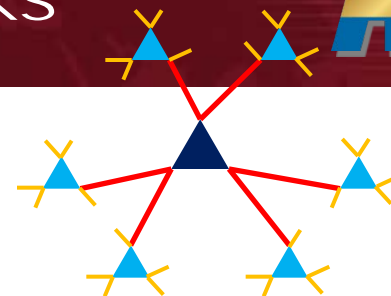
Figure 3. Stress-strain relationship at the rubbery state for Epon/D230, Epon/D400, and Epon/D2000. Strain rate = 2.5 mm/min. Testing temperatures are 120, 87, and 8°C , respectively.

L. Shan et al., J Polym Sci B: Polym Phys, 37, 2815-2819 (1999)

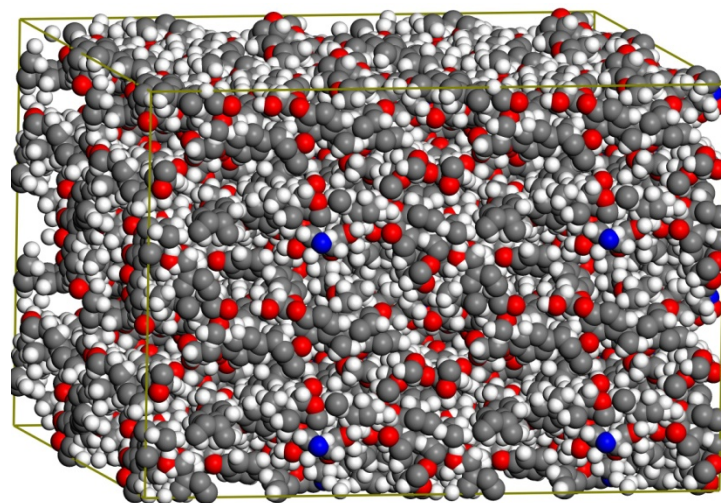
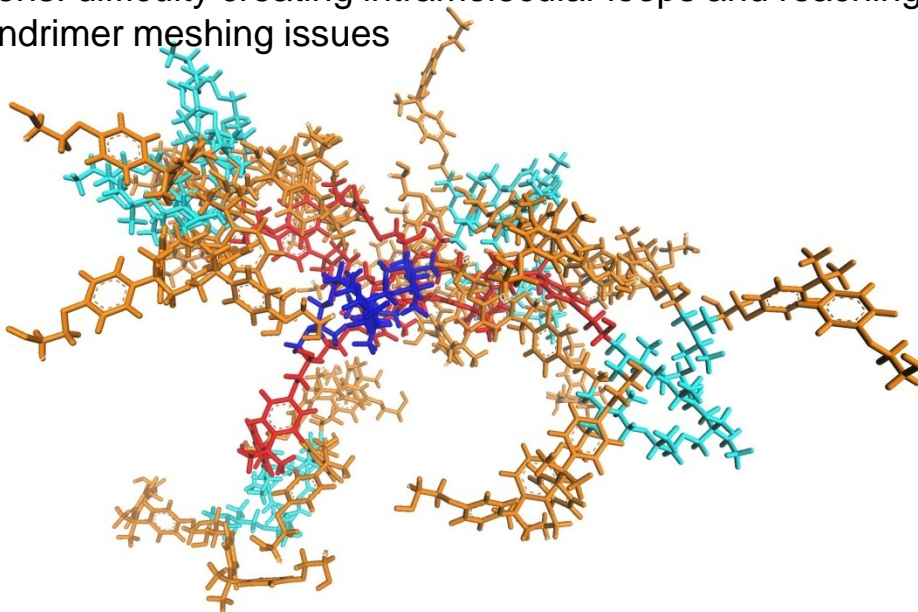
Methods



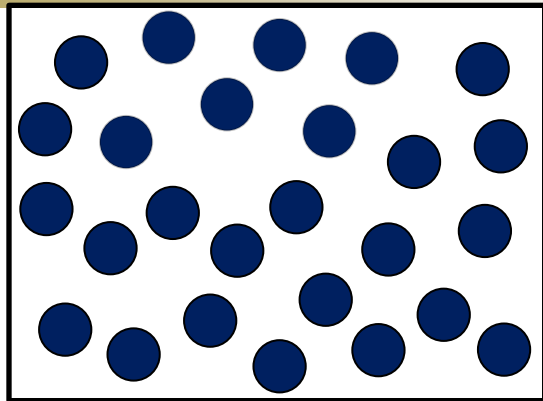
Growing Dendrimers (Boeing: Christensen & Browning)



- Build networks by growing ideal (perfect) dendrimers, then randomly modify crosslinks to add distortion/defects (dangling ends and unreacted sites) as well as to control stoichiometry
- Pack multiple dendrimers into a box using Amorphous Cell in Materials Studio or Amorphous Builder of MAPS and then compress/anneal/equilibrate in LAMMPS
- Pros: avoidance of artificial network strain during curing, low computational cost, availability of code
- Cons: difficulty creating intramolecular loops and reaching very high cure; small network approx. and inter-dendrimer meshing issues

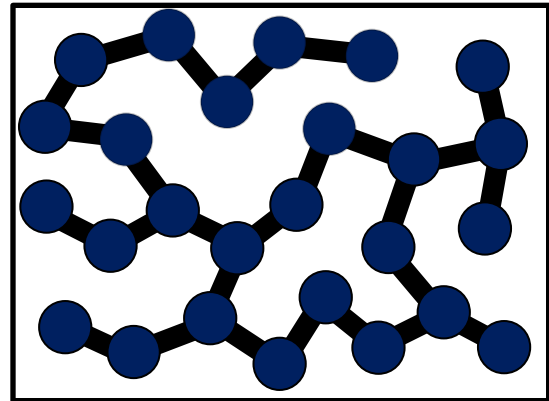
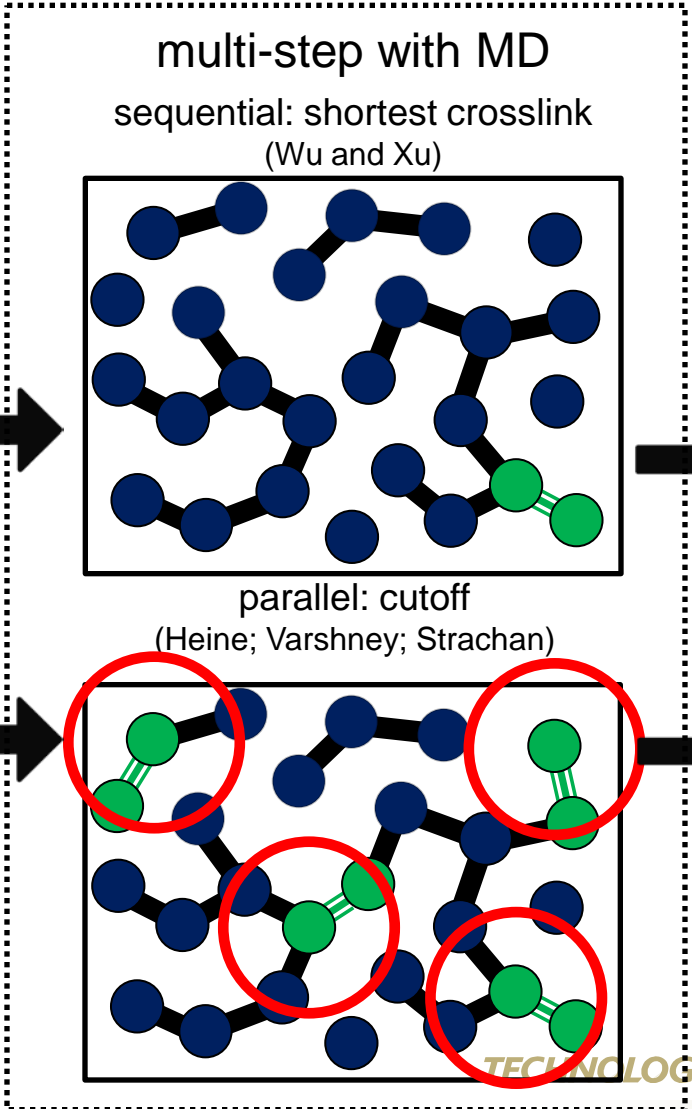


one-step



initial mix after MD

(Yarovsky and Evans, Lin and Khare)



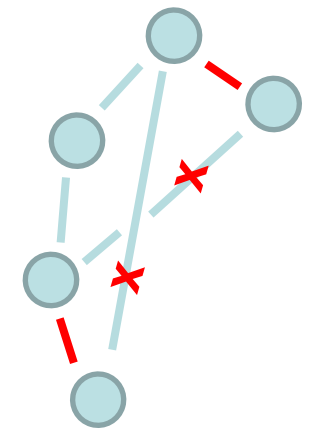
crosslinked network

Pros

- more realism (e.g., loops)
- complete (large) network
- chemical insight included
- up to 100% cure (difficult)

Cons

- high computational cost
- preventing artificial strain
- code complexity (changing topology and charges on-the-fly)



optimization
(Lin and Khare)

Method	Authors	Cure	Size	Strain	Human Effort	CPU Cost	Loops	Systematic	Comments
dendrimer	Christensen	~85%	M	0	M	L	N	Y	fast and no strain no intramolecular loops small network approx.
1-step rxn	Lin and Khare	100%	L	M	L	M	Y	Y	MC optimization high cure
1-step rxn	Yarovsky and Evans	~70%	S	H	M	L	Y	Y	steric/reactivity insight big cutoff low cure
multistep rxn: sequential	Wu and Xu	~90%	S	L	L	H	Y	Y	slow kinetics issue high CPU cost
multistep rxn: parallel	Heine et al.	~90%	L	M	L	M	Y	Y	growing cutoff needed
multistep rxn: both	Varshney et al.	~90%	L	M	L	M	Y	Y	sequential or parallel rxn
multistep rxn: parallel	Li and Strachan	~80%	L	M	M	M	Y	Y	dynamic Gasteiger charge calc.

per-dendrimer counts:

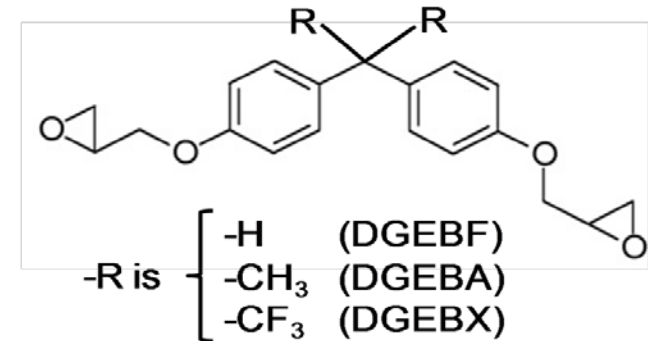
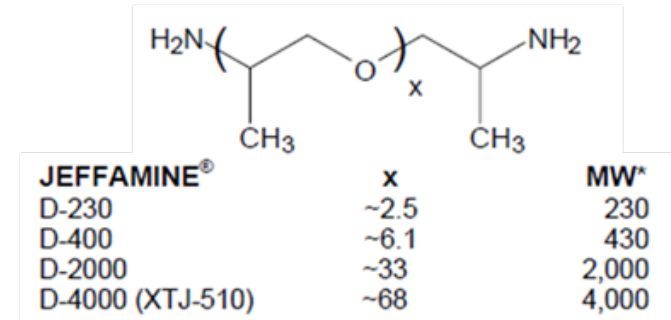
System	# of atoms	# of amine mers	# of epoxy mers	# of gens
A230	10,152	70	140	9
A2000	10,237	23	46	7
F230	9,312	70	140	9
F2000	9,961	23	46	7

stoichiometry = 2:1 (epoxy:amine)

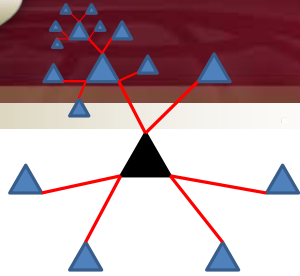
Each system contains 8 identical copies of a dendrimer

3 dendrimer reps of each system
(each rep has unique/random cross-link topology but same mer and total cross-link counts)

Both A and F systems of a given amine have identical cross-link topology

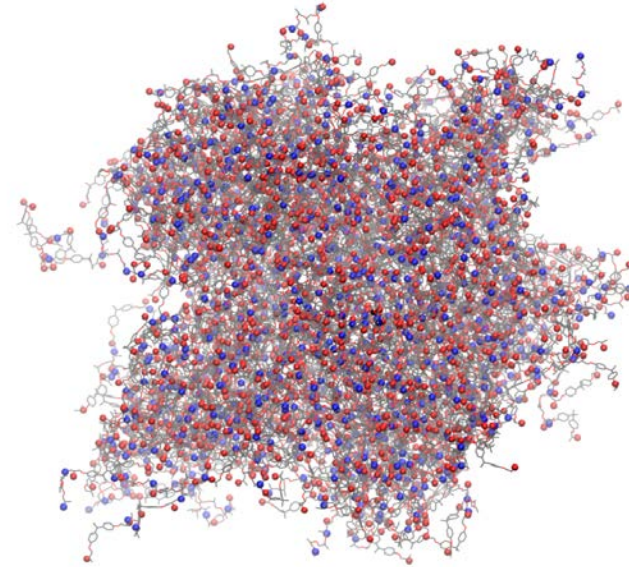


GAFF w/ COMPASS charges

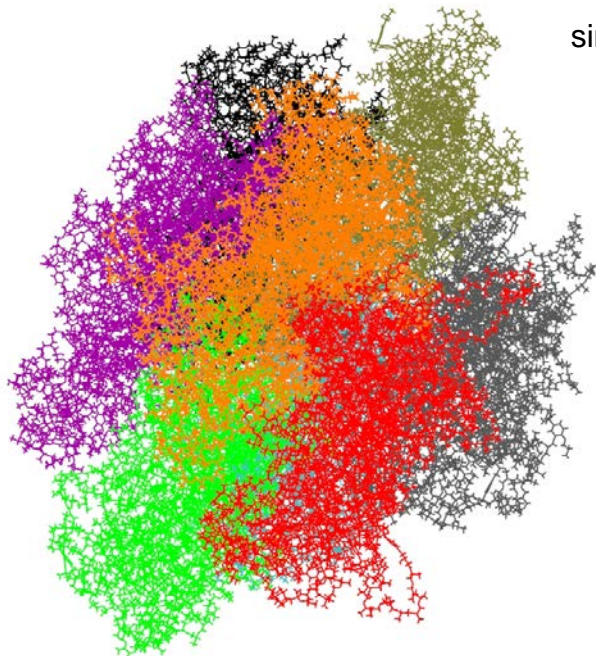


8 x 10K-atom-dendrimers

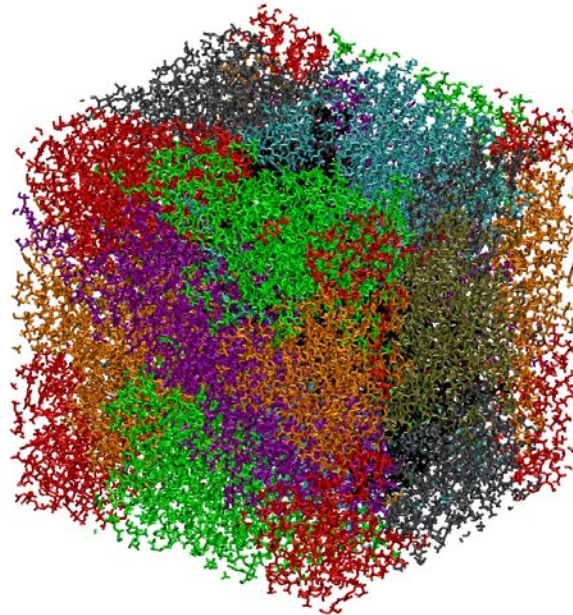
single dendrimer colored by generation



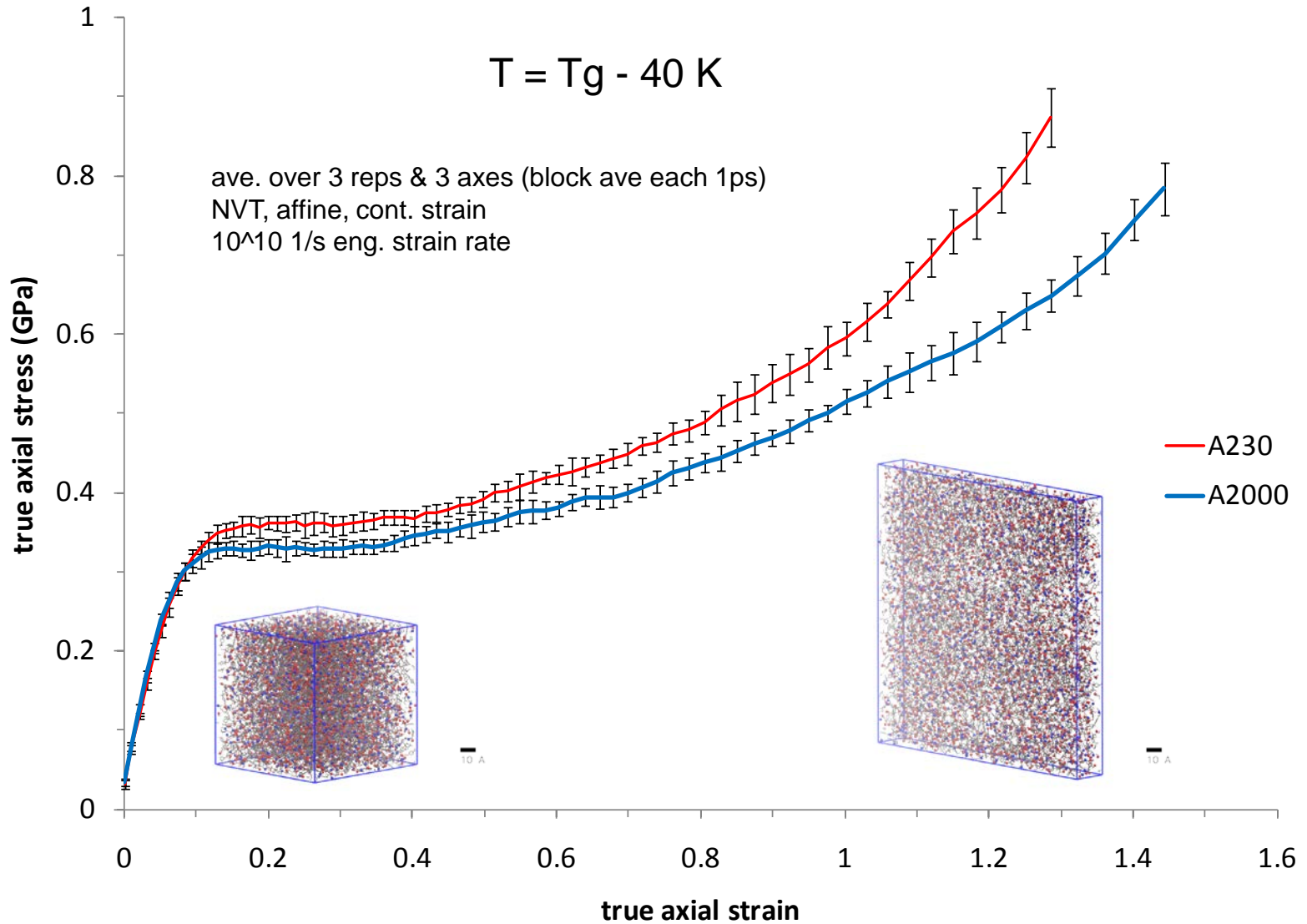
donors (N,OH) as balls
oxygen
nitrogen
carbon
no hydrogens



colored by dendrimer

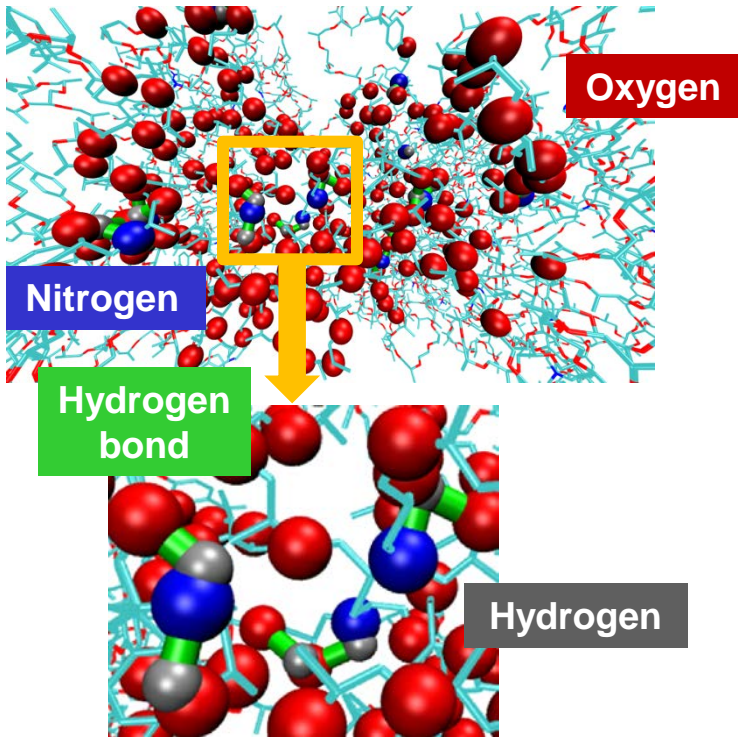


**Many H-bond donors
and more acceptors!**

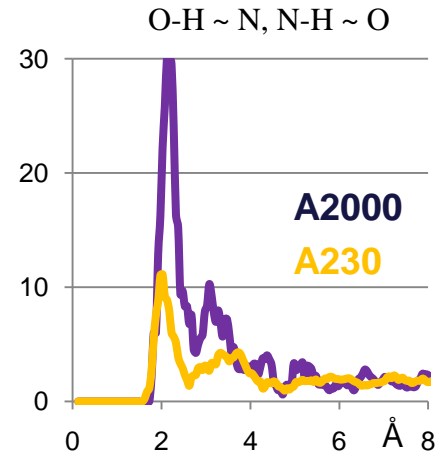


Results

Can H-bonding explain glassy modulus A2000 > A230 trend?



Radial Distribution Function:



More H-bonding (bigger peak) in A2000
(polymer flexibility, H-bond strength at Tg)

H-bond types:

$$\{h\} \text{O-H} \sim \text{O}_{\{ee,ea,h\}}, 1 \times 3 = 3 \text{ combinations}$$

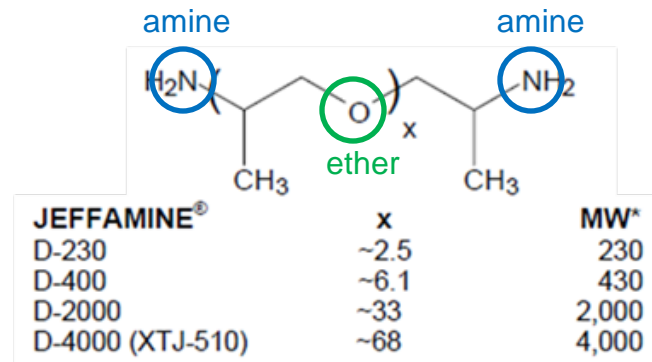
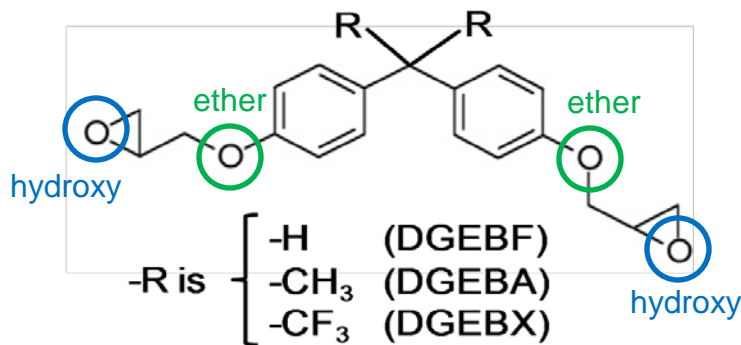
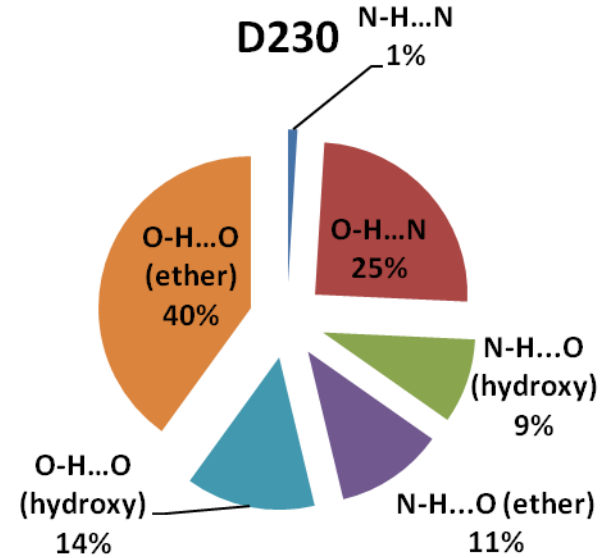
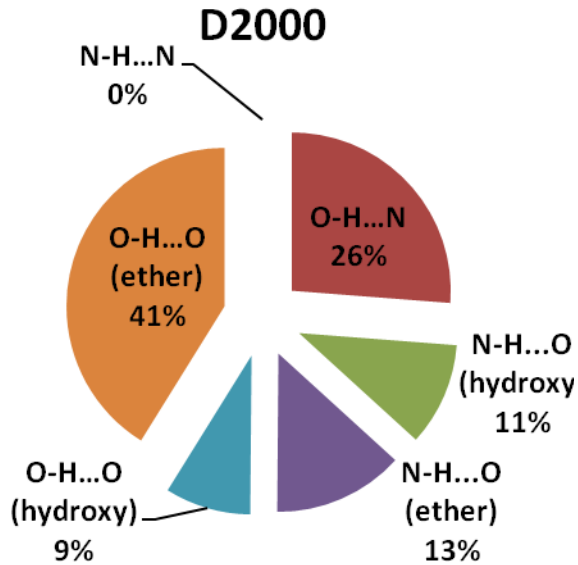
$$\{h\} \text{O-H} \sim \text{N}_{\{a1-3\}}, 1 \times 3 = 3$$

$$\{a1-2\} \text{N-H} \sim \text{O}_{\{ee,ea,h\}}, 2 \times 3 = 6$$

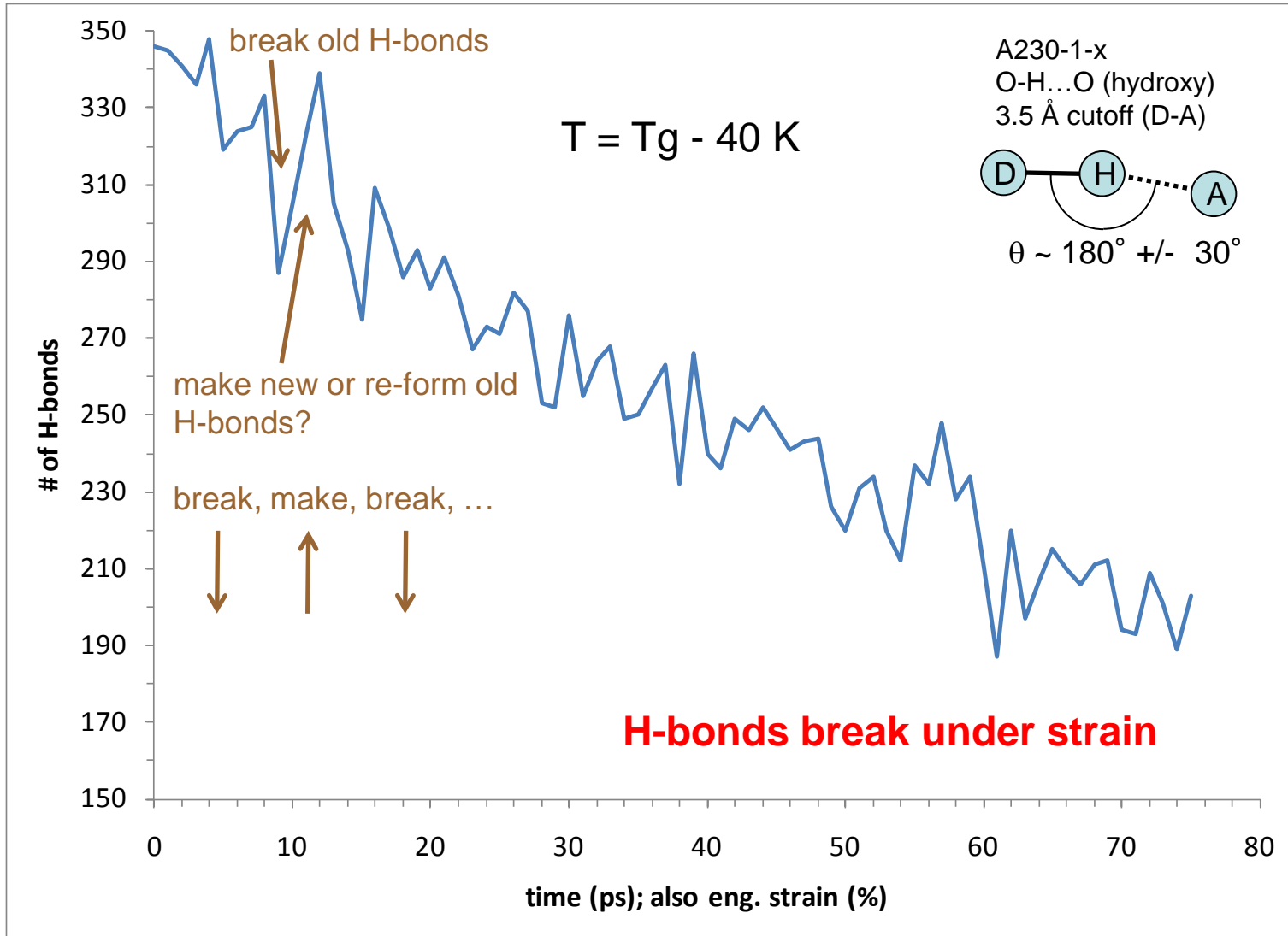
$$\{a1-2\} \text{N-H} \sim \text{N}_{\{a1-3\}}, 2 \times 3 = 6$$

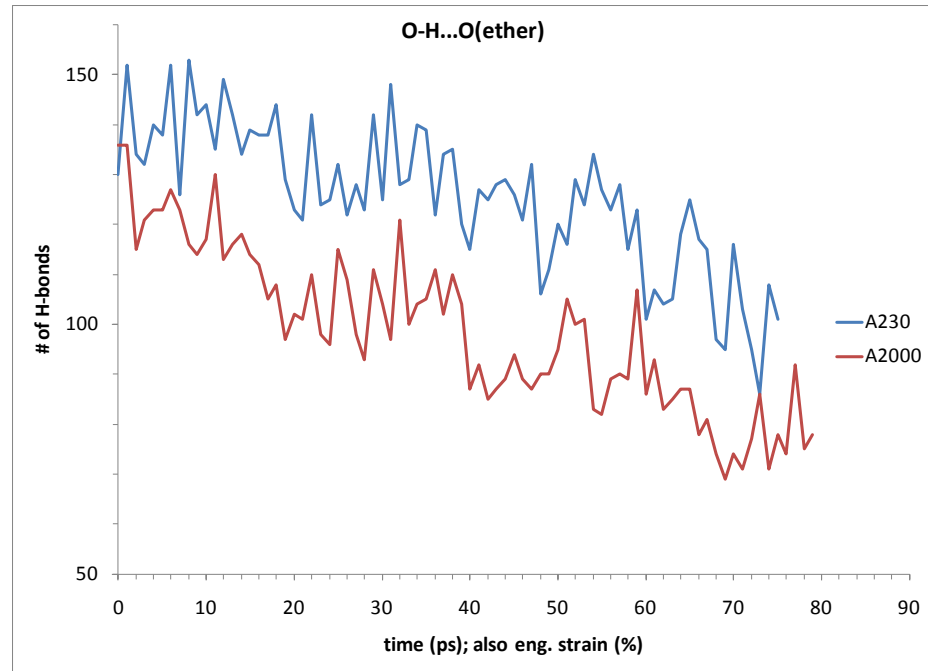
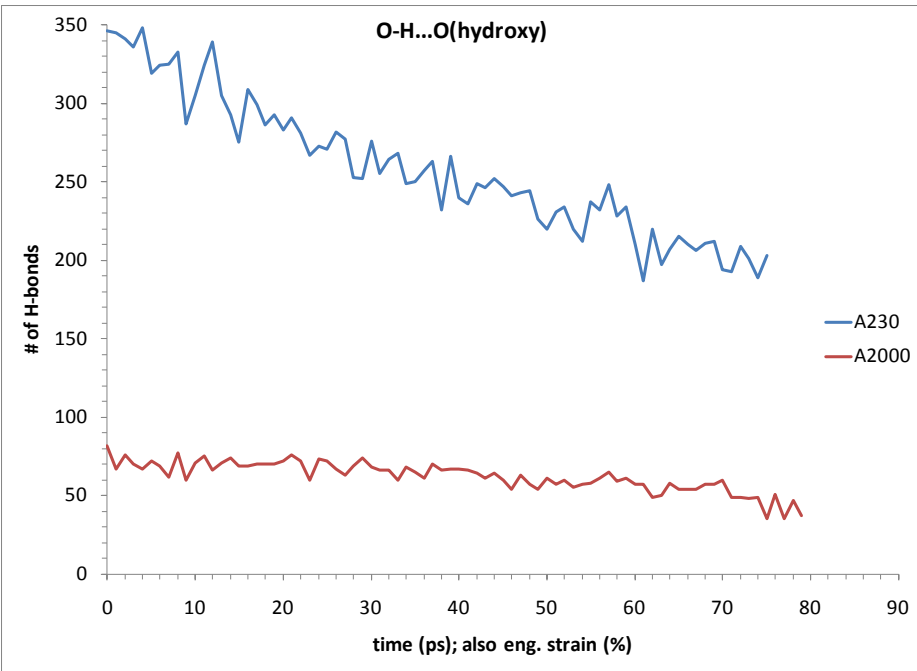
Labels of H-bonding species

Tag	Description	Proton Donor/Acceptor
a1	primary amine (-NH ₂),	D/A
a2	secondary amine (-NH-),	D/A
a3	tertiary amine (-N<)	A
h	hydroxyl (-OH) in epoxy resin	D/A
ee	ether (-O-) in epoxy resin	A
ea	any ether in Jeffamine curing agent	A



Universal fractions of H-bond types





D2000 hydroxy-ether H-bond count similar to D230 despite ~3x more donors in D230

Young's modulus (GPa): **big drop in E!**

$$T = T_g - 40 \text{ K}$$

Sys/Test	reg (exp)	noHB	noXL	noHB & noXL
A230	4.03 (2.25)	1.30	2.62	0.73
A2000	4.23 (3.35)	2.83	3.62	2.47
F230	3.64 (2.37)	1.03	2.34	0.38
F2000	4.05 (N/A)	2.69	3.44	2.45



noHB = no hydrogen-bonds (turn off Coulomb between all H-A pairs)

noXL = no cross-links (cut all N-C bonds & angles/dihedrals/impropers)

reg = regular (HB + XL)

exp = DMA storage modulus

Trends:

- A > F
- 2000 > 230 (agrees w/ DMA exp)

NOTES:

- stdev ~ 0.1 GPa
- E = init. stress-strain slope up to 5% strain
- after 100ps NPT re-equil after toggle
- for noXL, ramp N-C VDW from 0 to full over 1st half of re-equil

Order is preserved regardless of toggle: why?

$$A2000 > F2000 > A230 > F230$$

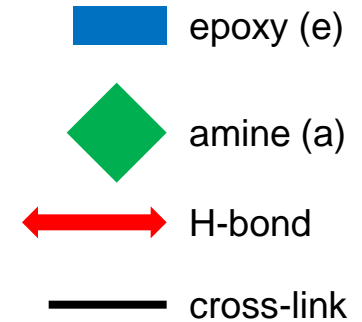
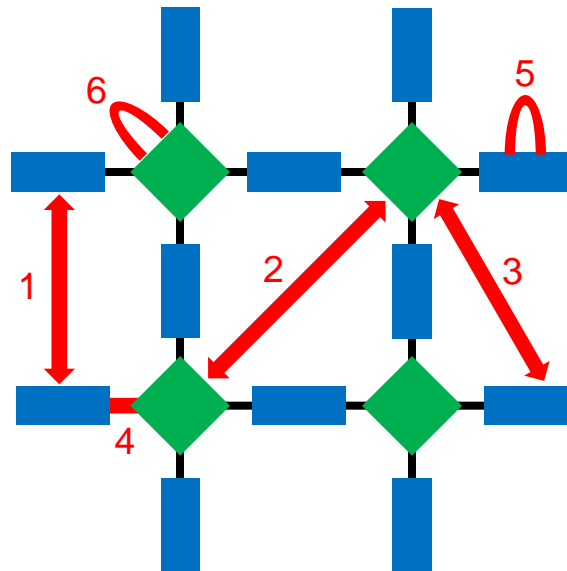
Observations:

- noHB and/or noXL affects 230 more than 2000
- noHB affects E more than anticipated
- noHB < noXL

H-bonding strongly affects mechanics

Physical vs. chemical cross-links

Where are H-bonds?



inter-mer:

1. e-e
2. a-a
3. e-a (no XL)
4. e-a (w/ XL)

} stiffeners?

intra-mer:

5. e
6. a

inter- vs. intra-dendrimer

Not all H-bonds are equal...

Which H-bonds increase stiffness?

Probably 1-3

H-bonds may act as **physical cross-links** to stiffen network

- ✓ strain hardening in stress-strain curves, in agreement w/ exp
- ✓ ~1.5-2.5 GPa drop in E after turning off H-bonds
- ✓ H-bonding strongly affects mechanics and may be important in design
- ✓ A>F & 2000>230 trends in E (in agreement w/ exp), regardless of toggle (noHB,noXL)
- ✓ Turning off H-bonds drops E more than cutting cross-links
- ✓ 230 has more H-bonds per mass (or volume) but 2000 has more per donor (more effective H-bonding?)
- ✓ Why 2000 > 230 modulus is still unknown (entanglements/sterics?)

Acknowledgments

Ian McAninch & Andrew Schoch

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ORISE/ORAU Postdoctoral Research Fellowship Award

LAMMPS, VMD, Materials Studio, MAPS

Thanks

“The instantaneous pressure [or stress tensor] of a simulation cell... will have mean square fluctuations (according to David Case quoting Section 114 of Statistical Physics by Landau and Lifshitz) of

$$\langle \delta\sigma^2 \rangle \sim \frac{kT}{V\beta} \sim \frac{1}{N}$$

, where b is the compressibility, which is RMS of roughly 100 bar for a 10,000 atom biomolecular system. Much larger fluctuations are regularly observed in practice.” (NAMD manual)

$$E = \left(\frac{\Delta\sigma}{\Delta\varepsilon} \right)_{meas}$$

To accurately and precisely measure elastic modulus:

$$\sqrt{\langle \delta\sigma^2 \rangle} \ll \Delta\sigma$$

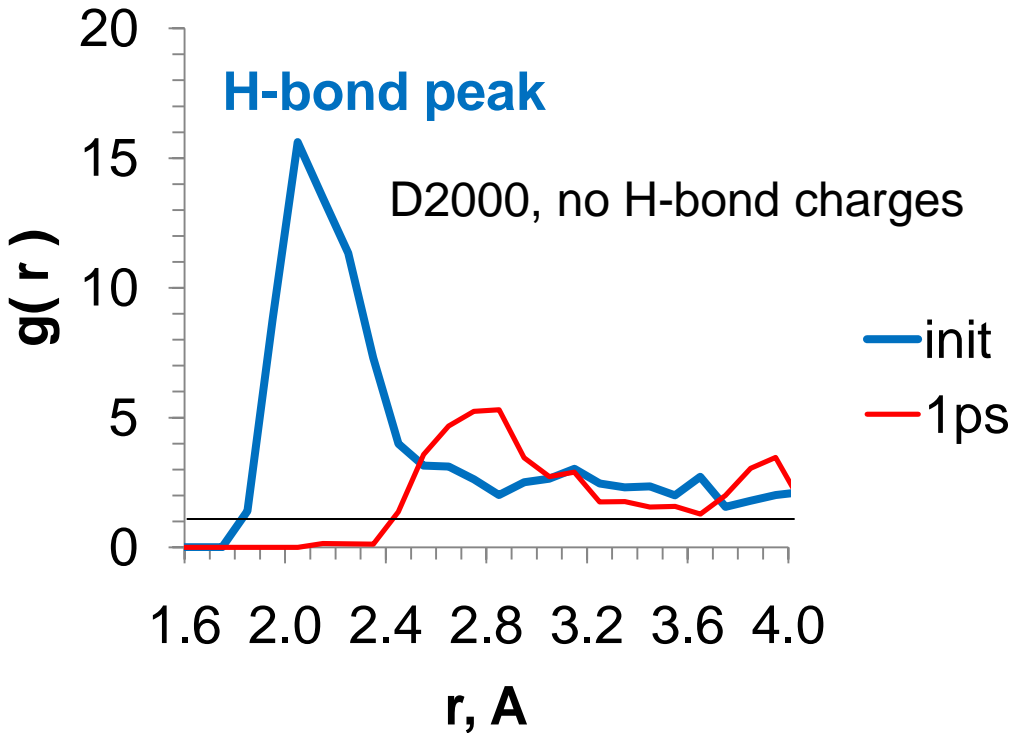
(stdev \ll magnitude)

Epoxy rubbery $E < \sim 10$ MPa, so ... $\Delta\sigma = E \cdot \Delta\varepsilon = (\sim 10\text{MPa})(\sim 0.01) = 1\text{bar}$

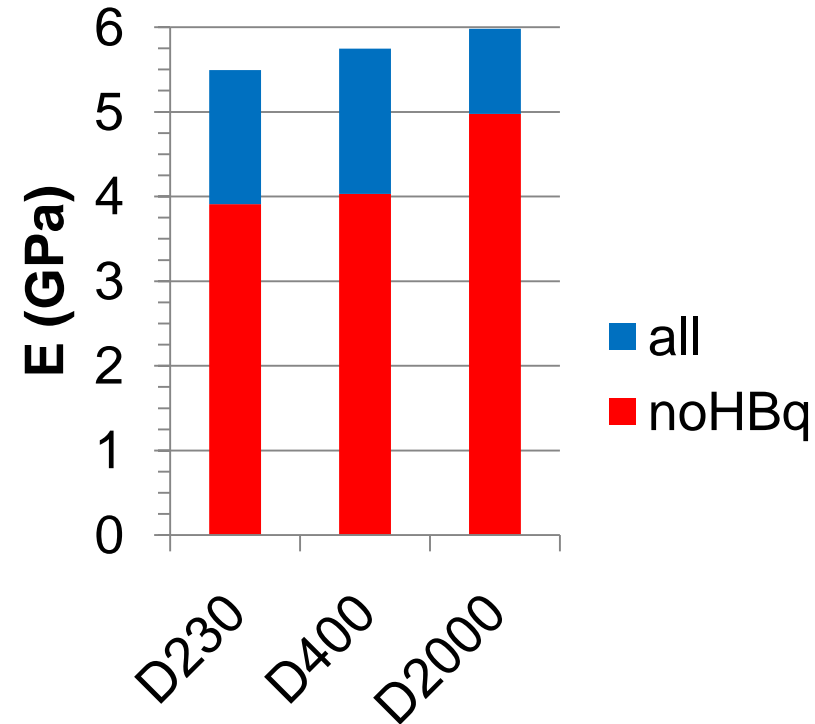
For $\sim 60\text{K}$ atoms, we measure: $\sqrt{\langle \delta\sigma^2 \rangle} \sim 30\text{bar}$

$$\sqrt{\langle \delta\sigma^2 \rangle} \leq \Delta\sigma \quad \text{if} \quad N = \frac{\langle \delta\sigma^2 \rangle_0}{\langle \delta\sigma^2 \rangle} \cdot N_0 = \frac{(30\text{bar})^2}{(1\text{bar})^2} \cdot (60\text{Katoms}) = 54\text{Matoms!}$$

H-O,N (-OH,-NH_x, x = 0,1,2)



glassy: T - T_g = -200 K



~1.5 GPa drop without H-bonds

(D,H,A) , E_{\min} (kcal/mol), r_{HA} (Å), θ_{D-H-A} (degrees)

- 1 (OH, HO, OH): (-2.29559, 1.85, 180)
- 2 (OH, HO, N): (-1.63628, 1.95, 180)
- 3 (OH, HO, NH): (-2.46018, 1.9, 180)
- 4 (OH, HO, NH2): (-3.40286, 1.85, 180)
- 5 (OH, HO, OE1): (-0.718034, 2, 180)
- 6 (OH, HO, OE2): (-1.23032, 1.9, 180)
- 7 (NH, HN, OH): (11.1487, 4, 180)
- 8 (NH, HN, N): (10.8725, 4, 180)
- 9 (NH, HN, NH): (14.189, 4, 180)
- 10 (NH, HN, NH2): (17.5055, 4, 180)
- 11 (NH, HN, OE1): (3.97717, 4, 180)
- 12 (NH, HN, OE2): (6.27921, 4, 180)
- 13 (NH2, HN, OH): (17.6293, 4, 180)
- 14 (NH2, HN, N): (17.195, 4, 180)
- 15 (NH2, HN, NH): (22.4308, 4, 180)
- 16 (NH2, HN, NH2): (27.6666, 4, 180)
- 17 (NH2, HN, OE1): (6.30295, 4, 180)
- 18 (NH2, HN, OE2): (9.93722, 4, 180)

minimum combination of Donor-Hydrogen-Acceptor:

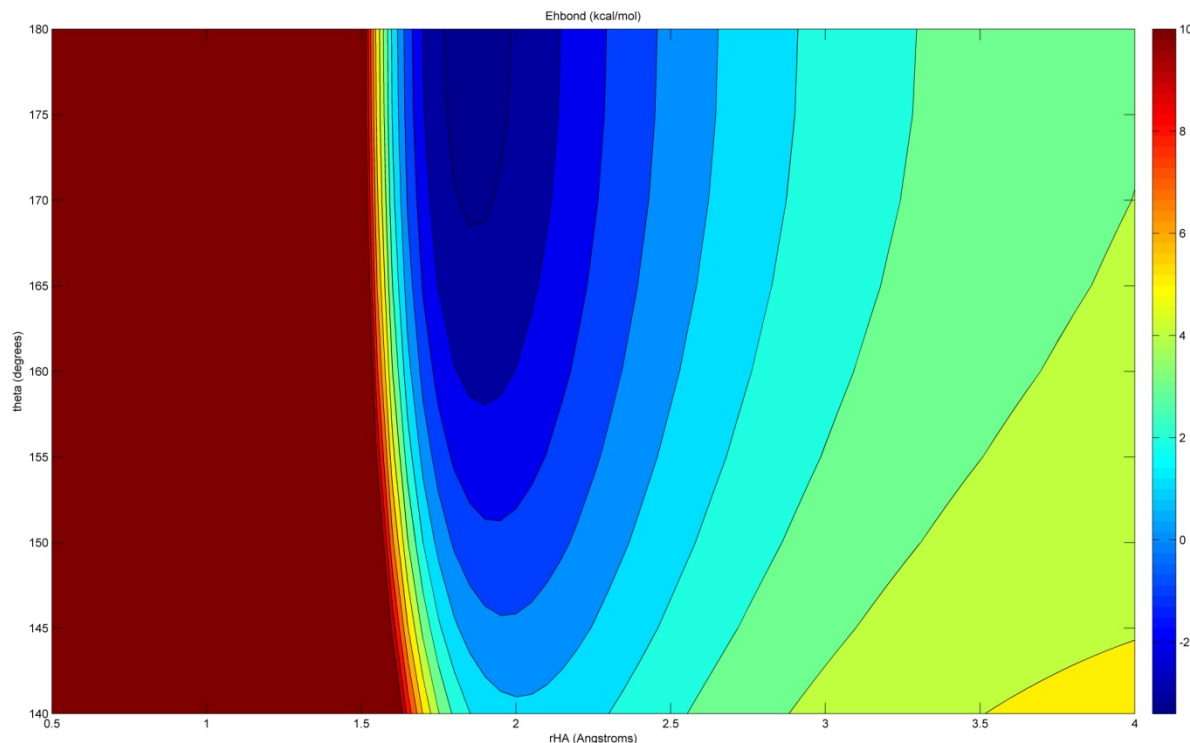
4 (OH, HO, NH2): (-3.40286, 1.85, 180)

Neglects local environment!

from MM (Coulomb + LJ of D-H...A only)

minimum in PotEng well

0.05 Å Δr_{HA} , 5 deg. $\Delta \theta$ scan



Contours w/ 1 kcal/mol spacing